

NANYANG TECHNOLOGICAL UNIVERSITY
SEMESTER 1 EXAMINATION 2015-2016
CV4102 - ADVANCED STEEL DESIGN

November/December 2015

Time Allowed: 2½ hours

INSTRUCTIONS

1. This paper contains **FOUR (4)** questions and comprises **SIX (6)** pages.
 2. Answer **ALL FOUR (4)** questions.
 3. This paper is an Open Book Examination.
 4. All questions carry equal marks.
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1. Figure Q1 shows a K-joint fabricated using (SHS) square hollow section members, together with the loading conditions, detailed specifications and dimensions of the members. Use design recommendations given in Eurocode 3, EN-1993, Part 1-8: 2005,
 - (a) Check if the joint parameters satisfy the ranges of validity. Hence, calculate the joint strength if the compressive stress in the chord $\sigma_{0,Ed} = 0.6f_{y0}$, and state the critical failure mechanism. (12 Marks)
 - (b) Recalculate the joint strength if the compressive stress in the chord is increased to 90% of the design strength, i.e. $\sigma_{0,Ed} = 0.9f_{y0}$, and discuss the effect of increasing and decreasing its magnitude and direction. (8 Marks)
 - (c) What is the limit of g when the K-joint can be considered as two separate Y-joints? (5 Marks)

Note: Question 1 continues on Page 2

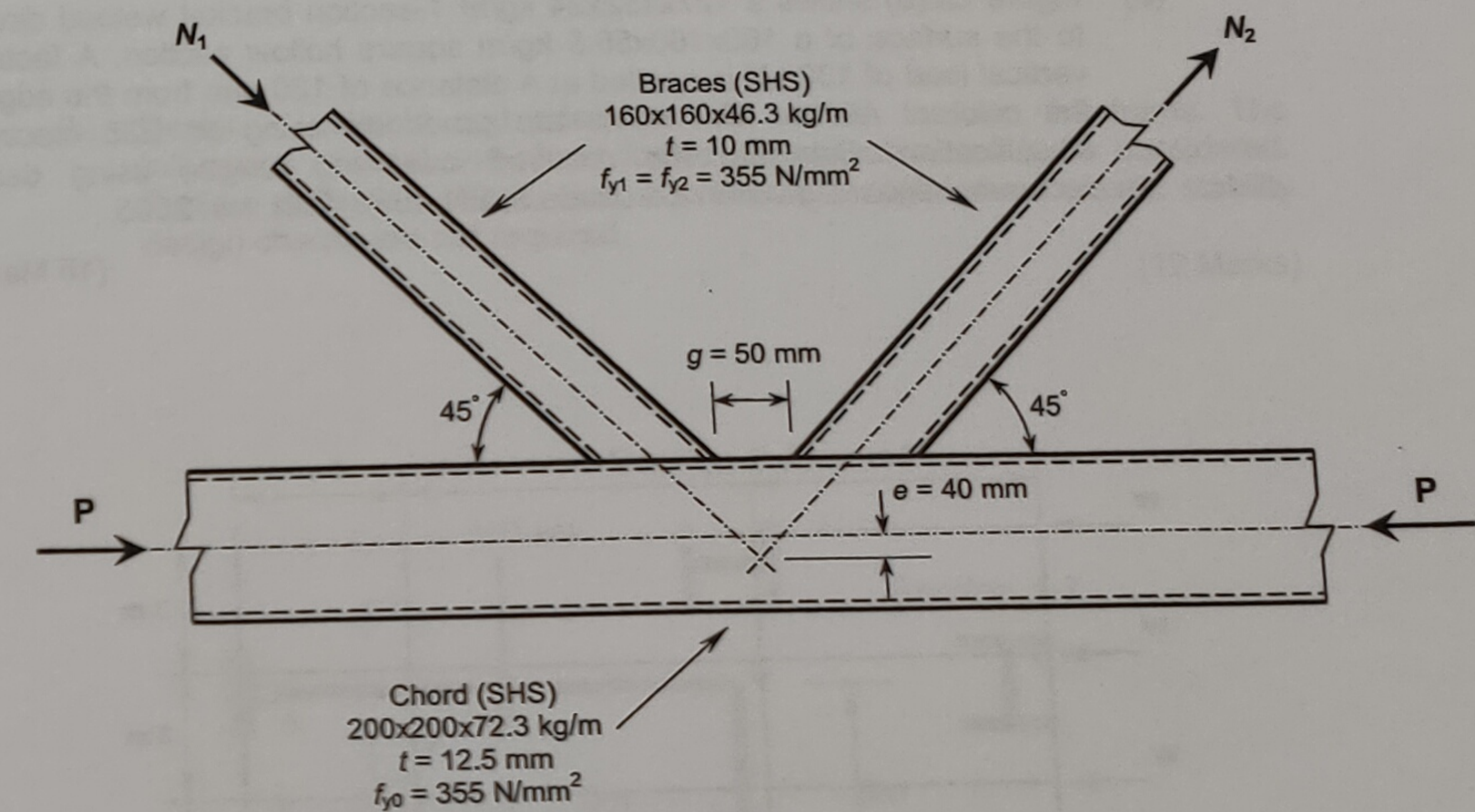
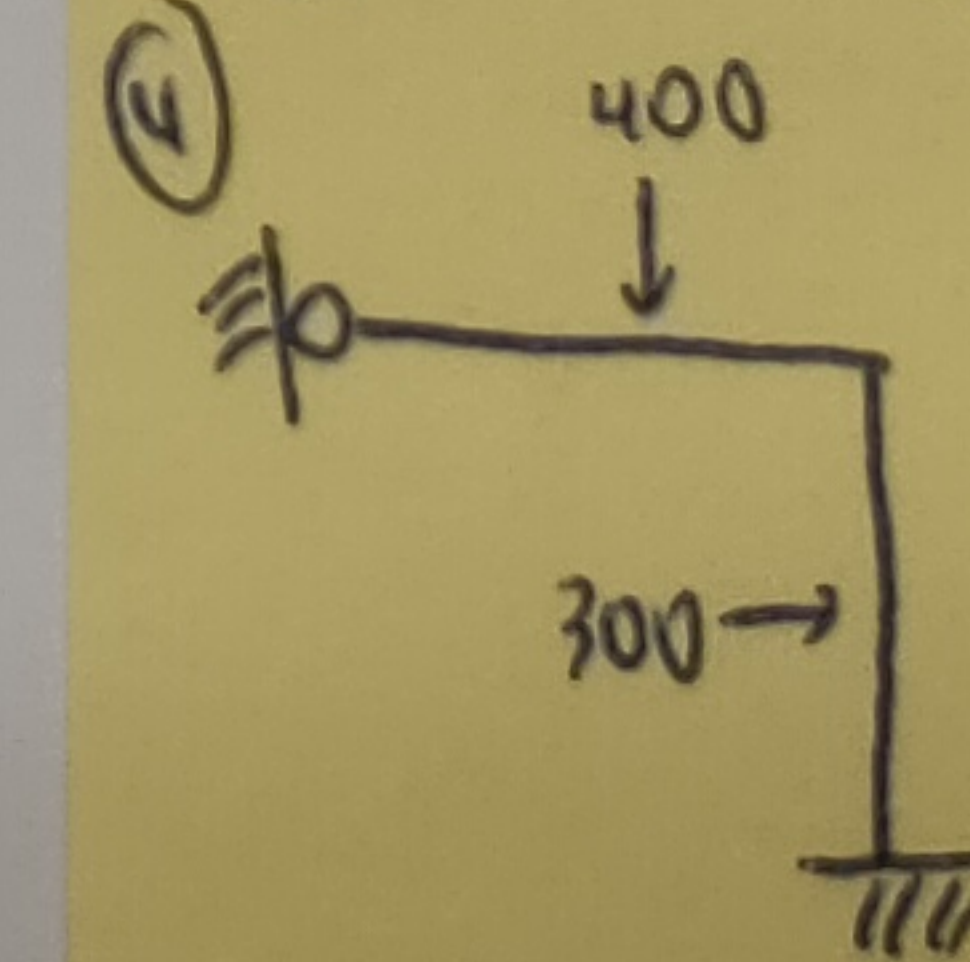
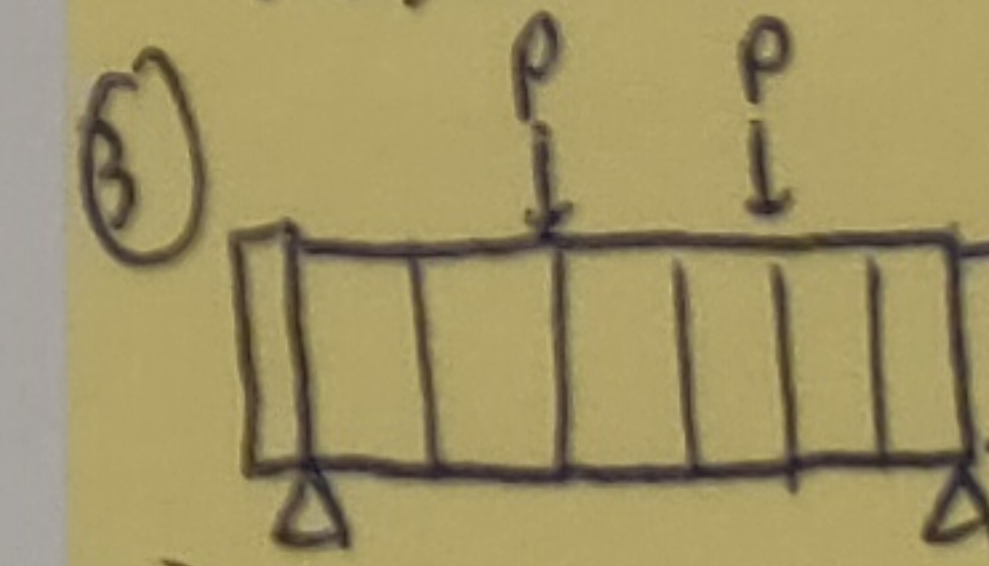


Figure Q1

(Note: drawings are not drawn to scale)

① K-gap SHS
② Portal Frame
Assume 1 mm weld throat



2. (a) A seven-storey rigid frame shown in Figure Q2(a) is subjected to factored horizontal wind load, w equal to 3 kN. The columns are fixed at the base. Using the portal frame method, calculate the axial force, shear force and bending moment of column marked A. (10 Marks)

- (b) Figure Q2(b) shows a 127x152x24 kg/m T-section bracket welded directly to the surface of a 160x160x56.5 kg/m square hollow section. A factored vertical load of 130 kN is applied at a distance of 120 mm from the edge of the column. All the fillet welds are produced using an E35 electrode classification. Calculate the required weld leg length, using design recommendations given in Eurocode 3, EN-1993, Part 1-8: 2005. (15 Marks)

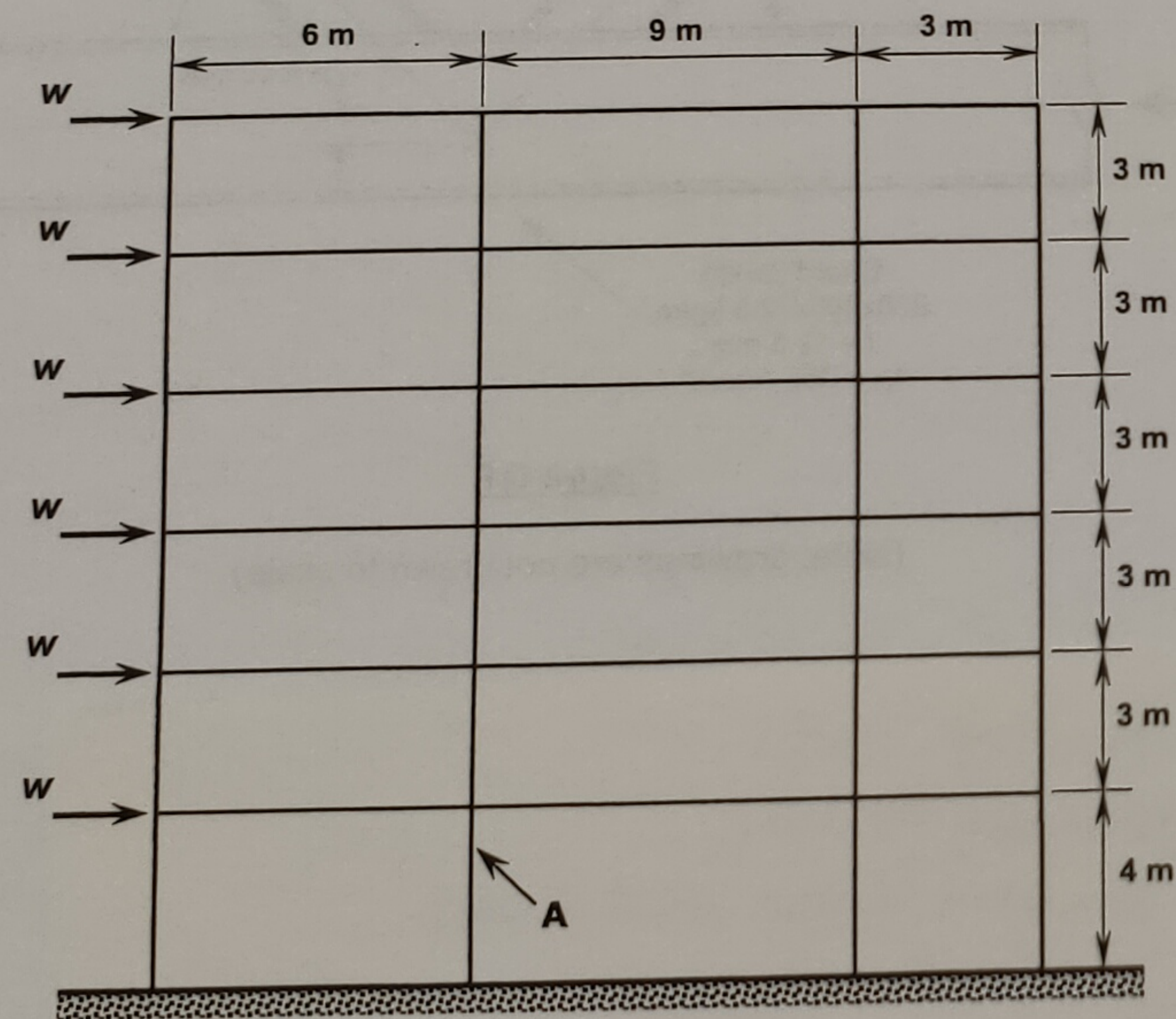


Figure Q2(a)

(Note: drawings are not drawn to scale)

Note: Question 2 continues on Page 4

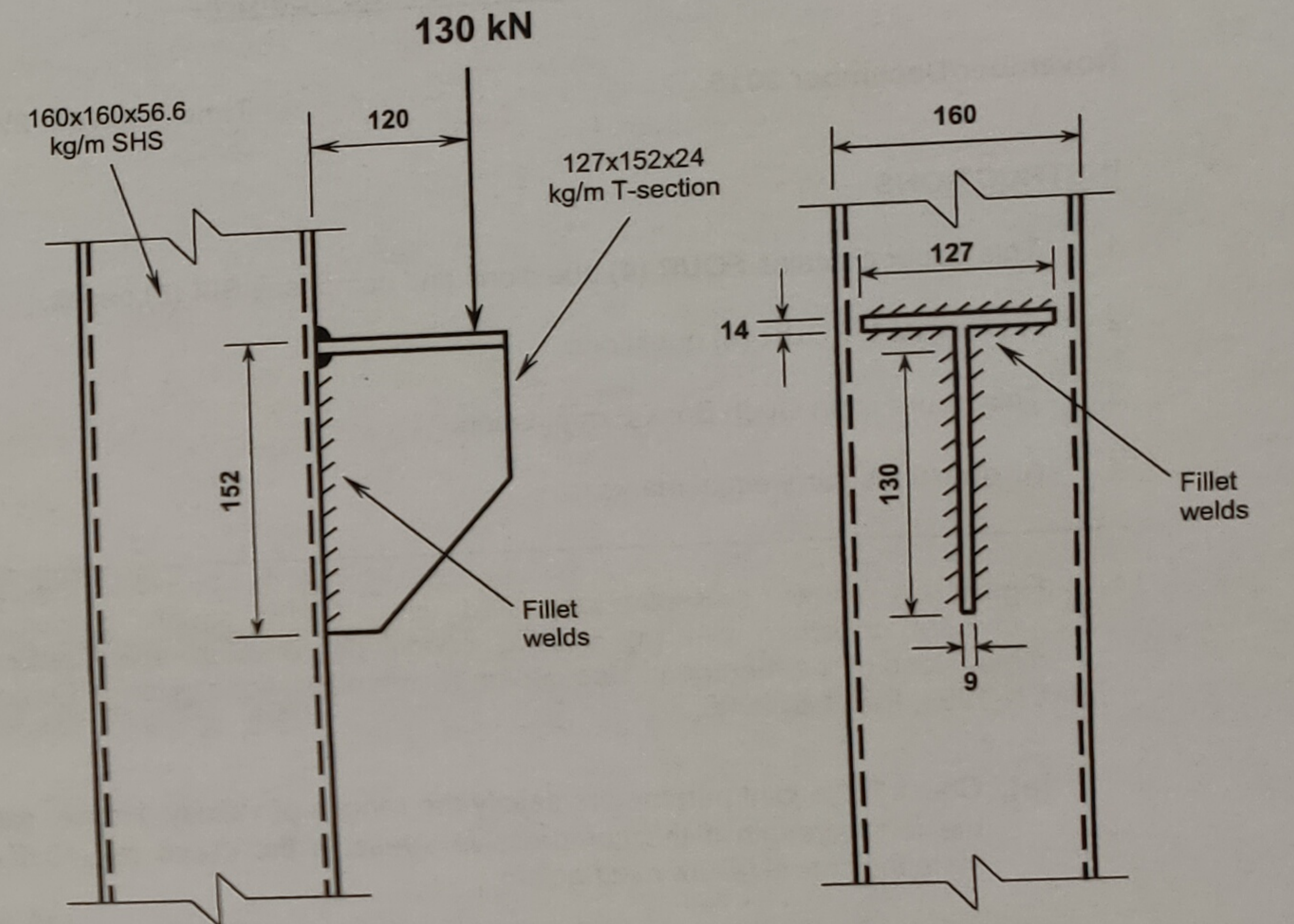


Figure Q2(b)

(Note: drawings are not drawn to scale)

(All dimensions are in mm unless otherwise stated)

3. The 24 m span simply-supported plate girder shown in Figure Q3(a) is fabricated from Grade S275 steel plates throughout. The girder is simply supported at the rigid end posts A and D, and effectively restrained in the lateral direction along the entire girder. It is supporting two (2) factored design concentrated loads, each P kN acting at the intermediate stiffeners B and C. Details of the rigid end posts at A and D and the stiffeners at B and C are shown in Figure Q3(b).

- Classify the flanges and the web of the plate girder.
- Compute the bending resistance of the plate girder.
- Compute the shear resistance of the plate girder.
- Compute the load bearing resistance of the rigid end posts at A and D.
- Compute the load bearing resistance of the stiffeners at B and C.
- What is the allowable load P ?

(25 Marks)

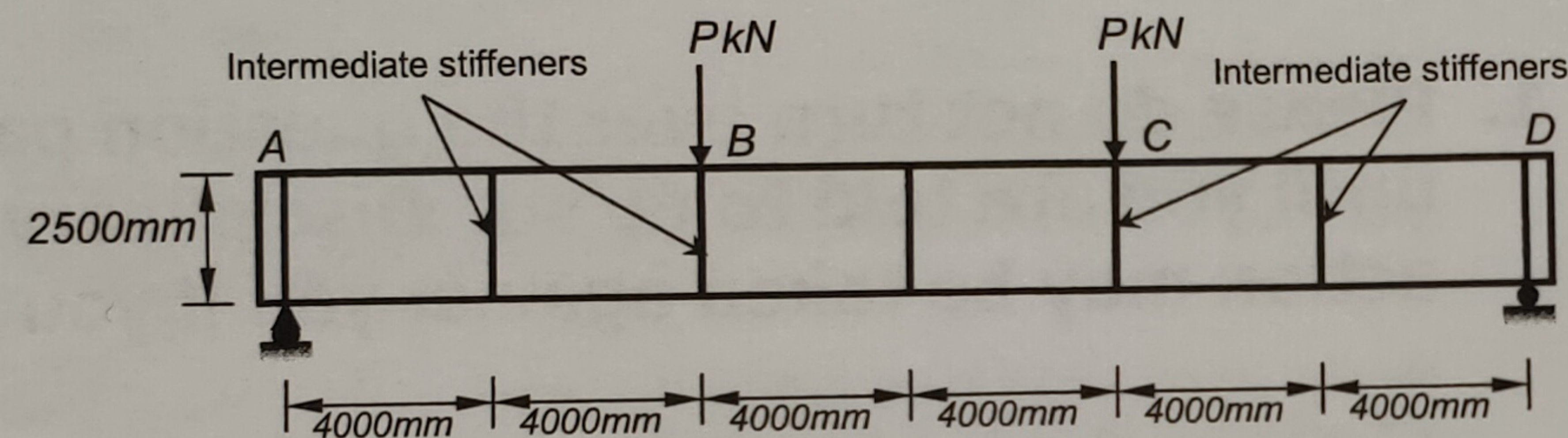
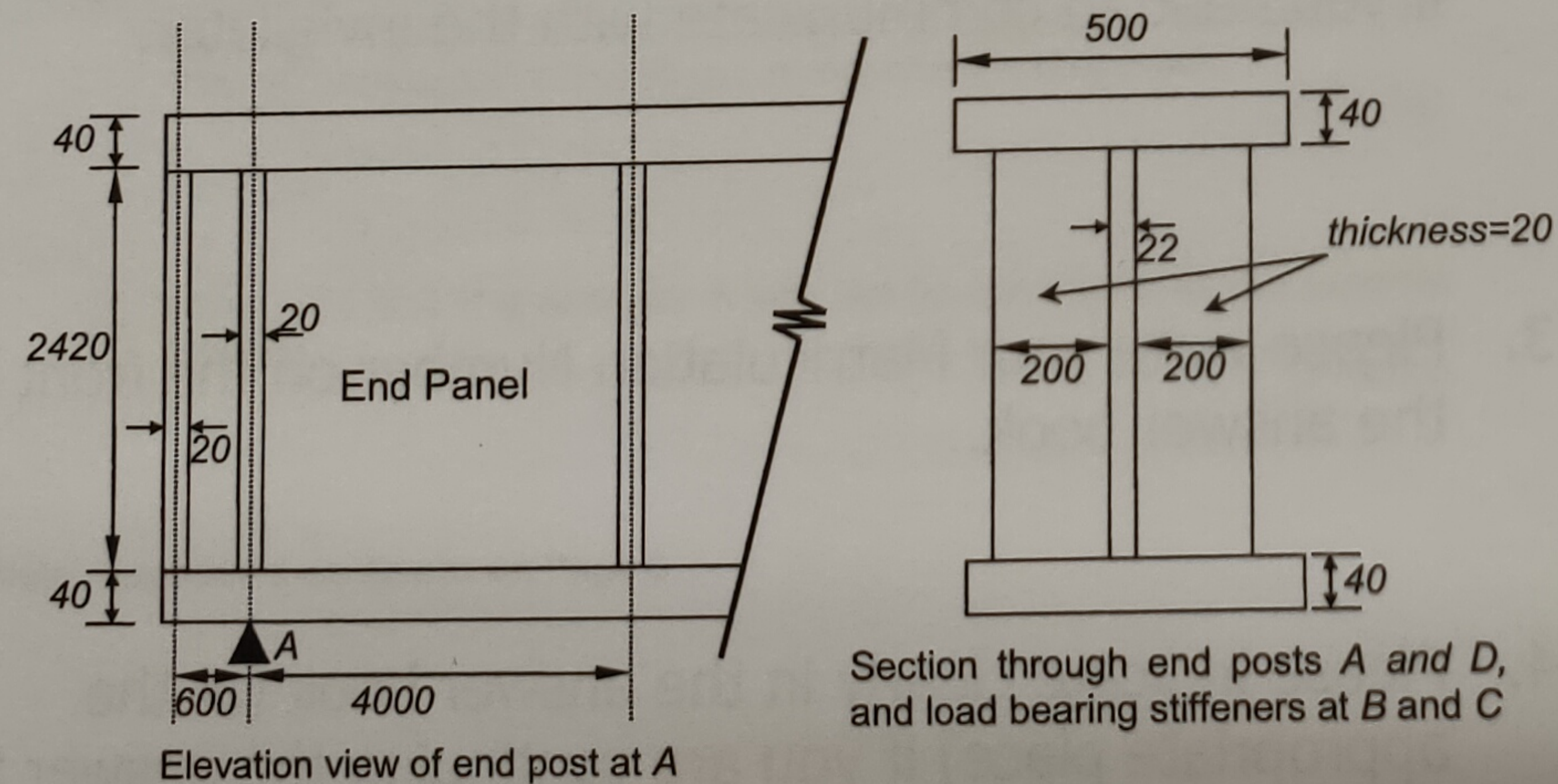


Figure Q3(a)



Elevation view of end post at A

Note:

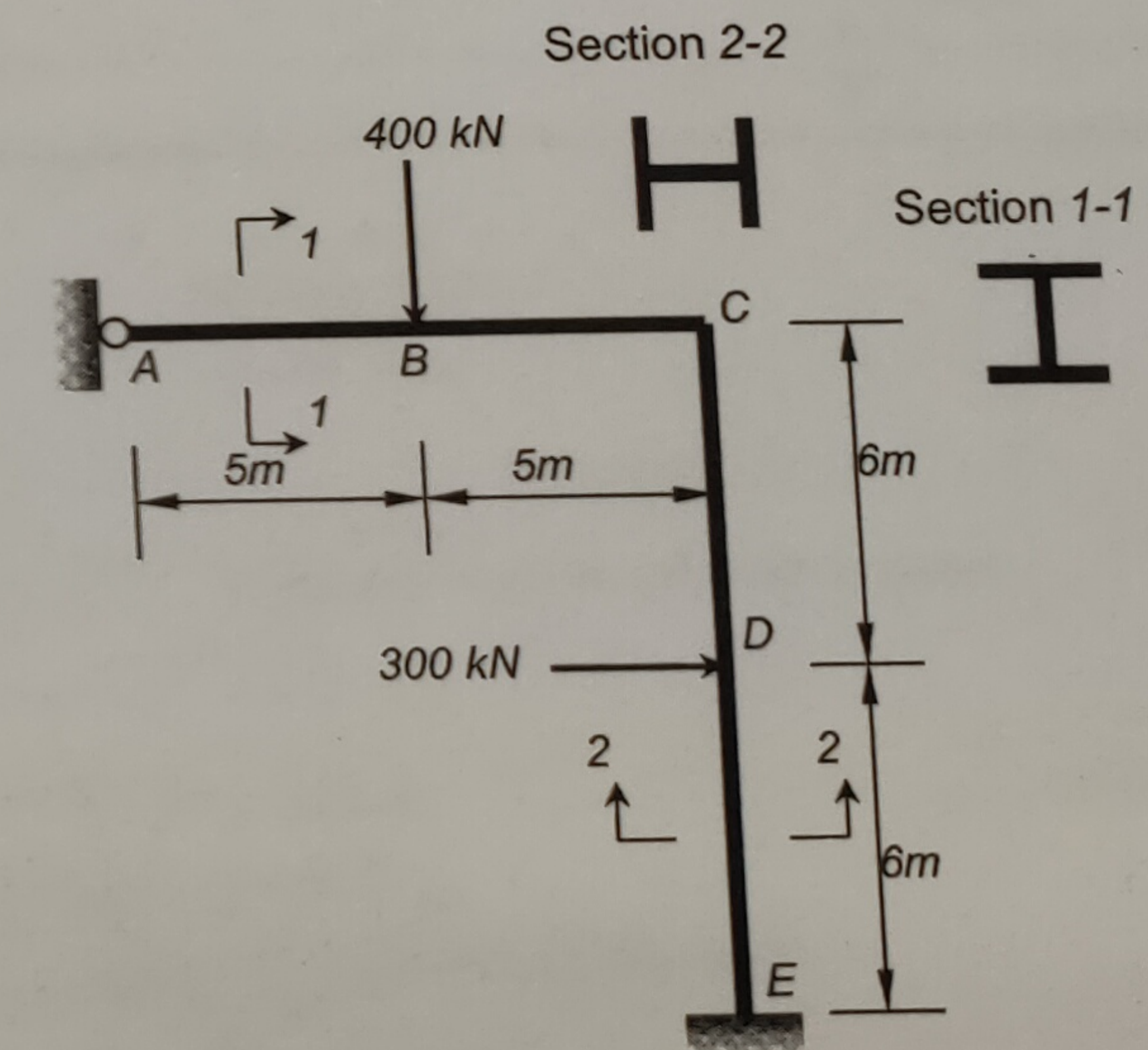
- Elevation details for end post at D are identical to the end post at A.
- All dimensions in mm.

Figure Q3(b)

4. The frame shown in Figure Q4 is pinned at A and fixed at E, and is subjected to factored design concentrated loads at B and D. It is fabricated using uniform S355 steel section throughout. Adequate restraints against stability are provided.

- Calculate the required plastic moment of resistance for the frame. Show clearly how you ensure the correctness of your solution. (13 Marks)

- Design a suitable and adequate UB section to form the frame. The influences of axial and shear forces, if applicable, are to be considered. Further deflection check, and in-plane and out-of-plane plastic stability design checks are not required. (12 Marks)



1) a) $\gamma = \frac{b_0}{2t_0} = \frac{200}{2(12.5)} = 8$

$\beta = \frac{b_1+b_2}{2b_0} = \frac{160+160}{2(200)} = 0.8$

Ranges of validity,

$\frac{b_1}{b_0} = \frac{b_2}{b_0} = \frac{160}{200} = 0.8 \geq 0.35$
 $\geq 0.1 + 0.01 \frac{b_0}{t_0}$
 $= 0.1 + 0.01 \left(\frac{200}{12.5}\right)$
 $= 0.26$

Brace in compression (N_c)

$\frac{h_1}{t_1} = \frac{b_1}{t_1} = \frac{160}{10} = 16 \leq 35 \leq 38\epsilon = 30.932$ (class 2, ok)

Brace in tension

$\frac{b_2}{t_2} = \frac{h_2}{t_2} = \frac{160}{10} = 16 \leq 35$

$0.5 \leq \frac{h_0}{b_0} = \frac{h_1}{b_1} = \frac{h_2}{b_2} = 1.0 \leq 2.0$

$\frac{b_0}{t_0} = \frac{h_0}{t_0} = \frac{200}{12.5} = 16 \leq 35 \leq 38\epsilon$ (class 2, ok)

$g = 50 \text{ mm}$

$\frac{g}{b_0} = \frac{50}{200} = 0.25$

$0.5(1-\beta) = 0.5(1-0.8) = 0.1$

$1.5(1-\beta) = 1.5(1-0.8) = 0.3$

$0.1 < \frac{g}{b_0} = 0.25 < 0.3$

$t_1 + t_2 = 10 + 10 = 20 \text{ mm}$

$g = 50 \text{ mm} \gg t_1 + t_2 \parallel$

★ For SHS,

$0.6 \leq \frac{b_1+b_2}{2b_1} = \frac{160+160}{2(160)} = 1.0 \leq 1.3$

$\frac{b_0}{t_0} = \frac{200}{12.5} = 16 \geq 15$

∴ Table 7.10 can be used.

$\beta \leq 1.0$

$N_{1,Rd} = \frac{8.9 \gamma^{0.5} k_n f_y t_0^2}{\sin \theta_1} \left(\frac{b_1+b_2}{2b_0}\right) / \gamma_{MS}$

Given $\sigma_{0,Ed} = 0.6 f_y$

$n = \frac{\sigma_{0,Ed}}{f_y} > 0$

$k_n = 1.3 - \frac{0.4(0.6)}{0.8} \leq 1.0$
 $= 1.0$

$N_{1,Rd} = \frac{8.9(8)^{0.5}(1)(355)(10)^2}{\sin 45^\circ} \left(\frac{160+160}{2(200)}\right) / 1.0$

$= 1579.75 \text{ kN}$

Since $\theta_1 = \theta_2 = 45^\circ$

$N_{2,Rd} = 1579.75 \text{ kN}$

$A_2 f_{y2} = A_1 f_{y1} = \frac{\pi}{4} \{160^2 - 140^2\} (355)$
 $= 1672.9 \text{ kN}$

⇒ chord face failure

b) $\sigma_{0,Ed} = 0.9 f_y$

$n = \frac{\sigma_{0,Ed}}{f_y} = 0.9 > 0$ (compression)

$k_n = 1.3 - \frac{0.4(0.9)}{0.8} \leq 1.0$
 $= 0.85$

$N_{1,Rd} = \frac{8.9 \gamma^{0.5} k_n f_y t_0^2}{\sin \theta_1} \left(\frac{b_1+b_2}{2b_0}\right) / \gamma_{MS}$

$= \frac{8.9(8)^{0.5}(0.85)(355)(12.5)^2}{\sin 45^\circ} \left(\frac{160+160}{2(200)}\right) / 1.0$

$= 1342.79 \text{ kN}$

since $\theta_1 = \theta_2 = 45^\circ$

$N_{2,Rd} = 1342.79 \text{ kN}$

★ By increasing the magnitude of the compressive strength, n value, where $n = \frac{\sigma_{0,Ed}}{f_y}$ will increase and this causes the k_n value to further decrease. As $N_{1,Rd}$ & k_n , a decrease in k_n results in a decrease in $N_{1,Rd}$, the resistance of the brace towards chord face failure.

If the direction is change to negative, means the chord is under tension, k_n will be equal to 1.0 and $N_{1,Rd}$ value will be 1579.75 kN.

c) For SHS, the joint can be treated as two separated T or Y joints if $g/b_0 > 1.5(1-\beta)$

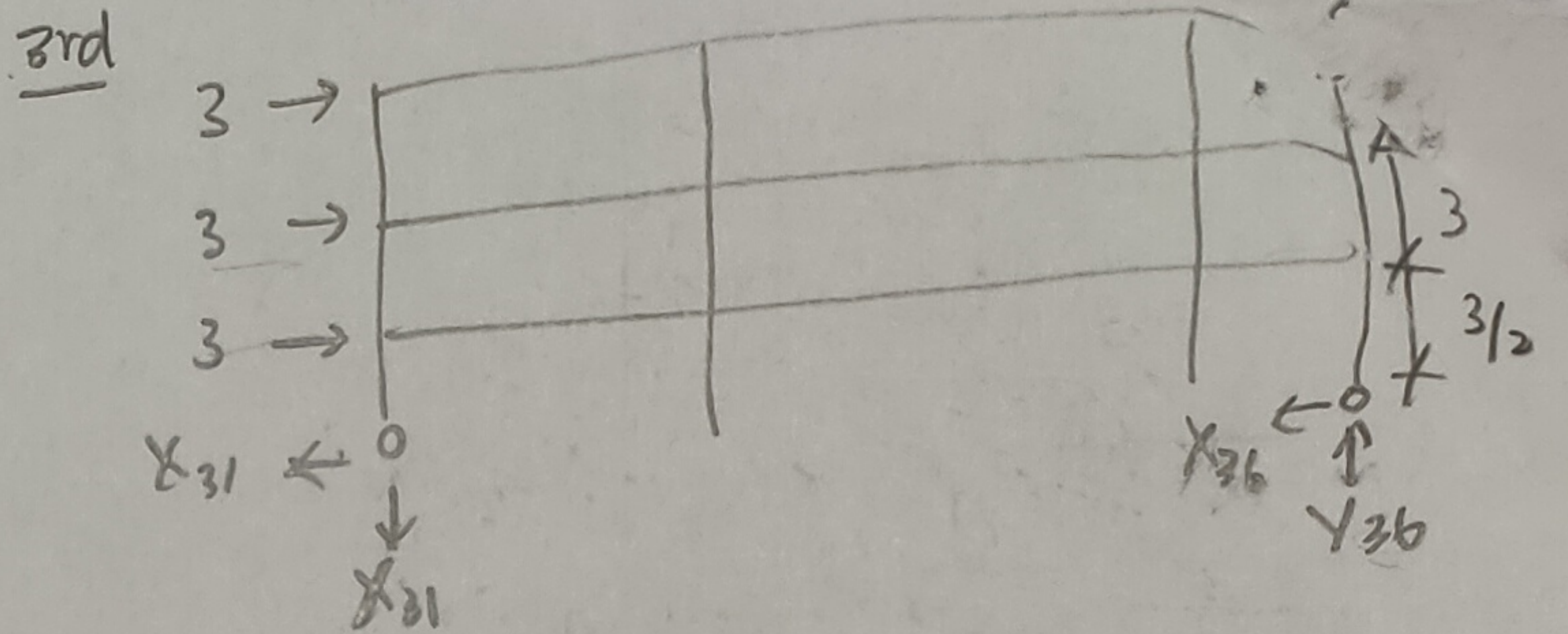
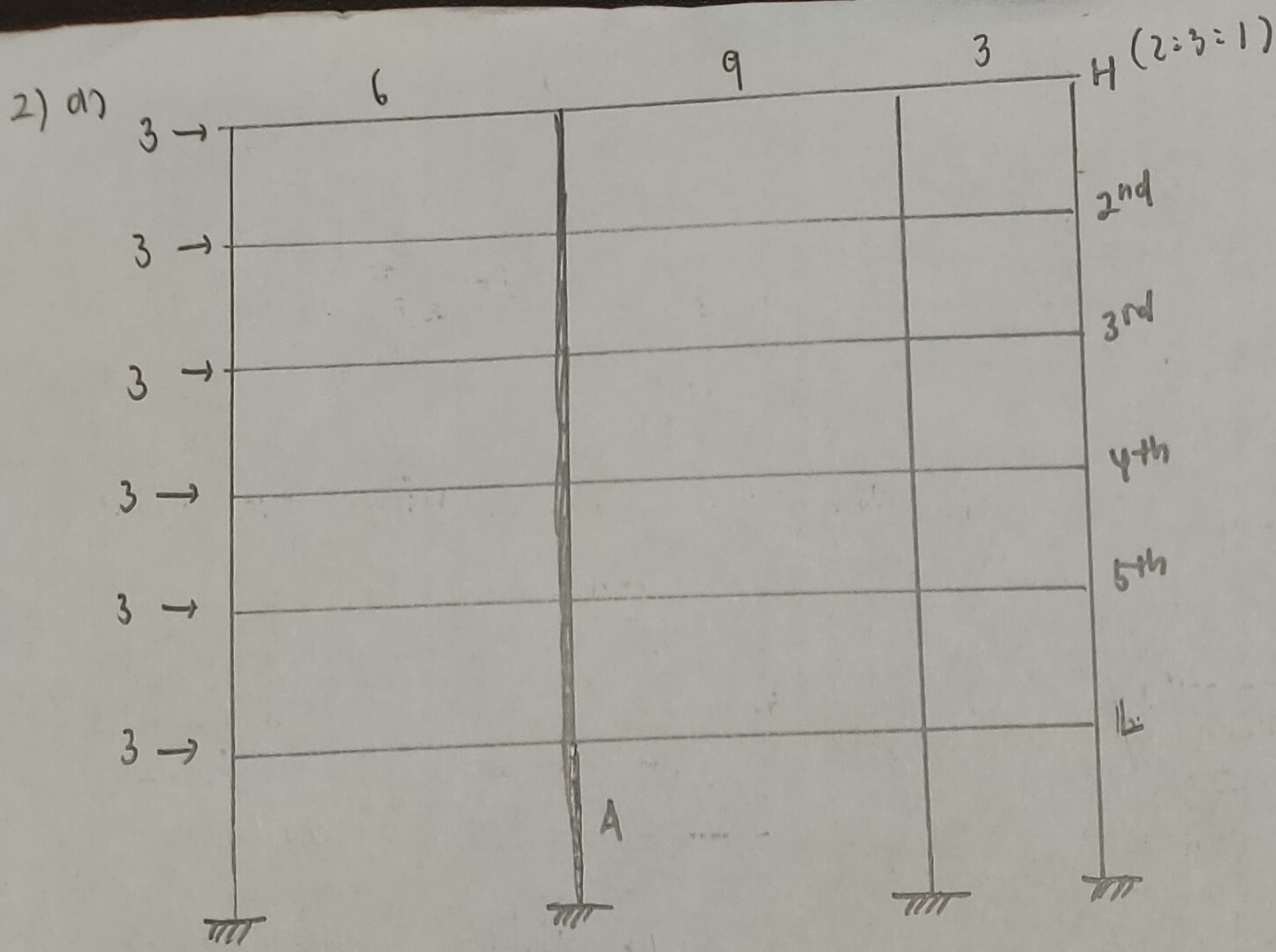
in this case,

$\frac{g}{b_0} > 1.5(1-\beta)$

$\frac{g}{200} > 1.5(1-0.8)$

$g > 0.3(200)$

$g > 60 \text{ mm} \parallel$

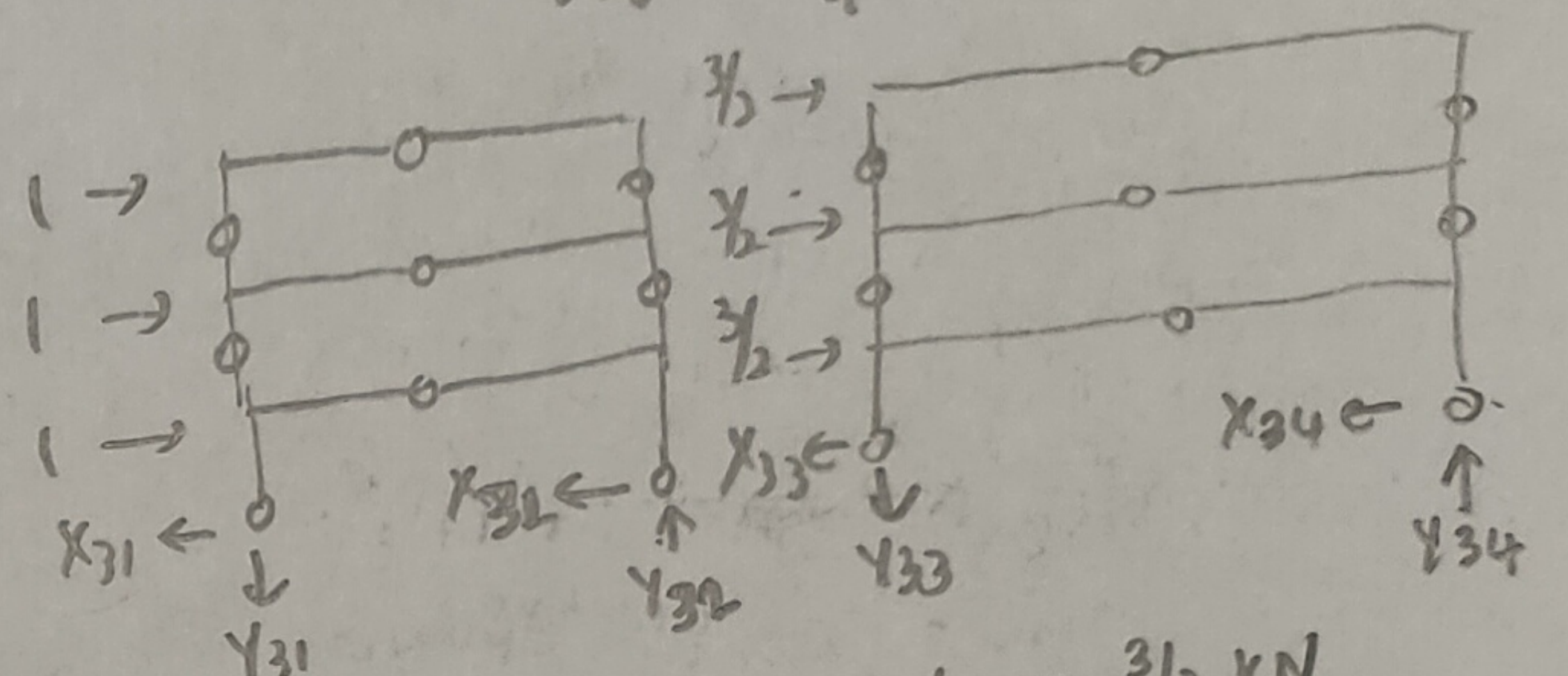


3rd

$$Y_{31} = Y_{36}$$

$$\sum M_{31} = 0 \quad 3(3+3+3/2) + 3(3+3/2) + 3(3/2) = (3+6+9)Y_{36}$$

$$Y_{36} = \frac{9}{4} \text{ kN}$$



$$X_{31} = X_{32} = (1+1+1)/2 = 3/2 \text{ kN}$$

$$X_{33} = X_{34} = (3/2+3/2+3/2)/2 = 9/4 \text{ kN}$$

By Induction.

4th storey $\Rightarrow Y_{46} = Y_{41} = \frac{3(3+3+3+3/2) + 3(3+3+3/2) + 3(3/2)}{3+6+9} = 4 \text{ kN}$

5th storey $\Rightarrow Y_{56} = Y_{51} = \frac{3(3+3+3+3+3/2) + 3(3+3+3+3/2) + 3(3+3+3/2) + 3(3/2)}{3+6+9} = 6.25 \text{ kN}$

$$X_{41} = X_{42} = (1+1+1+1)/2 = 2 \text{ kN}$$

$$X_{43} = X_{44} = (3/2+3/2+3/2+3/2)/2 = 3 \text{ kN}$$

$$X_{51} = X_{52} = (1 \times 5)/2 = 5/2 \text{ kN}$$

$$X_{53} = X_{54} = (3/2 \times 5)/2 = 15/4 \text{ kN}$$

Lowest storey.

$$Y_{61} = Y_{66}$$

$$\sum N_{66} = 0 \quad 3(3+3+3+3+3+2) + 3(3+3+3+3+2) + 3(3+3+3+2) + 3(3+3+2) + 3(3+2) + 3(2) = Y_{66}(3+6+9)$$

$$Y_{66} = \frac{23}{3} \text{ kN}$$

$$X_{61} = X_{62} = (1 \times 6)/2 = 3 \text{ kN}$$

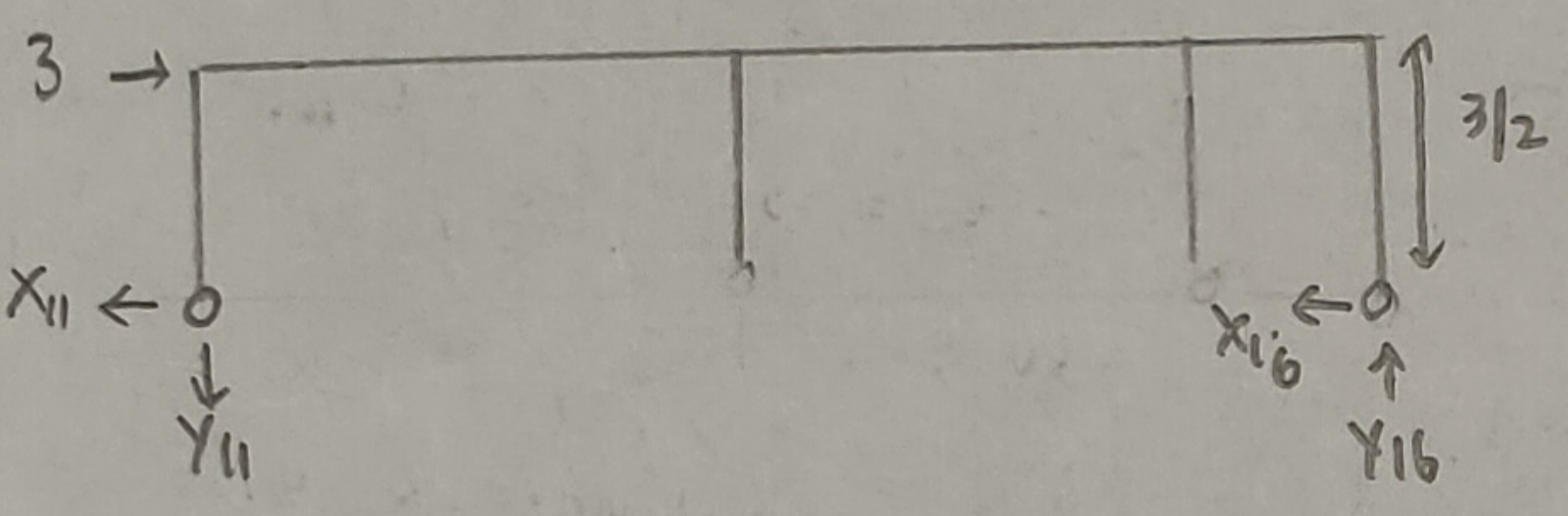
$$X_{63} = X_{64} = (3/2 \times 6)/2 = 9/2 \text{ kN}$$

Column A

	shear	Axial
H	$X_{12} + X_{13} = 5/4$	0
2	$X_{22} + X_{23} = 5/2$	0
3	$X_{32} + X_{33} = 15/4$	0
4	$X_{42} + X_{43} = 5$	0
5	$X_{52} + X_{53} = 25/4$	0
L	$X_{62} + X_{63} = 15/2$	0

inner column

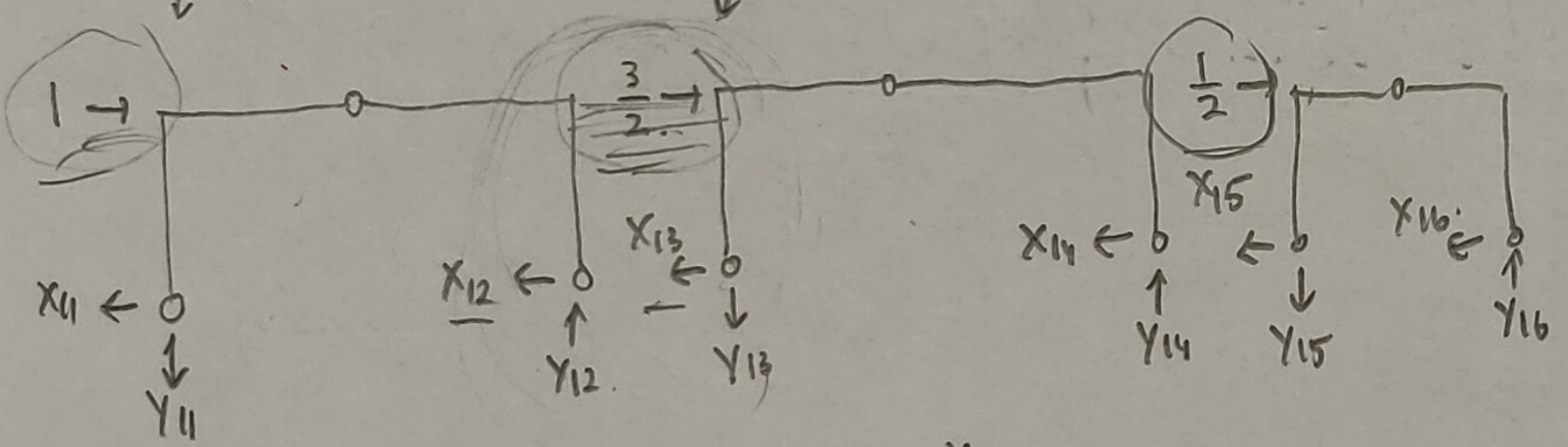
Start with highest storey



$$Y_{11} = Y_{16}$$

$$\sum M_{11} = 0 \quad 3(3/2) = (3+9+6)Y_{16}$$

$$Y_{16} = \frac{9}{18} \times 3 = \frac{9}{18} \times 3 = \frac{9}{6} \times 3 = \frac{9}{2} \times 3 = \frac{27}{2} \text{ kN}$$



* $Y_{11} = Y_{12} = Y_{13} = Y_{14} = Y_{15} = Y_{16}$

Using symmetry,

$$X_{11} = X_{12} = \frac{1}{2} \text{ kN}$$

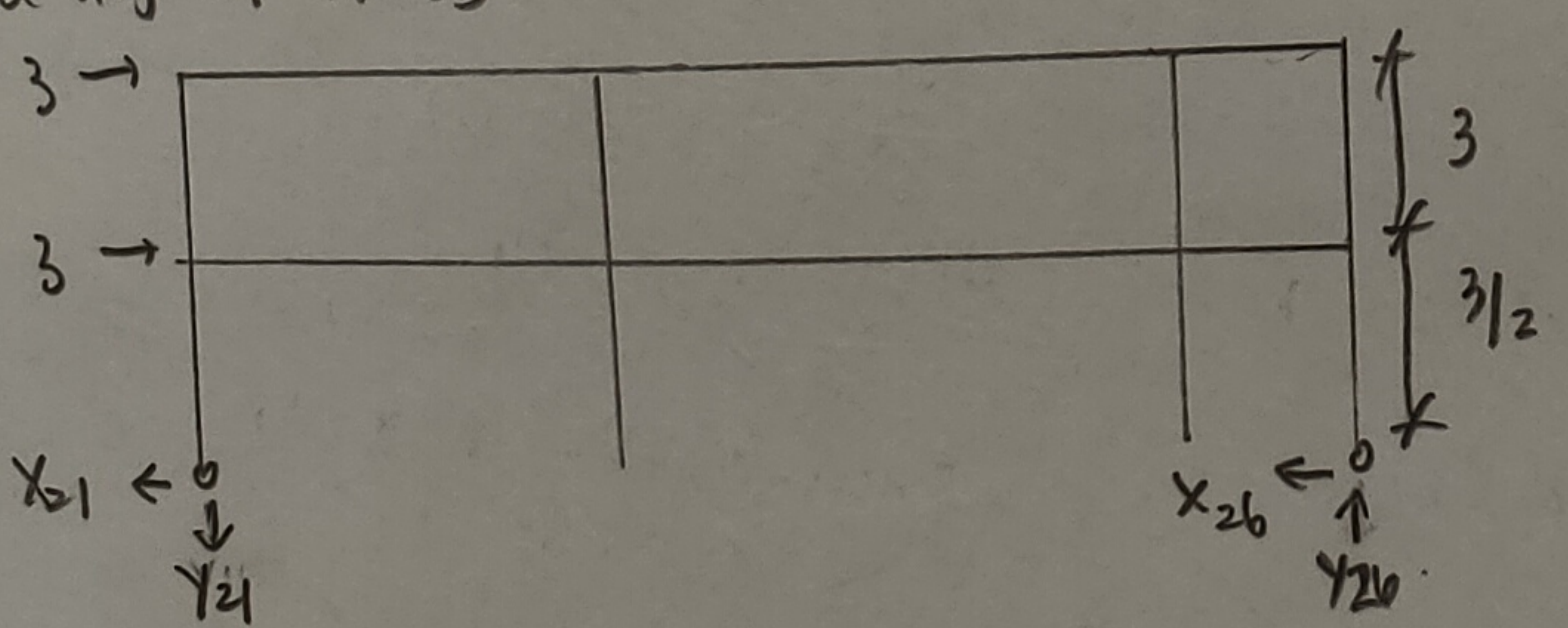
$$X_{13} = X_{14} = \frac{3/2}{2} = \frac{3}{4} \text{ kN}$$

$$X_{15} = X_{16} = \frac{1/2}{2} = \frac{1}{4} \text{ kN}$$

$$X_{23} = X_{24} = \frac{(3/2+3/2)}{2} = 3/2$$

$$X_{27} = X_{28} = \frac{(1+1)}{2} = 1$$

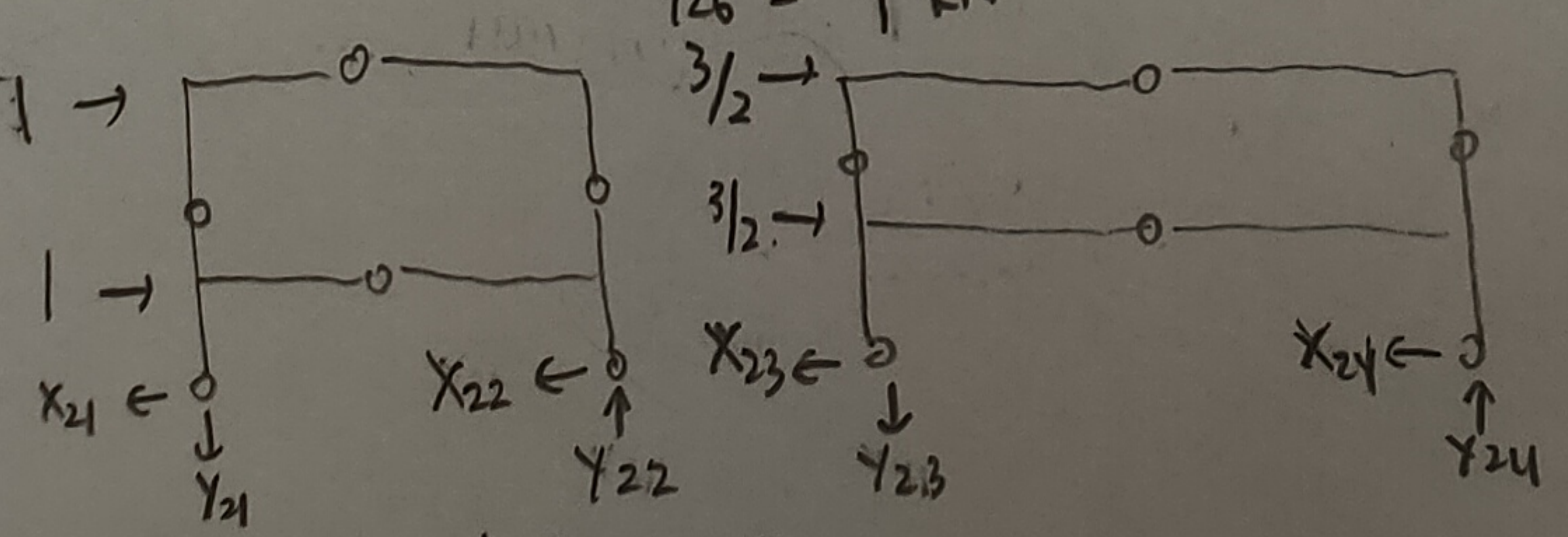
2nd highest storey



$$Y_{21} = Y_{26}$$

$$\sum M_{21} = 0 \quad 3(3+3/2) + 3(3/2) = Y_{26}(3+6+9)$$

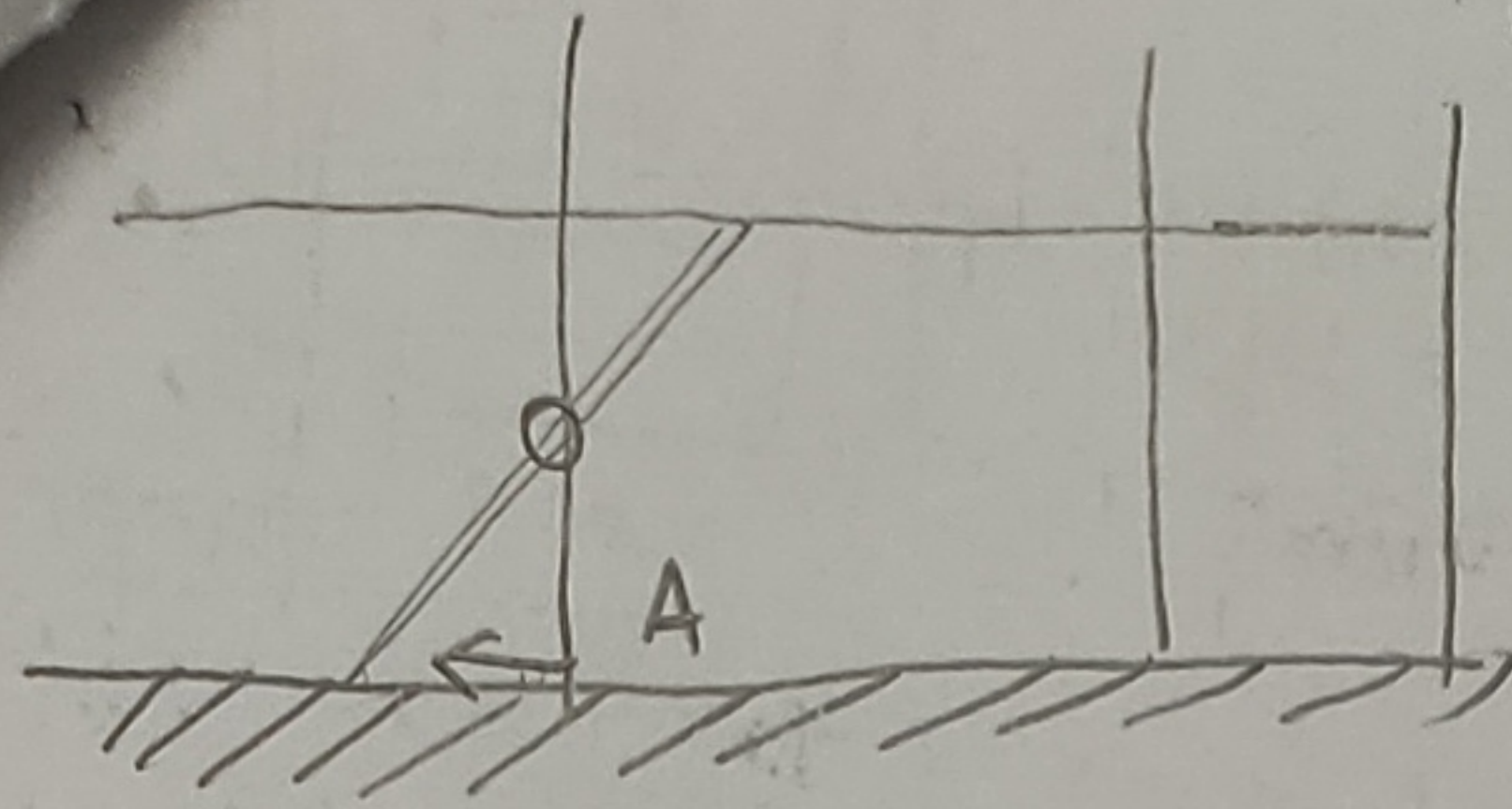
$$Y_{26} = 1 \text{ kN}$$



$$X_{21} = X_{22} = \frac{1}{2}(1+1) = 1 \text{ kN}$$

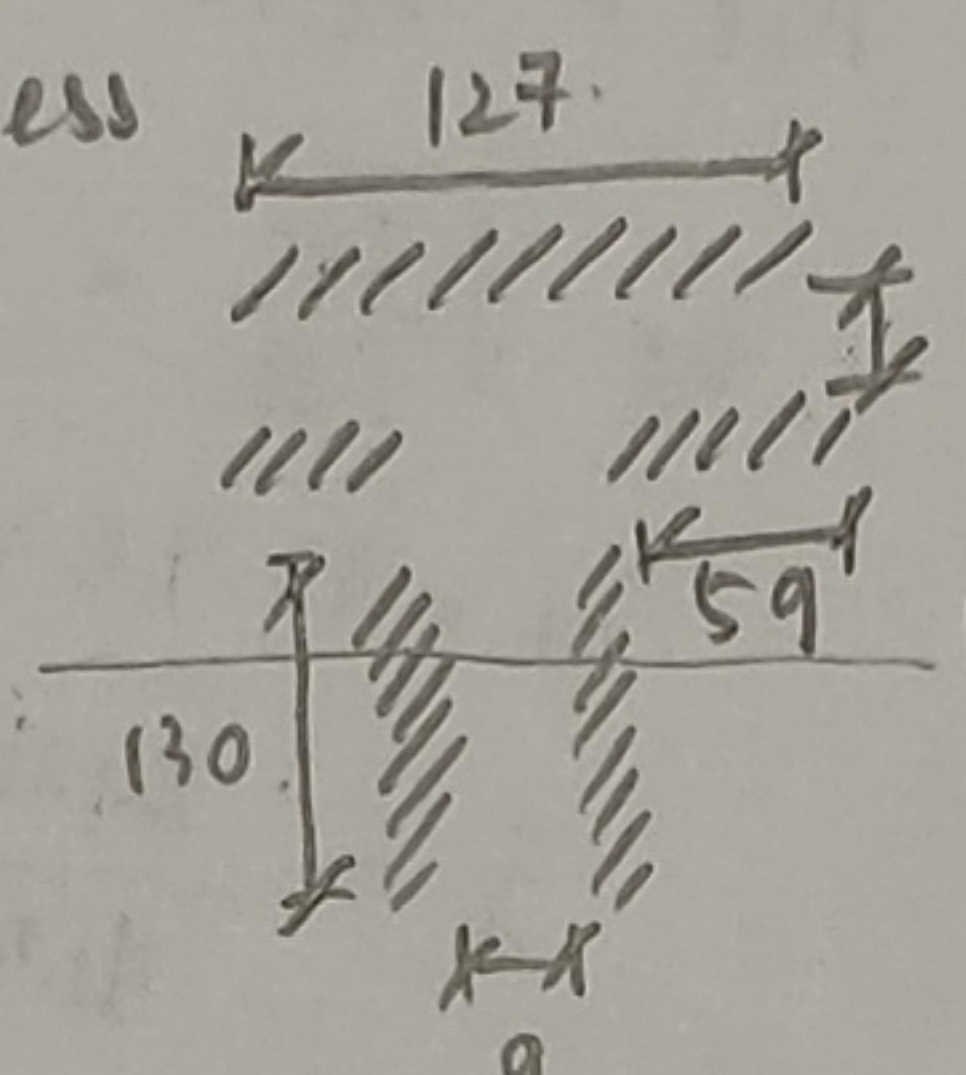
$$X_{23} = X_{24} = \frac{1}{2}(\frac{3}{2} + \frac{3}{2}) = \frac{3}{2} \text{ kN}$$

15/16/1



Bending moment, $P = (X_{62} + X_{63}) \times 2$
 $= 15/2 \times 2$
 $= 15 \text{ kN/m.}$

b) Assume 1mm weld throat thickness
 Total area of weld
 $= 127 + (130 \times 2) + (59 \times 2)$
 $= 505 \text{ mm}^2$



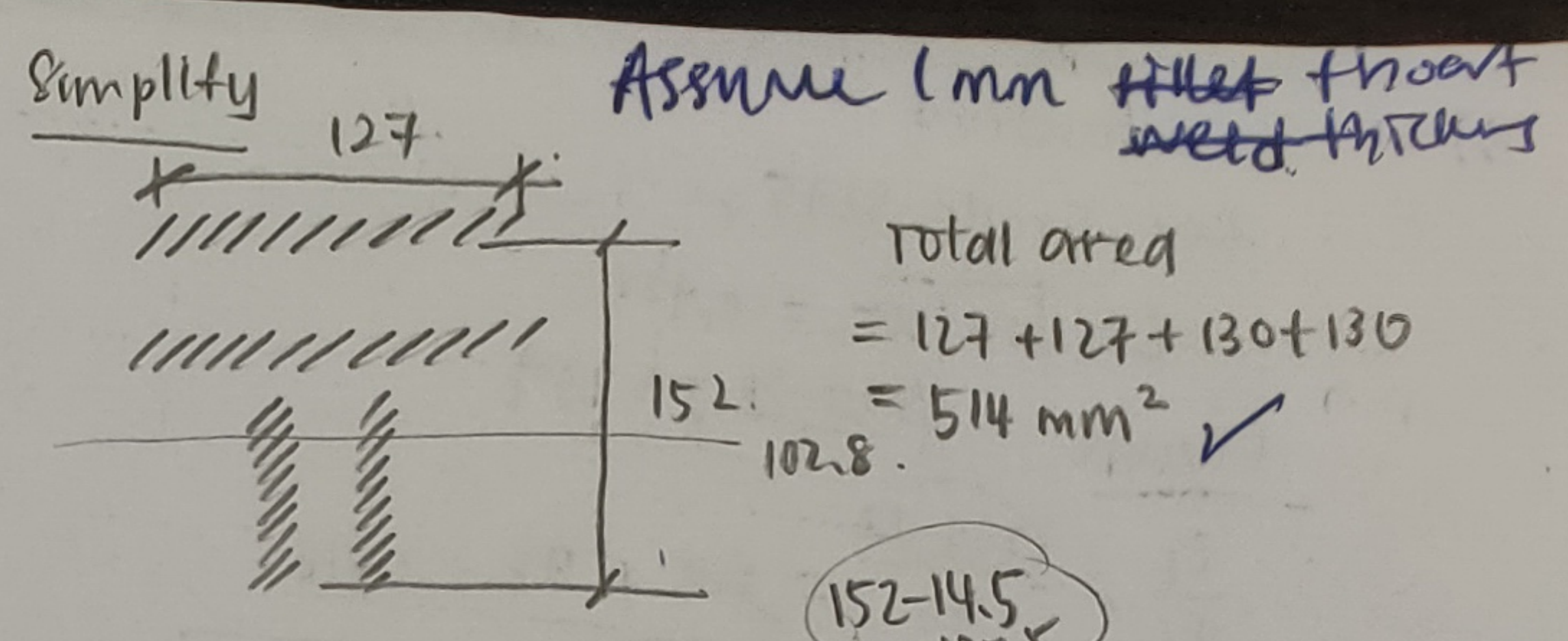
Find centroid (wrt bottom)
 $127(1)(155.4 + 0.5) + 2(130)(1)(\frac{130}{2}) + 2(59)(1)(130 + 0.5) = 505 y_{cen}$
 $52098.3 = 505 y_{cen}$
 $y_{cen} = 103.165 \text{ mm.}$

$I_{yy} = \left[\frac{127(1)^3}{12} + 127(1)(155.4 - 103.165)^2 \right] + 2 \left[\frac{130^3(1)}{12} + 130(1)(103.165 - \frac{130}{2})^2 \right]$
 $+ 2 \left[\frac{59(1)^3}{12} + 59(1)(130 - 103.165)^2 \right]$
 $= 346529.5 + 754560.5 + 84983.7$
 $= 1186073.67 \text{ mm}^4$

Vertical load = 130 kN.
 $e = 120 \text{ mm}$
 $M = Pe = 15.6 \text{ kNm}$

$f_b = \frac{Pe}{W_{el}} = 1635.11 \text{ N/mm}^2$
 $f_s = \frac{P}{\text{Area of weld}} = \frac{130}{505} = 257.43 \text{ N/mm}^2$
 $f_r = \sqrt{f_s^2 + f_b^2} = 1066.64 \text{ N/mm}^2$
 $f_{w,d} = \frac{f_u/\sqrt{3}}{\beta_w \gamma_{m2}} = \frac{430/\sqrt{3}}{0.85(1.25)} = 233.7 \text{ N/mm}^2$

f_r calc based on $a=1$.
 Actual stress = f_r/a
 $1066.64/a = 233.7$
 $a = 4.56$
 Assuming equal leg fillet weld
 weld leg length
 $s = 4.56/0.707 = 6.455 \text{ mm}$
 provide at least 7mm fillet weld



$127(1)(152 + 0.5) + 127(1)(130 + 0.5) + 2(130)(1)(\frac{130}{2}) = 514(y_{cen})$
 $y_{cen} = \frac{52841.53730}{514} = 102.8 \text{ mm.}$

$I_{yy} = \left[\frac{127(1)^3}{12} + 127(1)(152 + 0.5 - 102.8)^2 \right] + 2 \left[\frac{130^3(1)}{12} + 130(1)(102.8 - \frac{130}{2})^2 \right]$
 $+ 2 \left[\frac{59(1)^3}{12} + 59(1)(130 - 102.8)^2 \right]$
 $= 292252.94 + 138062.24 + 772448.1$
 $= 1202763.28 \text{ mm}^4$

$W_{el} = \frac{I_{yy}}{y} = \frac{1202763.28}{152 - 102.8} = 24814.6 \text{ mm}^3$
 $W_{el} = \frac{I_{yy}}{y} = \frac{1186073.67}{155.4 + 1} = 7638.5 \text{ mm}^3$
 $W_{el} = 24814.6 + 7638.5 = 32453.1 \text{ mm}^3$

Vertical load = 130 kN
 $e = 120 \text{ mm}$
 $Pe = M = 15.6 \text{ kNm}$
 $f_b = \frac{Pe}{W_{el}} = 681.67 \text{ N/mm}^2$
 $f_s = \frac{P}{\text{Area}} = \frac{130 \times 10^3}{514} = 253 \text{ N/mm}^2$
 $f_r = \sqrt{f_b^2 + f_s^2} = 727.1 \text{ N/mm}^2$

$f_{w,d} = 233.7 \text{ N/mm}^2$
 f_r based on $a=1$
 $f_r/a = 727.1/a = 233.7$
 $a = 3.12$
 Assuming equal leg fillet weld
 $s = 3.12 / \cos 45^\circ = 4.41$
 provide 5mm fillet weld
 at least 5mm weld.

3) i) Classification

For Grade S275,

$$\epsilon = \sqrt{235/275} = 0.924$$

Flange $\frac{500-22}{2} = 239$

$$\frac{c_f}{t_f} = \frac{250-22}{40} = 5.7 \leq 9\epsilon = 8.316$$

Class 1 5.975

Web

$$\frac{c_w}{t_w} = \frac{2420}{22} = 110 \leq 124\epsilon = 114.576$$

class 3

ii) Bending resistance

⇒ Method 1

$$M_{y,Rd} = W_{pl,y} f_{yf} + W_{el,w} f_{yw}$$

$$W_{pl,y} f_{yf} = A_f (h_w + t_f) f_{yf} = (500 \times 40) (2420 + 40) (275) / 10^6 = 13530 \text{ kNm}$$

$$I_w = \frac{2420^3 \times 22}{12} = 2.598 \times 10^{10} \text{ mm}^4$$

$$W_{el,w} = \frac{I_w}{z} = \frac{2.598 \times 10^{10}}{2420/2} = 21473466.67 \text{ mm}^3$$

$$W_{el,w} f_{yw} = 5905.2 \text{ kNm}$$

$$M_{y,Rd} = 13530 + 5905.2 = 19435.2 \text{ kNm}$$

→ Flange induced buckling

$$\frac{h_w}{t_w} \leq k \frac{E}{f_{yf}} \sqrt{\frac{A_w}{A_{fc}}}$$

iii) Shear resistance

$$a/h_w = 4000/2420 = 1.65 \geq 1$$

$$k_\tau = 5.34 + 4 \left(\frac{h_w}{a} \right)^2 = 6.804$$

$$\frac{h_w}{t_w} \leq 31 \frac{\epsilon}{\eta} \sqrt{k_\tau}$$

$$\frac{2420}{22} = 110 \leq 31 \frac{0.924}{1} \sqrt{6.804} = 78.72$$

web is NOT stocky

$$V_{b,Rd} = V_{bw,Rd} + V_{bf,Rd} \leq \frac{n f_w h_w t_w}{\sqrt{3} \gamma_{M1}}$$

$$\bar{\lambda}_w = \frac{h_w}{37.4 t_w \epsilon \sqrt{k_\tau}} = \frac{2420}{37.4 (22) (0.924) \sqrt{6.804}} = 1.22 > 1.08$$

$$\chi_w = 1.37 / (0.7 + \bar{\lambda}_w) = 0.714$$

$$V_{bw,R} = \frac{\chi_w f_{yw} h_w t_w}{\sqrt{3} \gamma_{M1}} = \frac{0.714 (275) (2420) (22)}{\sqrt{3} (1.00)} = 6035.43 \text{ kN}$$

* Assume no contribution from flange

$$V_{bf,Rd} = \frac{(500)(40)^2 (275)}{(1039.71)(1.00)} (1 - 0) \text{ at support}$$

$$c = 4000 (0.15 + \frac{26(500)(40)^2 (275)}{(2)(2420)^2 (275)}) = 1039.71$$

$$= 211.591 \text{ kN}$$

For end post.

$$\bar{\lambda}_w = 1.22$$

$$N_{st,ten} = \frac{2420 \times 275 \times 22}{1000 \sqrt{3}}$$

$$= P - 5679.24$$

$$N_{Ed} = 2P - 5679.24 < 7830.23$$

vi)

$$V_{max} = P$$

$$M_{max} = 8P$$

$$P < 2429.4 \text{ kNm}$$

$$P < 6035.43 \text{ kNm}$$

$$P < 6754.735$$

iv) Rigid End Post

$$e = 600 + 11 \times 22 = 622 \text{ mm} > 0.1 h_w = 242$$

$$A_e = A_u = 422 \times 20 = 8440 \text{ mm}^2$$

$$\frac{4 h_w t_w^2}{e} = 7532.34 \text{ mm}^2$$

Hence, minimum size requirement OK!

$$I_{st} = 2 \left(\frac{422^3 \times 20}{12} \right) + \frac{600 \times 22^3}{12} = 251037226.7 \text{ mm}^4$$

$$A_{st} = 2(422 \times 20) + 600 \times 22 = 30080 \text{ mm}^2$$

$$i_{st} = \sqrt{\frac{I_{st}}{A_{st}}} = 91.35 \text{ mm}$$

$$\lambda_1 = 93.9 \epsilon = 86.764$$

$$\bar{\lambda} = \frac{2420}{91.35} \frac{1}{86.764} = 0.305 > 0.2$$

$$\phi = 0.5 [1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2] = 0.572$$

$$\chi = \frac{1}{\phi + \sqrt{\phi^2 - \bar{\lambda}^2}} = 0.947$$

$$N_{b,Rd} = 0.947 \times A_{st} \times f_y = 7830.23 \text{ kN}$$

v) Load bearing stiffness

$$15 \epsilon t_w = 15 (0.924) (22) = 304.92 \text{ mm}$$

$$A_{st} = (304.92 + 20 + 304.92) (22) + 2(200 \times 20)$$

$$= 21856.48 \text{ mm}^2$$

$$I_{st} = \frac{(200 + 22 + 200)^3 \times 20}{12} + 2 \left(\frac{304.92 \times 22^3}{12} \right)$$

$$= 125793544.7 \text{ mm}^4$$

$$i_{st} = \sqrt{\frac{I_{st}}{A_{st}}} = 75.865 \text{ mm}$$

$$\lambda_{11} = 93.9 \epsilon = 86.764$$

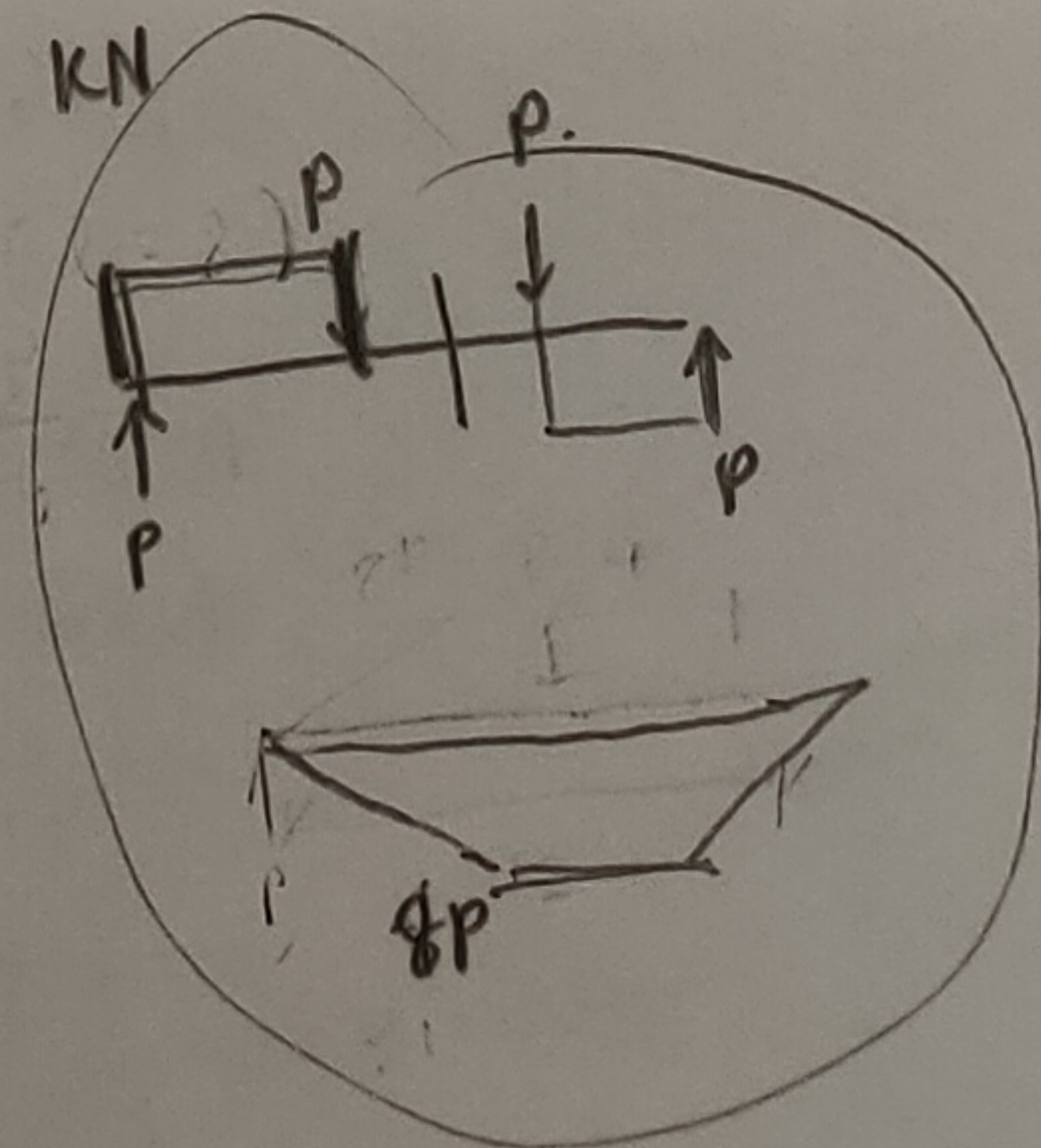
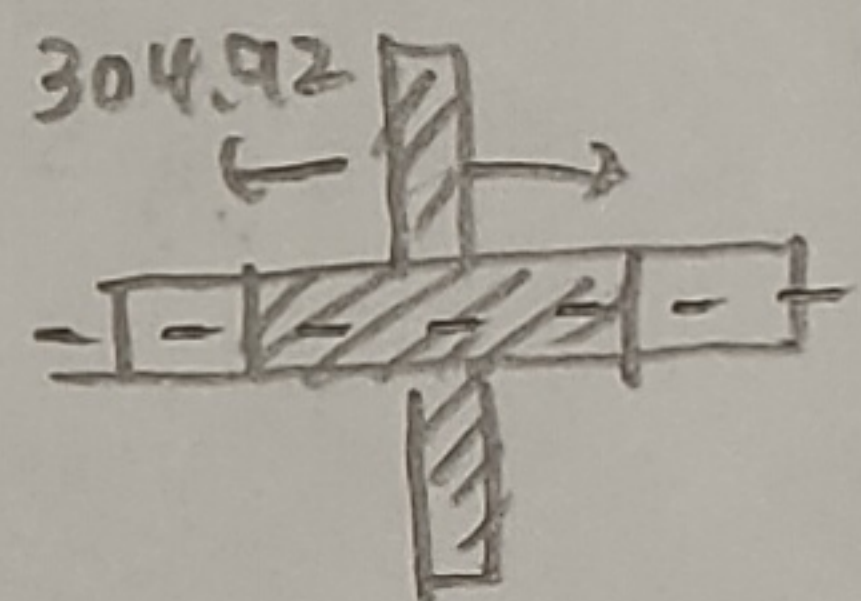
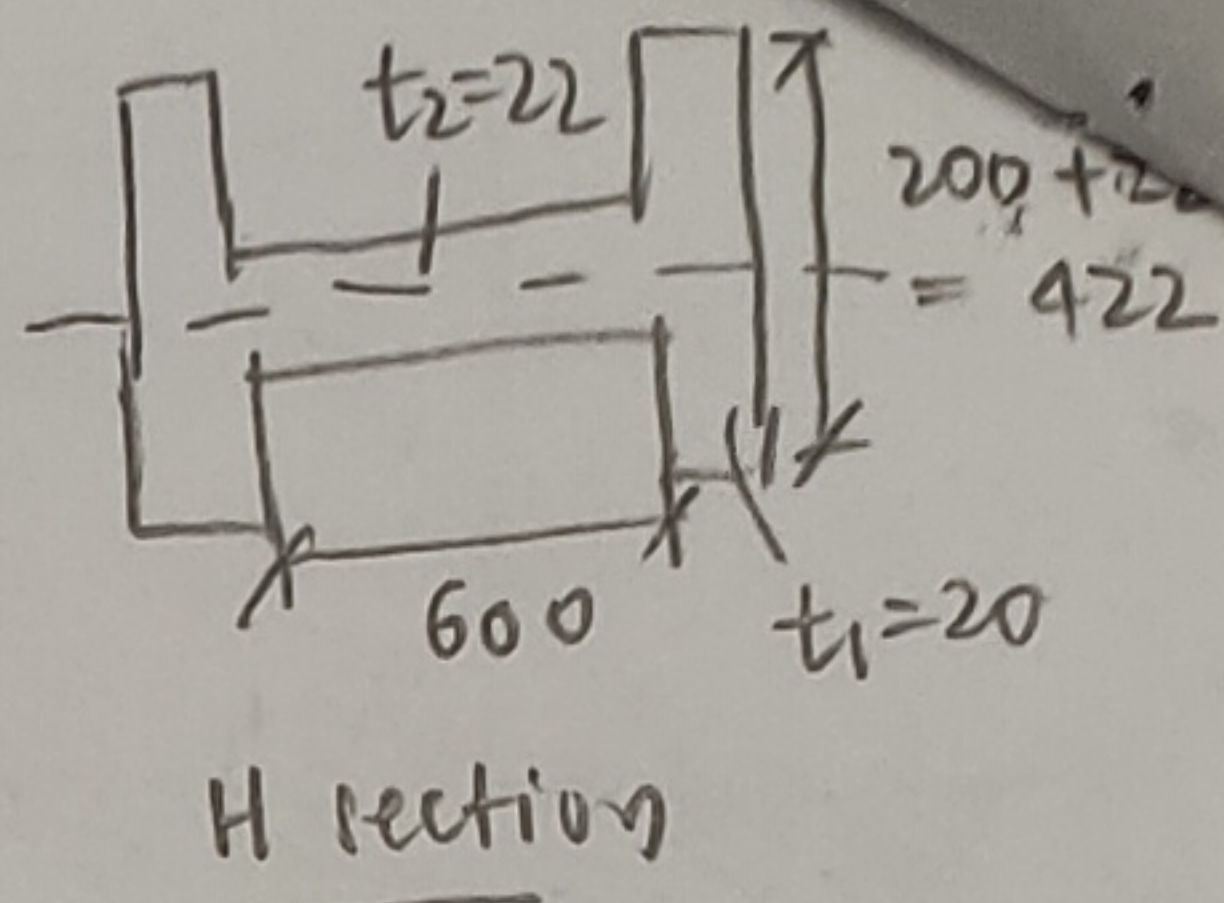
$$\bar{\lambda} = \frac{2420}{75.865} \times \frac{1}{86.764} = 0.368 > 0.2$$

$$\phi = 0.5 [1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2]$$

$$= 0.609$$

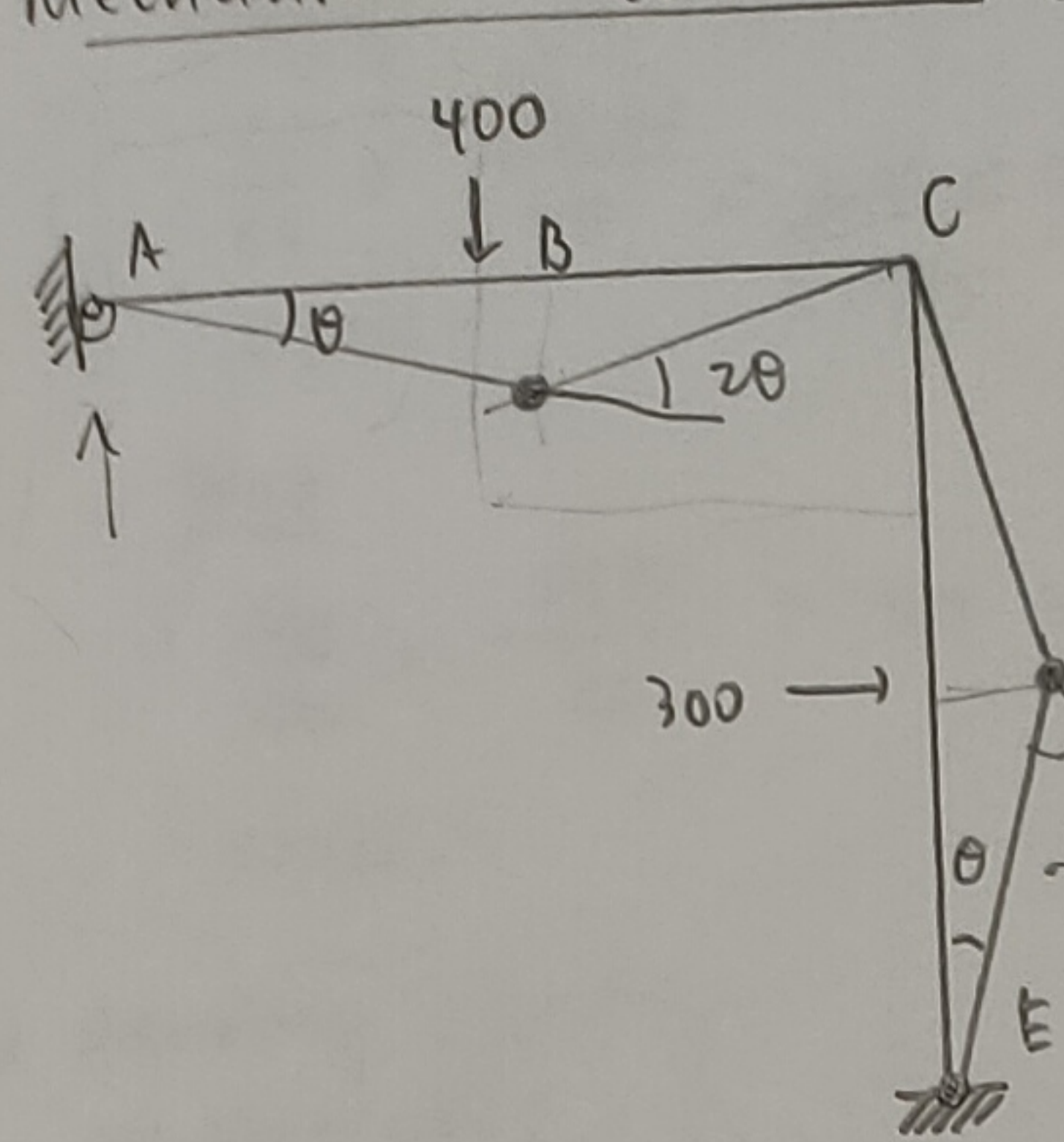
$$\chi = \frac{1}{\phi + \sqrt{\phi^2 - \bar{\lambda}^2}} = 0.914$$

$$N_{b,Rd} = 0.914 \times 21856.48 \times 275 = 5494.336 \text{ kN}$$

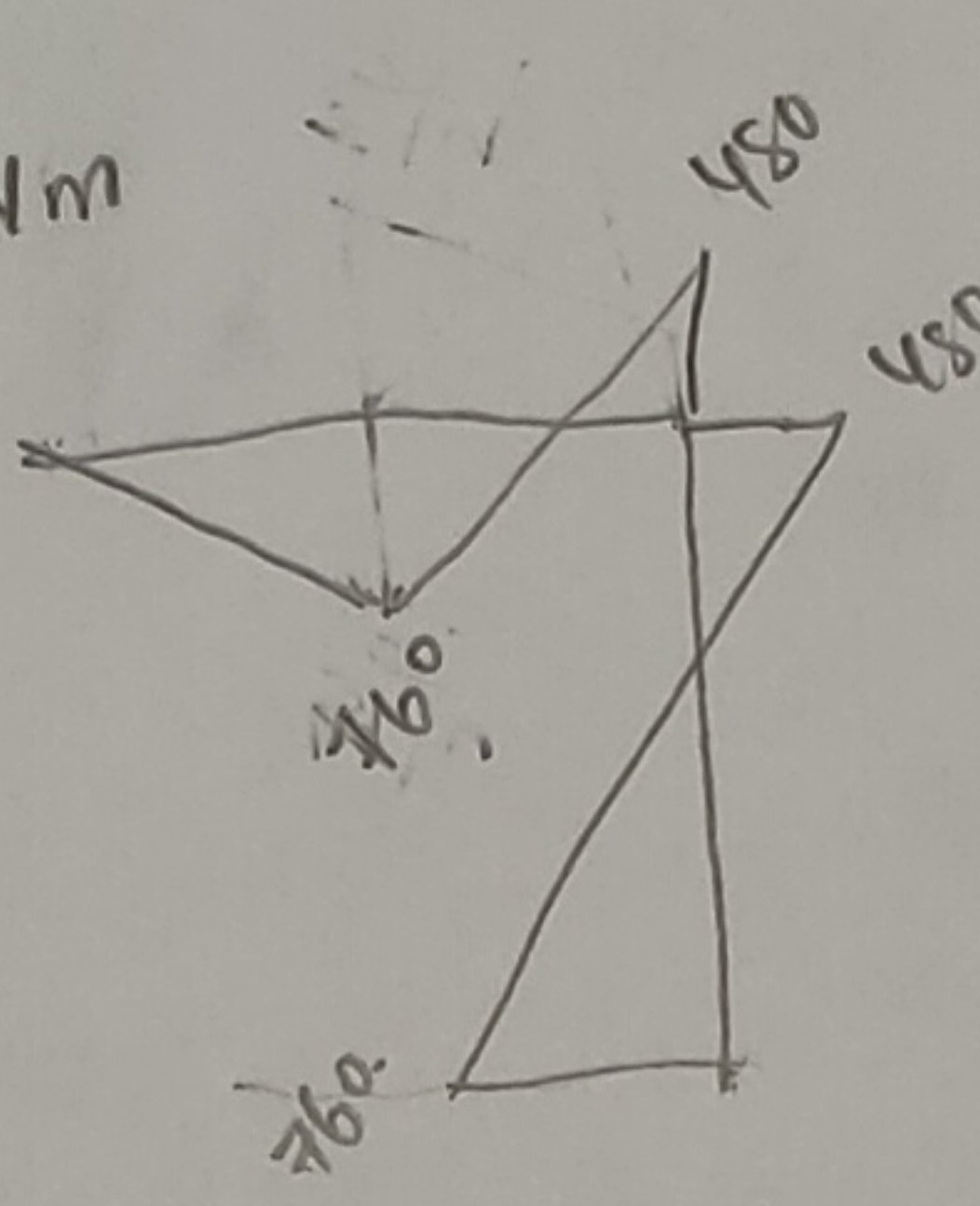


4) a) $n_s = (2+3) - 3 = 2$
 $n_{ph} = 2 + 1 = 3$

* uniform steel $\Rightarrow M_p$ same throughout
 Mechanism 1 (B-D-E) combined

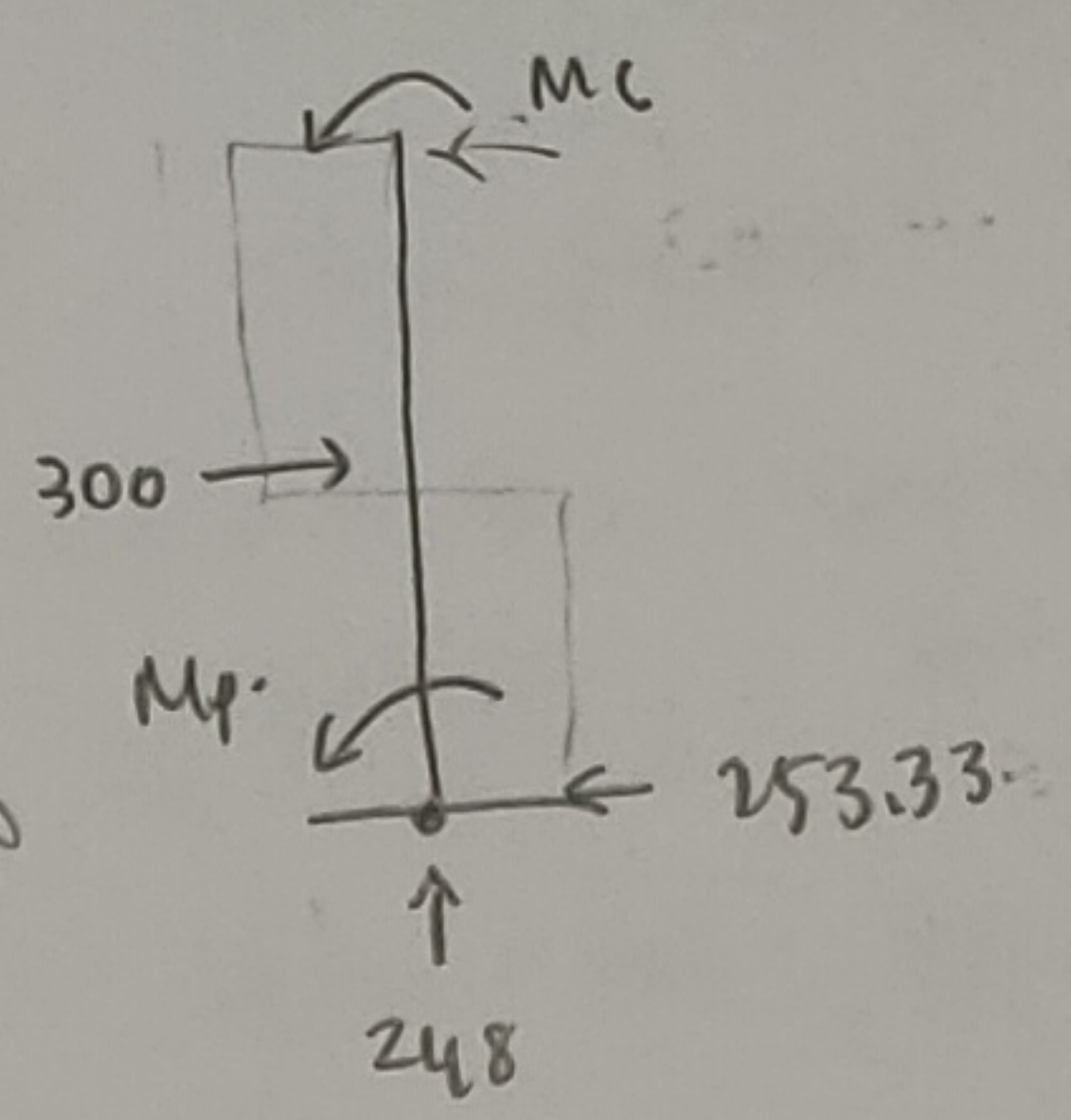


$\sum W_e = \sum W_i$
 $400(5\theta) + 300(6\theta) = M_p(2\theta) + M_p(2\theta) + M_p(\theta)$
 $3800 = 5M_p$
 $M_p = 760 \text{ kNm}$



$n_{ph} = n_s + 1 = 2 + 1 = 3$ (mechanism satisfied)

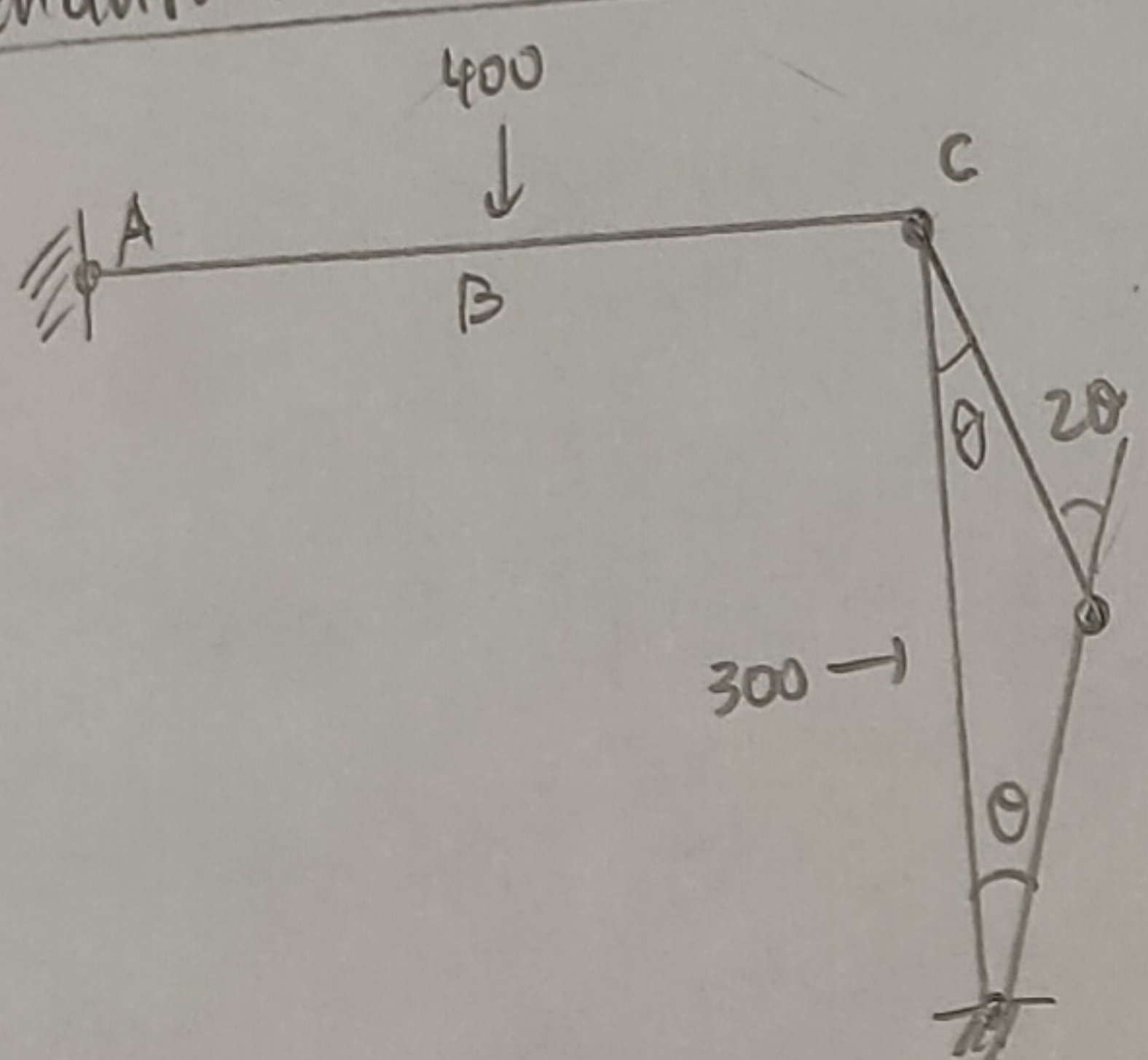
check moments @ C



$\sum M_c = 0$
 $253.33(12) = M_p + M_c + 300(6)$
 $M_c = 480 \text{ kN} < M_p$
 \therefore plasticity satisfied

\therefore Mechanism 1 is the correct mechanism!

Mechanism 2 (C-D-E) column



$\sum W_e = \sum W_i$
 $300(6\theta) = M_p(\theta) + M_p(2\theta) + M_p(\theta)$
 $1800 = 4M_p$
 $M_p = 450 \text{ kNm}$

b) $w_{pl} \geq \frac{M_p}{f_y} = \frac{760 \times 10^3}{355} = 2140.85 \text{ cm}^3$

Choose 457 x 191 x 98 $w_{pl} = 2230 \text{ cm}^3$

- $A = 12500 \text{ mm}^2$
- $h_w = 407.6 \text{ mm}$
- $t_w = 11.4 \text{ mm}$
- $b_f = 192.8 \text{ mm}$
- $t_f = 19.6 \text{ mm}$
- $r = 10.2 \text{ mm}$
- $C_f + t_f = 41.1 > 9\epsilon$ (class 1)
- $C_w + t_w = 39.8 > 72\epsilon$

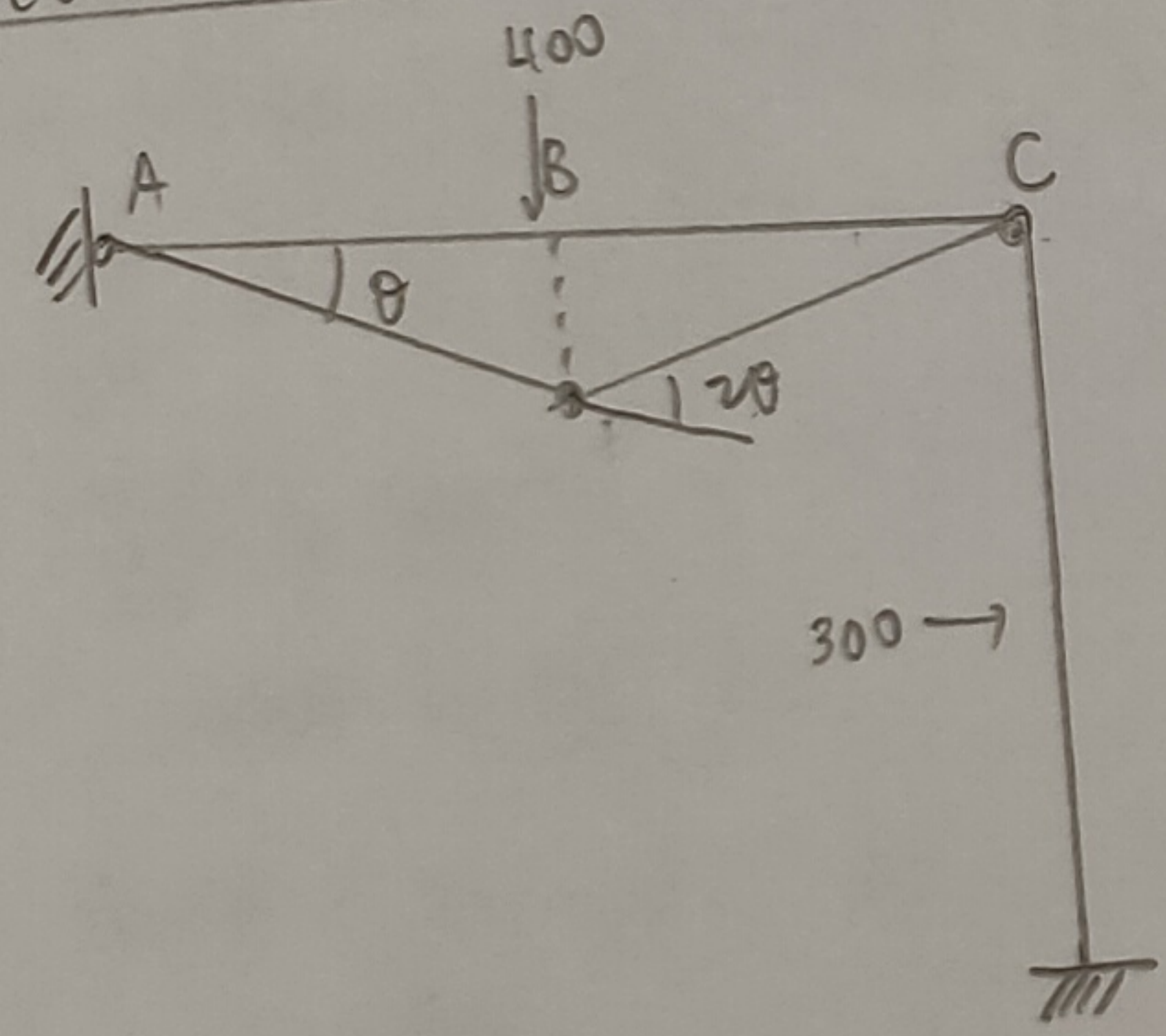
$A_v = A - 2b_f t_f + (t_w + 2t_f) t_f > h_w t_w$
 $= 12500 - 2(192.8)(19.6) + (11.4 + 2(19.6))(19.6)$

$> 407.6(11.4)$
 $= 5565.52 > 4646.64$

$V_{pl,Rd} = \frac{A_v f_y}{\sqrt{3}}$
 $= 1140.71 \text{ kN} > 253.33$

$M_{c,Rd} = f_y w_{pl} = 791.65 \text{ kN} > 700$

Mechanism 3 (B-C) beam

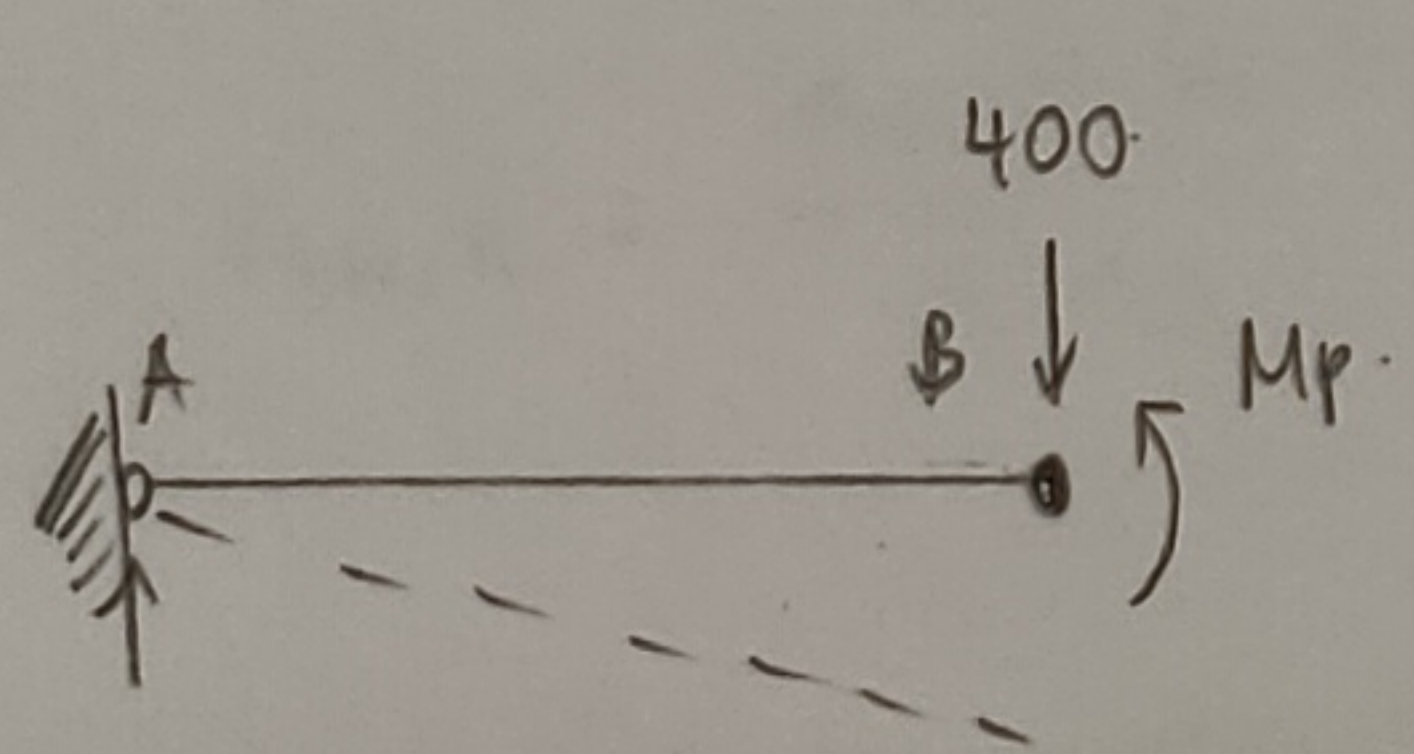


$\sum W_e = \sum W_i$
 $400(5\theta) = M_p(2\theta) + M_p(\theta)$
 $2000 = 3M_p$
 $M_p = 666.67 \text{ kNm}$

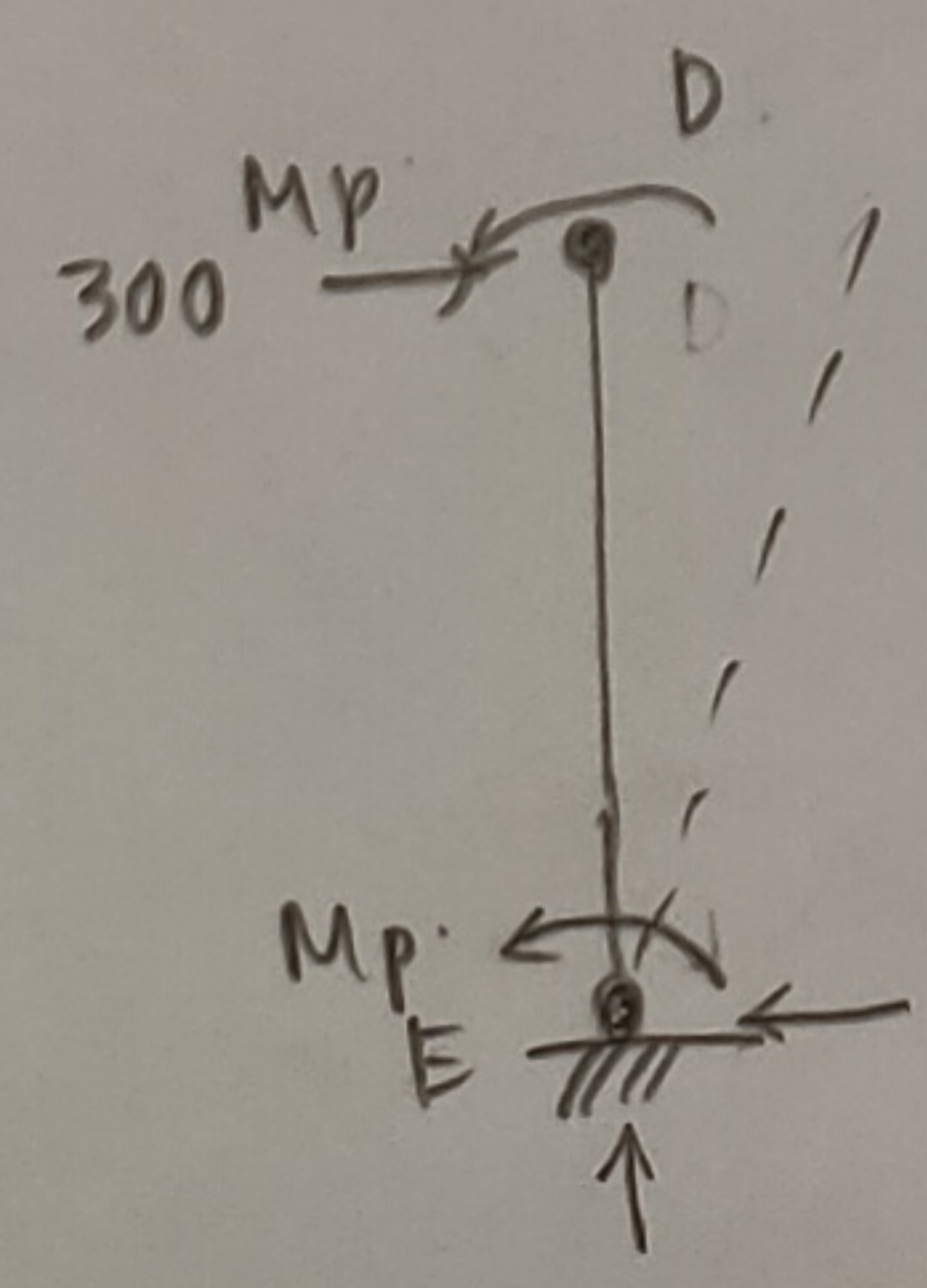
$(0.5 V_{pl,Rd}) > 253.33$
 low shear

\therefore Mechanism 1 is the most likely correct mechanism with $M_p = 760 \text{ kNm}$

Equilibrium check



$\sum M_B = 0$
 $A_y(5) = M_p$
 $A_y = 152 \text{ kN}$



$\sum M_D = 0$ $M_p + M_p = E_x(6)$
 $E_x = 253.33 \text{ kN}$

$\sum M_A = 0$ $400(5) + 253.33(12) = 300(6) + E_y(10) + M_p$
 $E_y = 248 \text{ kN}$

$\sum M_E = 0$ $152(10) + 300(6) = M_p + 400(5) + A_x(12)$
 $A_x = 46.67 \text{ kN}$

$\sum F_y = 152 + 248 - 400 = 0$
 $\sum F_x = 253.33 + 46.67 - 300 = 0$

Equilibrium satisfied!

