

$$1/ Q_r = 4 \times 10^4 \text{ m}^3/\text{yr} \quad c_r = 30 \text{ } \mu\text{g/L} \quad - \text{Tributaries}$$

$$\text{Depth} = 2\text{m}, \text{ Surface Area } A = 10^4 \text{ m}^2, \quad c = 15 \text{ } \mu\text{g/L} \quad - \text{Bay}$$

$$c_0 = 0 \text{ } \mu\text{g/L} \quad - \text{sea}$$

$$k_d = 1 \text{ yr}^{-1}, \quad k_s = 0$$

~~(a) The pesticide concentration from tributaries is higher than its in the bay
 → mixing, will dilute the concentration. Together with its decay~~

(a) Pesticide from tributaries → bay, mixing & dilute, exchange with coastal area, decay → steady state concentration

Conc Pesticide in the bay is mixed with water from coastal area, concentration lower

~~$$(b) E' = \frac{Q(c_r - c)}{c - c_0} = \frac{4 \times 10^4 (30 - 15)}{15 - 0} = 4 \times 10^4$$~~

$$V \frac{dc}{dt} = W + Q(c_r - c) - kVc - E'(c - c_0)$$

$$\text{Steady state: } V \frac{dc}{dt} = 0 \Rightarrow E' = \frac{W + Q(c_r - c) - kVc}{c - c_0}$$

$$= \frac{0 + 4 \times 10^4 (30 - 15) - 1 \times (2 \times 10^4) \times 15}{15 - 0}$$

$$= 2 \times 10^4 \text{ m}^3/\text{yr}$$

$$(c) c' = 1.5 \text{ mg/L} = 1500 \text{ } \mu\text{g/L}$$

$$\frac{\text{m}^3}{\text{yr}} \times \frac{\mu\text{g}}{\text{L}} = 10^{-6} \frac{\text{kg}}{\text{yr}}$$

$$\text{Steady state: } 0 = W + Q(c_r - c') - kVc' - E'(c' - c_0)$$

$$\Rightarrow W = kVc' + E'(c' - c_0) - Q(c_r - c')$$

$$= 1 \times (2 \times 10^4) \times 1500 + 2 \times 10^4 (1500 - 0) - 4 \times 10^4 (30 - 1500)$$

$$= 118.8 \text{ kg/yr}$$

$$(d) T_c = \frac{1}{1/T_w + k_d} = \frac{1}{4 \times 10^4 / 2 \times 10^4 + 1} = \frac{1}{3} \text{ yr}$$

Assume instant mixing, $c_{\text{spill}} = \frac{m}{V} = \frac{100}{2 \times 10^4} = 5 \times 10^{-3} \text{ kg/m}^3 = 5 \text{ mg/L}$

Concentration in the bay after the spill:

$$c = c_{\text{initial}} + c_{\text{spill}} e^{-t/T_c}$$

$$= 15 \times 10^{-3} + 5 e^{-3t} \quad (\text{mg/L})$$

$$c = 1.5 \text{ mg/L} \Leftrightarrow 1.5 = 15 \times 10^{-3} + 5 e^{-3t}$$

$$\Leftrightarrow t = 0.405 \text{ yrs}$$

2/ (a) Estuary number η : imposed characteristic time $1/k$

Distance L_d for diffusion/dispersion $\sim (E/k)^{1/2}$

Distance L_a for advection $\sim U/k$

$$\text{ratio square given } \eta = kE/U^2 = \frac{L_d^2}{L_a^2} = \frac{\text{diffusive/dispersive distance}}{\text{advection distance}}$$

η : measures transport by dispersion relative to advection for non-conservative substance ($k > 0$) over a time scale $1/k$

$\eta \gg 1$: diffusion dominate $\eta \approx 1$: both $\eta \ll 1$: advection predominate

For conservative substance, Peclet number (Pe) should be used.

(b). At any time t , the distribution is symmetric & bell-shaped in space

+ maximum concentration is located at Ut unit of distance downstream

of the spill

• At any location x , the concentration as function of time is skewed

+ spreading increases during time period which the concentration is observed

+ \bar{x} is not well-defined

+ maximum concentration happens at $t = \frac{x}{U}$

At time $t=0$, the concentration is maximum at the part of spillage and it hasn't been spreaded

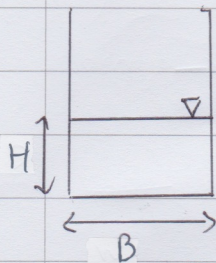
(c) (i) 95% encompassed $\Rightarrow 3.95 = 300$

$$\Leftrightarrow 3.9 \sqrt{2E_t t} = 300$$

$$\Leftrightarrow 3.9 \sqrt{2E_t \cdot 8} = 300$$

$$\Leftrightarrow E_L = 369.8 \text{ m}^2/\text{h} = 0.103 \text{ m}^2/\text{s}$$

(iii) Longitudinal dispersion coeff, $E_L = 0.011 \frac{U^2 B^2}{H U_*}$



$$R = \frac{A}{P} = \frac{BH}{B+2H} = \frac{45 \times 2}{45+2 \times 2} \approx 1.837 \text{ m}$$

$$U_* = \sqrt{gRS} = \sqrt{9.81 \times 1.837 \times 10^{-3}} = 0.134 \text{ m/s}$$

$$\Rightarrow U = \sqrt{\frac{E_L + \mu_*}{0.011 B^2}} = \sqrt{\frac{0.103 \times 2 \times 0.134}{0.011 \times 45^2}} = 0.035 \text{ m/s}$$

Distance needs to observe lateral concentration profile const to within $\sim 1\%$:

$$L_m = 0.4 \frac{UB^2}{E_t}$$

For natural rivers, $E_t = 0.6 H U_* = 0.6 \times 2 \times 0.134 = 0.161 \text{ m}^2/\text{s}$

$$\Rightarrow L_m = 0.4 \times \frac{0.023 \times 45^2}{0.161} \approx 115.71 \text{ m}$$

Location of measurement, $x = Ut = 0.035 \times 8 \times 60 \times 60 \approx 1 \text{ km}$

\Rightarrow No significant variation

$$\left. \begin{aligned} \text{(ii)} \quad \frac{m}{2\sqrt{\pi E_L t}} &= 50 \text{ mg/L} \\ &= 50 \text{ g/m}^3 \end{aligned} \right\} \Rightarrow \frac{\text{mass}}{90 \times 2 \times \sqrt{\pi \times 369.8 \times 8}} = 50$$

$$m = \frac{\text{mass}}{\text{Area}} = \frac{\text{mass}}{90} \Rightarrow \text{mass} = 867.65 \text{ kg}$$

$$3/(a) \quad c_c [ML^{-3}] \quad c_o [ML^{-3}] \quad Q_o [L^3 T^{-1}] \\ M_o [L^4 T^{-2}] \quad x [L]$$

$$n = 5, \quad m = 3 \Rightarrow 2 \pi \text{ groups}$$

Use c_c, c_o, x, Q_o as repeating variables

$$\pi_1 = c_c^a c_o^b x^c Q_o^d \\ = (ML^{-3})^a (ML^{-3})^b (L)^c (L^3 T^{-1})^d$$

$$\left. \begin{array}{l} M: 1 + a = 0 \\ L: -3 - 3a + b + 3c = 0 \\ T: -d = 0 \end{array} \right\} \Rightarrow \begin{array}{l} a = -1 \\ b = 0 \\ d = 0 \end{array}$$

$$\Rightarrow \pi_1 = \frac{c_c}{c_o}$$

$$\pi_2 = M_o^a c_o^b x^c Q_o^d \\ = (L^4 T^{-2})^a (ML^{-3})^b (L)^c (L^3 T^{-1})^d$$

$$\left. \begin{array}{l} M: a = 0 \\ L: 4 - 3a + b + 3c = 0 \\ T: -2 - d = 0 \end{array} \right\} \Rightarrow \begin{array}{l} a = 0 \\ b = 2 \\ d = -2 \end{array}$$

$$\Rightarrow \pi_2 = \frac{M_o x^2}{Q_o^2}$$

$$\Rightarrow \frac{c_c}{c_o} = f\left(\frac{M_o x^2}{Q_o^2}\right)$$

$$(b) \quad d = 0.1 \text{ m}$$

$$Q_o = w_o A = w_o \pi \frac{d^2}{4} = 0.0157 \text{ m}^3/\text{s}$$

$$w_o = 2 \text{ m/s}$$

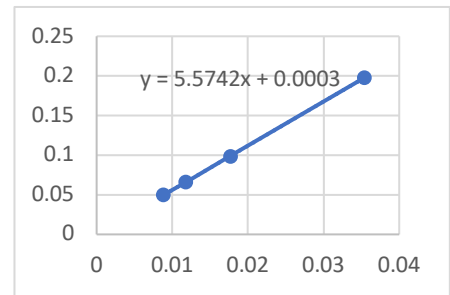
$$M_o = w_o Q_o = 0.0314 \text{ m}^4/\text{s}^2$$

$$c_o = 1000 \text{ mg/L}$$

(b)

x [m]	C_c [mg/L]	C_c / C_o	$M_o x^2 / Q_o^2$	$Q_o^2 / M_o x^2$	$Q_o / M_o^{1/2} x$
2.5	198	0.198	795.7747	0.001257	0.035449
5	99	0.099	3183.099	0.000314	0.017725
7.5	66	0.066	7161.972	0.00014	0.011816
10	50	0.05	12732.4	7.85E-05	0.008862

$Q_o = 0.015708 \text{ m}^3/\text{s}$ $M_o = 0.031416 \text{ m}^4/\text{s}^2$ $C_o = 1000 \text{ mg/L}$



⇒ Coefficient = 5.5742

(c) CMC: protect against acute or lethal effects (in a brief period of time) – immediate effect

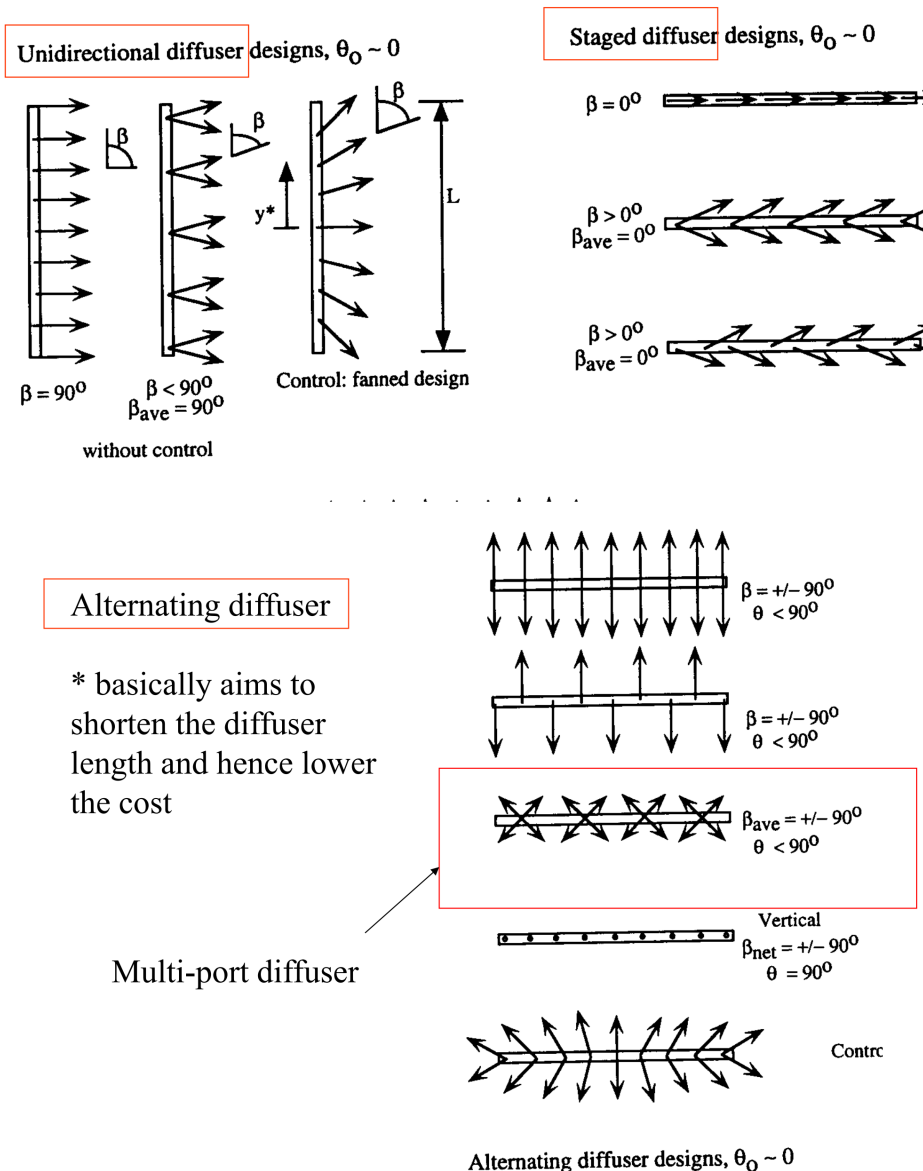
CCC: protect against chronic effects (in contact for a long period of time) – long-term effect

CMC \geq CCC, and is more restrictive

CCC “must” be at the edge of the regulatory mixing zone

(d) The analysis is inappropriate. The relationship in (b) only applies to the zone of established flow, not near the discharge location.

4. (a)



$$4 | (b) w_0 = \frac{Q_0}{A} = \frac{10}{10 \times 0.1} = 10 \text{ m/s}$$

$$\text{2D jet: } q_0 = w_0 b = 10 \times 0.1 = 1 \text{ m}^2/\text{s}$$

$$M_0 = q_0 w_0 = 10 \text{ m}^3/\text{s}^2$$

$$\frac{c_c}{c_0} = 2.4 q_0 M_0^{-1/2} z^{-1/2} = 2.4 \times 1 \times 10^{-1/2} \times 20^{-1/2} \approx 0.1697$$

$$\Rightarrow c_c = 0.1697 c_0 \approx 0.1697 \times 600 = 101.82 \text{ ppm} \Rightarrow \text{doesn't meet requirement}$$

$$(c) \text{ No of parts} = 2 \Rightarrow Q_0 = \frac{10}{2} = 5 \text{ m}^3/\text{s} \left. \vphantom{\begin{array}{l} \text{No of parts} \\ Q_0 \end{array}} \right\} \Rightarrow A = \frac{Q_0}{w_0} = \frac{5}{10} = 0.5 \text{ m}^2$$

$$w_0 = 10 \text{ m/s}$$

$$M_0 = w_0^2 A = 10^2 \times 0.5 = 50 \text{ m}^4/\text{s}^2$$

$$\frac{c_c}{c_0} = 5.6 Q_0 M_0^{-1/2} z^{-1} = 5.6 \times 5 \times 50^{-1/2} \times 20^{-1} = 0.198$$

$$\Rightarrow c_c = 118.8 \text{ ppm} \Rightarrow \text{doesn't meet}$$

$$(d) \text{ No interference: } S_N > b_c = 0.127 z = 0.127 \times 20 = 2.54 \text{ m}$$

* (need to check with Prof) !!!

$$\Rightarrow \text{No of parts} < \frac{L}{S_N} = \frac{10}{2.54} \approx 4.9$$

$$\Rightarrow N = 4 \Rightarrow S_N = \frac{L}{N-1} = \frac{10}{4-1} = 3.33 \text{ m}$$

$$Q_0 = \frac{10}{4} = 2.5 \text{ m}^3/\text{s}; w_0 = 10 \text{ m/s} \Rightarrow A = \frac{Q_0}{w_0} = 0.25 \text{ m}^2$$

$$M_0 = w_0^2 A = 10^2 \times 0.25 = 25 \text{ m}^4/\text{s}^2$$

$$\frac{c_c}{c_0} = 5.6 Q_0 M_0^{-1/2} z^{-1} = 5.6 \times 2.5 \times 25^{-1/2} \times 20^{-1} = 0.14$$

$$\Rightarrow c_c = 84 \text{ ppm} < 100 \text{ ppm} \text{ (Meet standards !!)}$$