

2018/19

1) a) $v = 40 - 0.2k$

$q = vk$

$q = (40 - 0.2k)k$

$q = 40k - 0.2k^2$

For q_{max} ,

$q' = 0$

$q' = 40 - 0.4k = 0$

$40 = 0.4k$

$k_0 = 100 \text{ veh/km}$

$v_0 = 40 - 0.2(100)$
 $= 20 \text{ km/h}$

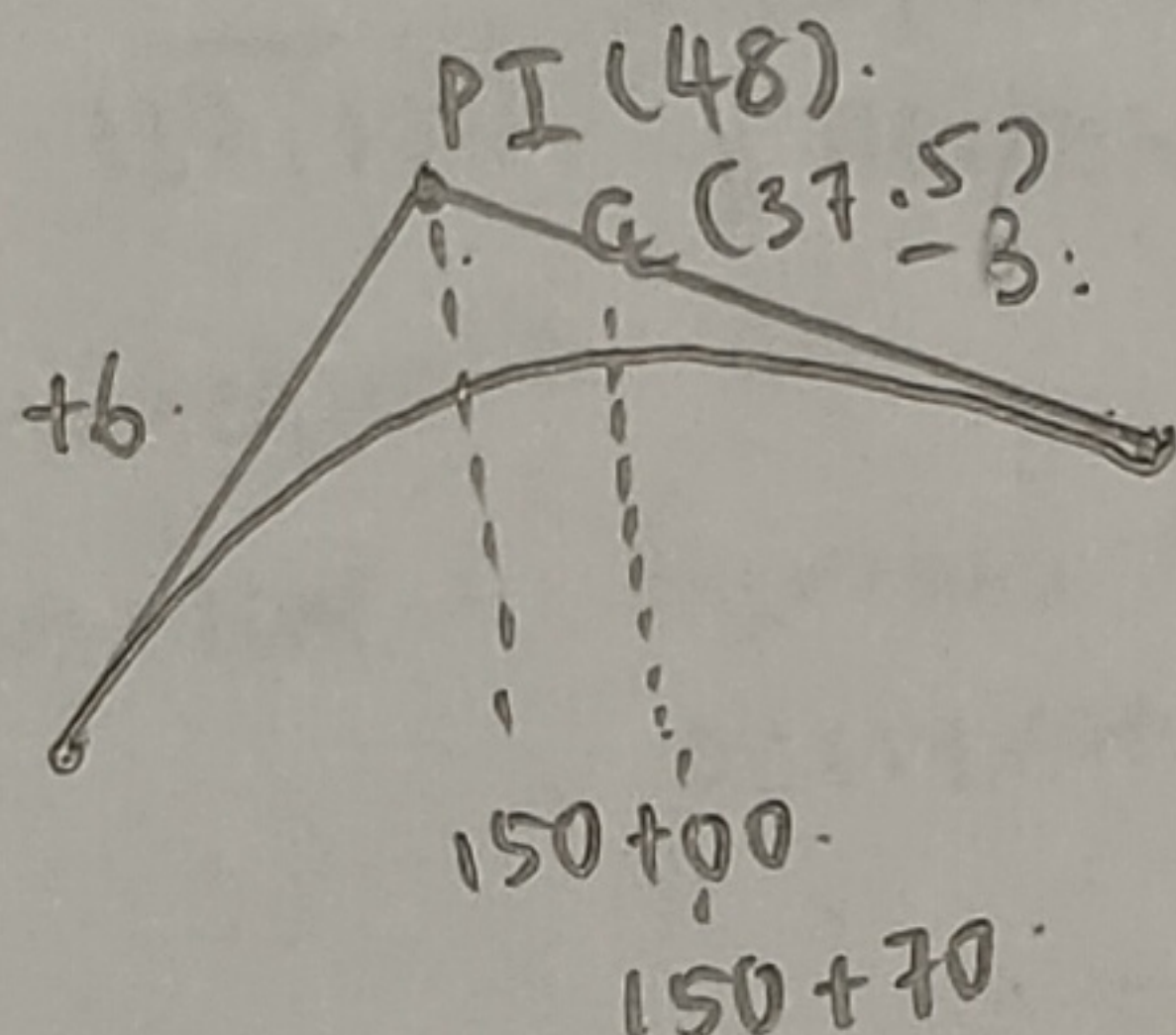
$q_{max} = v_0 k_0$
 $= 100(20)$
 $= 2000 \text{ veh/hr}$

$\frac{L}{2} + 70 = \frac{-g_1}{g_2 - g_1} L$

$x = 280$

$y = 150 \times 67$

b) -
2) a)



For highest pt,

$y' = 0$

$y = y_0 + g_1 x + \frac{1}{2} r x^2$

$y' = g_1 + r x = 0$

$g_1 + \frac{g_2 - g_1}{L} x = 0$

$x = \frac{-g_1}{g_2 - g_1} L$

For centerline, $x = \frac{L}{2} + 70$

$\frac{L}{2} + 70 = \frac{-g_1}{g_2 - g_1} L$

$\frac{L}{2} + 70 = \frac{-6}{-3 - 6} L$

$\frac{L}{2} + 70 = \frac{2}{3} L$

$70 = \frac{L}{6}$

$L = 420 \text{ m}$

b) For y_0

$\tan \theta = 6\%$

$\frac{48 - y_0}{420/2} = \frac{6}{100}$

$48 - y_0 = 12.6$

$y_0 = 35.4 \text{ m}$

$y = 35.4 + 0.06x + \frac{1}{2} \left(\frac{-0.09}{420} \right) x^2$

$y = 35.4 + 0.06x - 1.0714 \times 10^{-4} x^2$

For centerline, $x = \frac{L}{2} + 70 = 280 \text{ m}$

$y = 35.4 + 0.06(280) - 1.0714 \times 10^{-4} (280)^2$

$y = 43.8 \text{ m}$

Vertical clearance = $43.8 - 37.5 = 6.3 \text{ m}$

2018

$x_1 + x_2 + x_3 = x_4 + x_1$ $x_2 + x_3 = x_4 = 5$
 $x_3 = 5 - x_2$

- 1) a)
- b)
- 2) a)
- b)

4) $t_1 = t_2 + t_3 + t_4$
 a) $18 + 2x_1 = 12 + 2x_2 + 8 + x_4 = 10 + x_3 + 8 + x_4$
 $18 + 2x_1 = 20 + 2x_2 + x_4 = 18 + x_3 + x_4$

3) a) Zone A = 1000 hh
 Zone B = 2000 hh

$P_A = (6 \times 1000 - \frac{1000}{20} x_A^2) = 6000 - 50x_A^2$

$P_B = (6 \times 2000 - \frac{2000}{20} x_B^2) = 12000 - 100x_B^2$

$x_A + x_B = 5$ $x_A = 5 - x_B$

$P = 6000 - 50x_A^2 + 12000 - 100x_B^2$
 $= 18000 - 50(5-x_B)^2 - 100x_B^2$
 $= 18000 - 50(25 - 10x_B + x_B^2) - 100x_B^2$
 $= 18000 - 1250 + 500x_B - 50x_B^2 - 100x_B^2$

$P = 16750 + 500x_B - 150x_B^2$
 $\frac{dP}{dx_B} = 500 - 300x_B = 0$ (max)
 $x_B = 1.67 \text{ km}$
 $x_A = 3.33 \text{ km}$

$-2 + 2x_1 - 2x_2 = x_4$ $2x_2 - x_3 = -2$
 $-2 + 2x_1 - 2x_2 = 5$ $x_3 = 2x_2 + 2$
 $2x_1 - 2x_2 = 7$ $5 - x_2 = 2x_2 + 2$
 $x_1 - x_2 = 3.5$ $3x_2 = 3$
 $x_1 = 3.5 + x_2$ $x_2 = 1$
 $x_3 = 2(1) + 2 = 4$
 $x_4 = 5$

travel demand = $4.5 + 4 + 1 = 9.5$

b) $B \rightarrow C$ $D = 7 - 0.5t$

at equilibrium,
 $A \rightarrow C$ $x_4 = 4$
 $B \rightarrow C \Rightarrow D = 7 - 0.5t$
 $\Rightarrow 0 = 7 - 0.5t$ $t_4 = 8 + 4 = 12$
 $= 7 - 0.5(8 + x_4)$
 $D = 3 - 0.5x_4$ $D = 7 - 0.5(12) = 1$
 $x_4 = x_2 + x_3 + D$ $= 7 - 6 = 1$
 $x_4 = x_2 + x_3 + 1 - 0.5x_4$
 $1.5x_4 = x_2 + x_3 + 1$

$t_1 = t_2 + t_3 + t_4$
 $t_3 = t_2$
 $x_3 = 2 + 2x_2$
 $1.5x_4 = x_2 + 2 + 2x_2 + 1$
 $1.5x_4 = 3x_2 + 3$
 $x_4 = 2x_2 + 2$
 $x_2 = \frac{1}{2}x_4 - 1$
 $x_3 = \frac{1}{2}x_4 + 1$
 $x_1 = \frac{10}{3}$
 $DAC = x_1 + x_2 + x_3$
 $= \frac{10}{3} + \frac{1}{2}x_4 - 1 + \frac{1}{2}x_4 + 1$
 $= \frac{10}{3} + x_4$
 $T_3 = 18 + x_3 + x_4 + 1$
 $= 19 + x_3 + x_4$
 $T_2 = 20 + 2x_2 + x_4 + 1 = 21 + 2x_2 + x_4$
 $T_1 = 18 + 2x_1$
 $T = 8 + x_4$
 $D = 7 - 0.5(8 + x_4) = 1 - 0.5x_4$
 $= 1 - 0.5(8 + x_4) = 1 - 4 - 0.5x_4 = -3 - 0.5x_4$
 $= 1$

b) In the middle

$P_A = 17133$
 $P_B = 35096$

I	J	A _{IJ}	F _{IJ}	k _{IJ}	A _{IJ} F _{IJ} k _{IJ}	P _{IJ}	Q _{IJ}
A	S1	6	0.09	1	0.54	0.27	3769
	S2	12	0.16	1	1.92	0.78	13364
B	S1	6	0.359	1	2.154	0.529	18566
	S2	12	0.16	1	1.92	0.471	16530

$16530 + 13364 = 29894$

$P_A =$

BETTER

In same location

$\frac{dP}{dx}$
 $P_A = 16891$
 $P_B = 35442$

I	J	A _{IJ}	F _{IJ}	k _{IJ}	P _{IJ} k _{IJ} k _{IJ}	P _{IJ}	Q _{IJ}
A	S1	6	0.09	1	0.54	$\frac{1}{3}$	5630
	S2	12	0.09	1	1.08	$\frac{2}{3}$	11261
B	S1	6	0.359	1	2.154	$\frac{1}{3}$	11814
	S2	12	0.359	1	4.308	$\frac{2}{3}$	23628

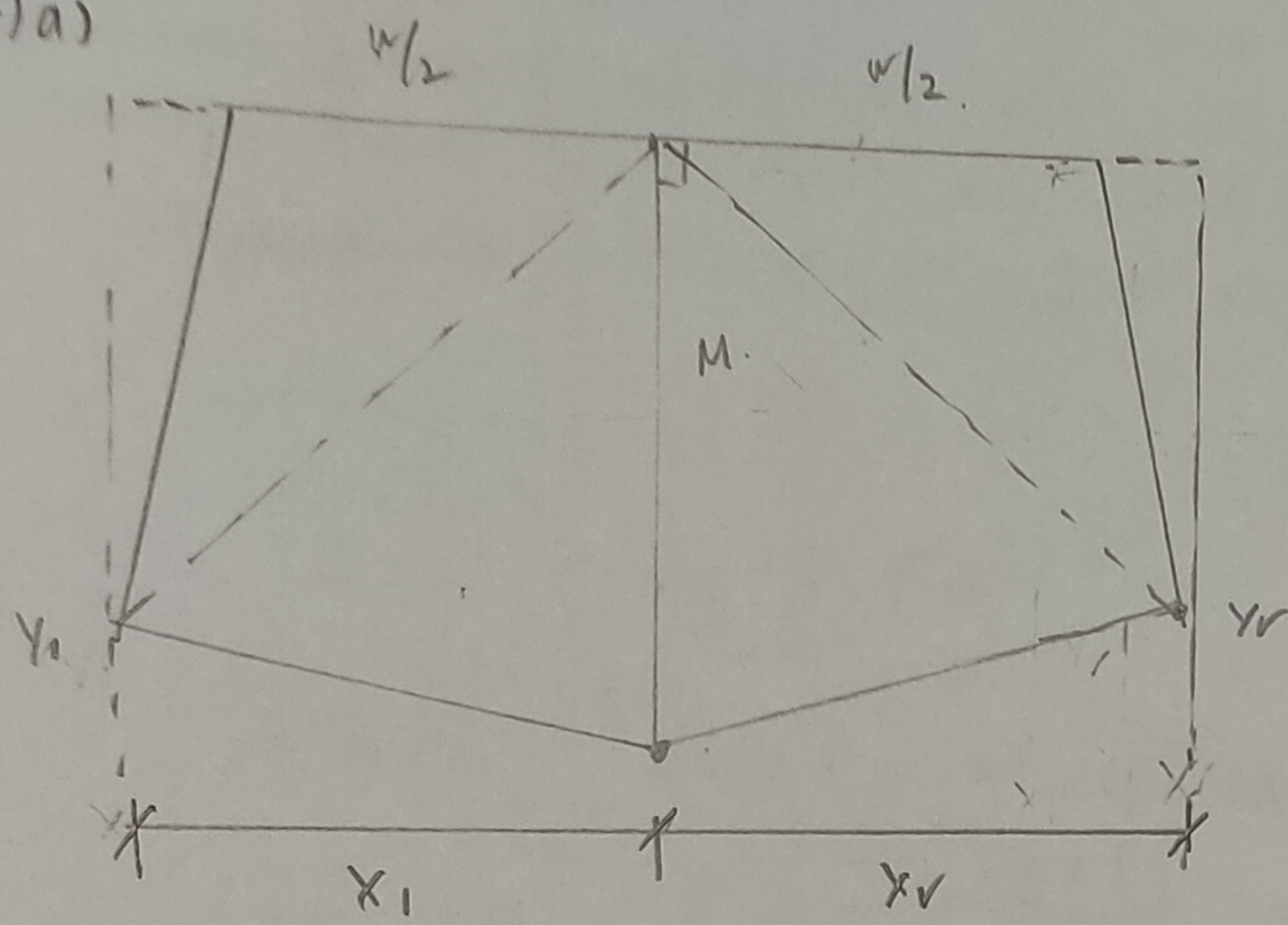
$11261 + 23628 = 34889$

$t_1 = t_2 + t_4 = t_3 + t_4$
 $18 + 2x_1 = 20 + 2x_2 + x_4 = 18 + x_3 + x_4$
 $18 + 2x_1 = 12 + 2x_2 + 8 + x_4$
 $18 + 2x_1 = 12 + \frac{2}{3} + 8 + x_4$
 $x_1 = \frac{10}{3}$
 $DAC = x_1 + x_2 + x_3$
 $= \frac{10}{3} + \frac{1}{2}x_4 - 1 + \frac{1}{2}x_4 + 1$
 $= \frac{10}{3} + x_4$
 $T_3 = 18 + x_3 + x_4 + 1$
 $= 19 + x_3 + x_4$
 $T_2 = 20 + 2x_2 + x_4 + 1 = 21 + 2x_2 + x_4$
 $T_1 = 18 + 2x_1$
 $T = 8 + x_4$
 $D = 7 - 0.5(8 + x_4) = 1 - 0.5x_4$
 $= 1 - 0.5(8 + x_4) = 1 - 4 - 0.5x_4 = -3 - 0.5x_4$
 $= 1$

$18 + 2x_1 = 20 + 2x_2 + 4$
 $18 + 2x_1 = 24 + 2x_2$
 $x_1 = \frac{7}{2} + x_2$
 $9 + x_1 = 12 + x_2$
 $x_1 = 3 + x_2$
 $9 + 3 + x_2 + 2x_2 = 12 + x_2 + x_4$
 $x_3 = 2x_2 + 3$
 $x_2 + x_3 = x_4$
 $x_2 + 2x_2 + 3 = x_4$
 $3x_2 = x_4 - 3$
 $x_2 = \frac{1}{3}x_4 - 1$
 $x_3 = \frac{1}{3}x_4 + 1$
 $x_1 = \frac{10}{3}$
 $D = x_1 + x_2 + x_3$
 $= \frac{10}{3} + \frac{1}{3}x_4 - 1 + \frac{1}{3}x_4 + 1$
 $= \frac{10}{3} + x_4$
 $D = x_1 + x_2 + x_3 = \frac{10}{3} + x_4$
 $= \frac{19}{3}$

$x_2 + x_3 = x_4$
 $x_2 + 2x_2 + 3 = x_4$
 $3x_2 = x_4 - 3$
 $x_2 = \frac{1}{3}x_4 - 1$
 $x_3 = \frac{1}{3}x_4 + 1$
 $x_1 = \frac{10}{3}$
 $D = x_1 + x_2 + x_3 = \frac{10}{3} + x_4$
 $= \frac{19}{3}$

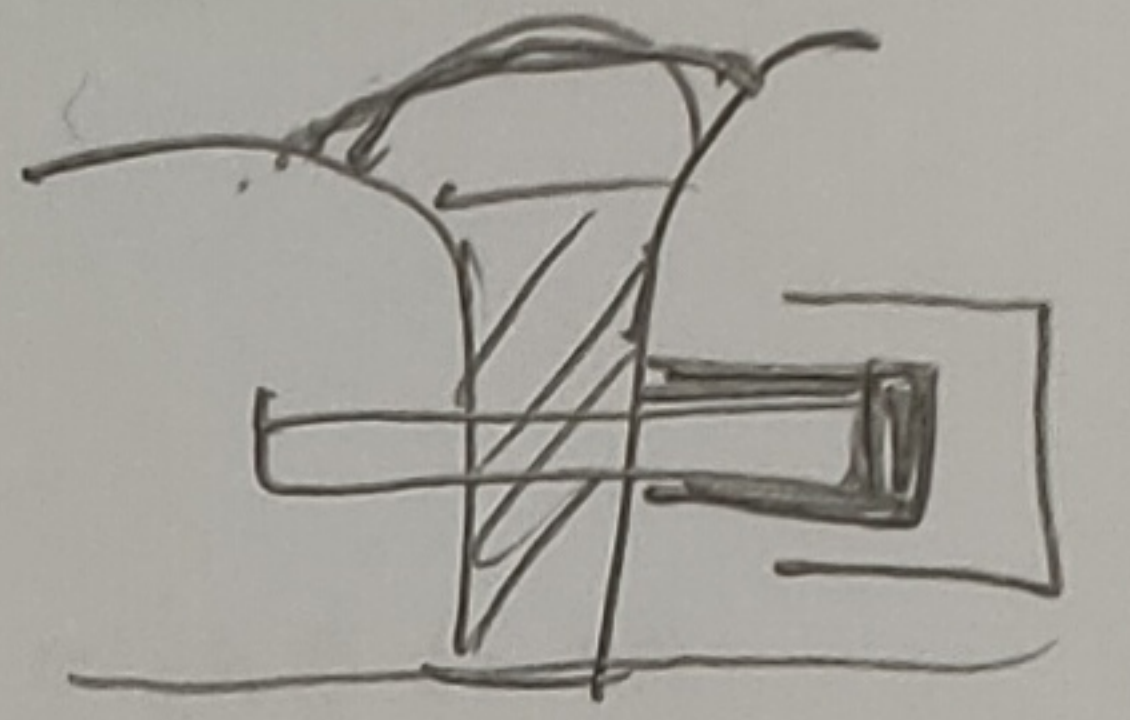
5) a)



$$A = \frac{1}{2} \cdot \frac{w}{2} \cdot y_1 + \frac{1}{2} M (x_1 + x_v) + \frac{1}{2} \cdot \frac{w}{2} \cdot y_v$$

$$= \frac{w}{4} (y_1 + y_v) + \frac{M}{2} (x_1 + x_v)$$

$$A = \frac{M}{2} (x_1 + x_v) + \frac{w}{4} (y_1 + y_v)$$



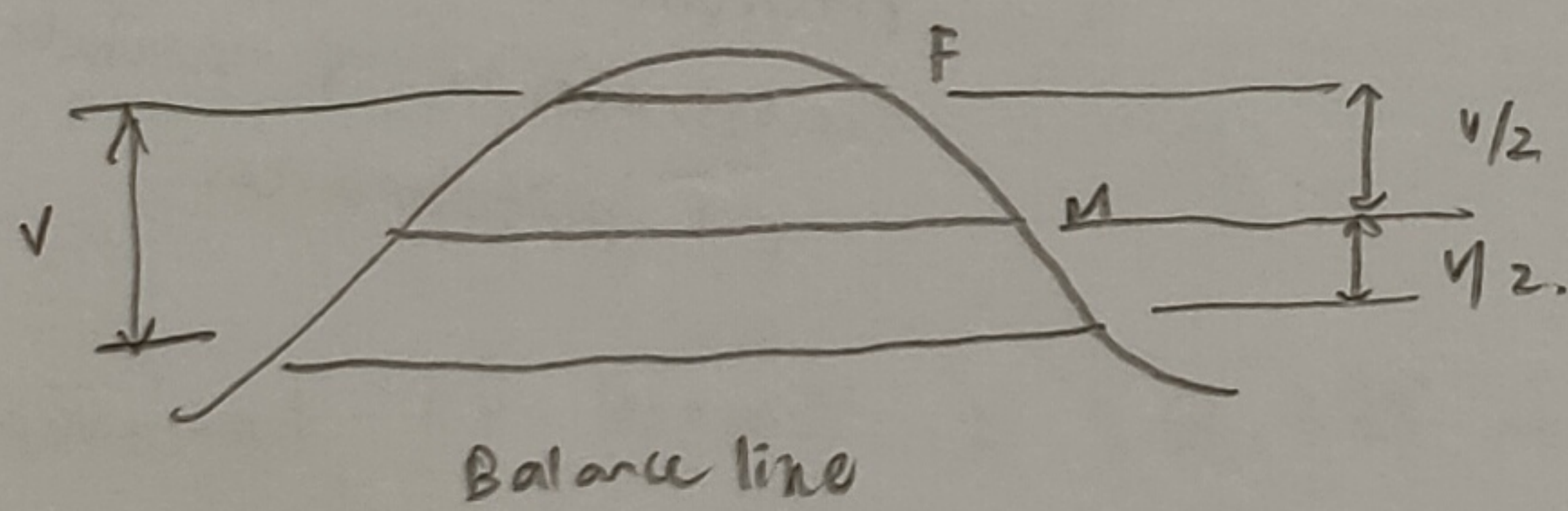
b)

Station	Calculation	Area	
150+50	$(\frac{1.5}{2}) (14.4 + 13.8) + \frac{12}{4} (3.6 + 2.3)$	38.85 m ² cut	$\frac{38.85 + 53.6}{2} (50) = 2311.25 \text{ m}^3$
151+00	$(\frac{2.0}{2}) (16.8 + 16.7) + \frac{12}{4} (3.3 + 3.4)$	53.6 m ² cut	
151+50	$(\frac{2.2}{2}) (18 + 18.3) + \frac{12}{4} (4.3 + 6.0)$	70.83 m ² cut	$\frac{53.6 + 70.83}{2} (50) = 3110.35 \text{ m}^3$
			<u>5422 m³</u>

c) Overhaul is the cost to haul material beyond the free haul distance F and it is measured in terms of \$/stn-m³.

There are 2 methods to calculate overhaul in mass diagram. One is to use graphical calculation and the other is using median haul distance.

In median distance, $OH = V(M-F)$.



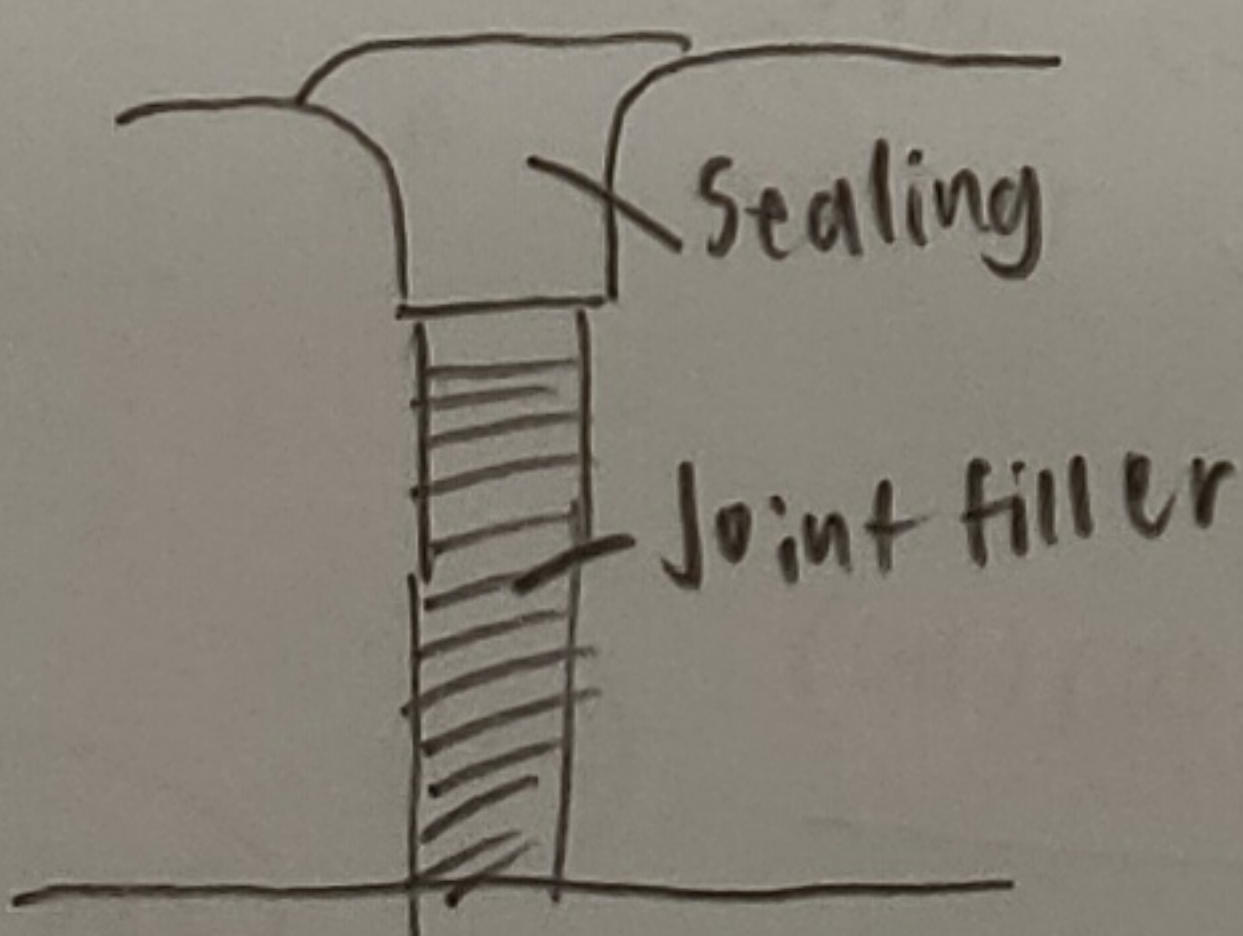
$$\frac{\Delta V}{2}$$

$$\text{Balance line (LEH)} = \frac{C_b}{C_{oh}} + F$$

- mark balance line and free haul line on the mass diagram
- compute ΔV , the volume between the 2 lines
- $\Delta V/2$ → read from graph → get median line
- measure median line (stn)

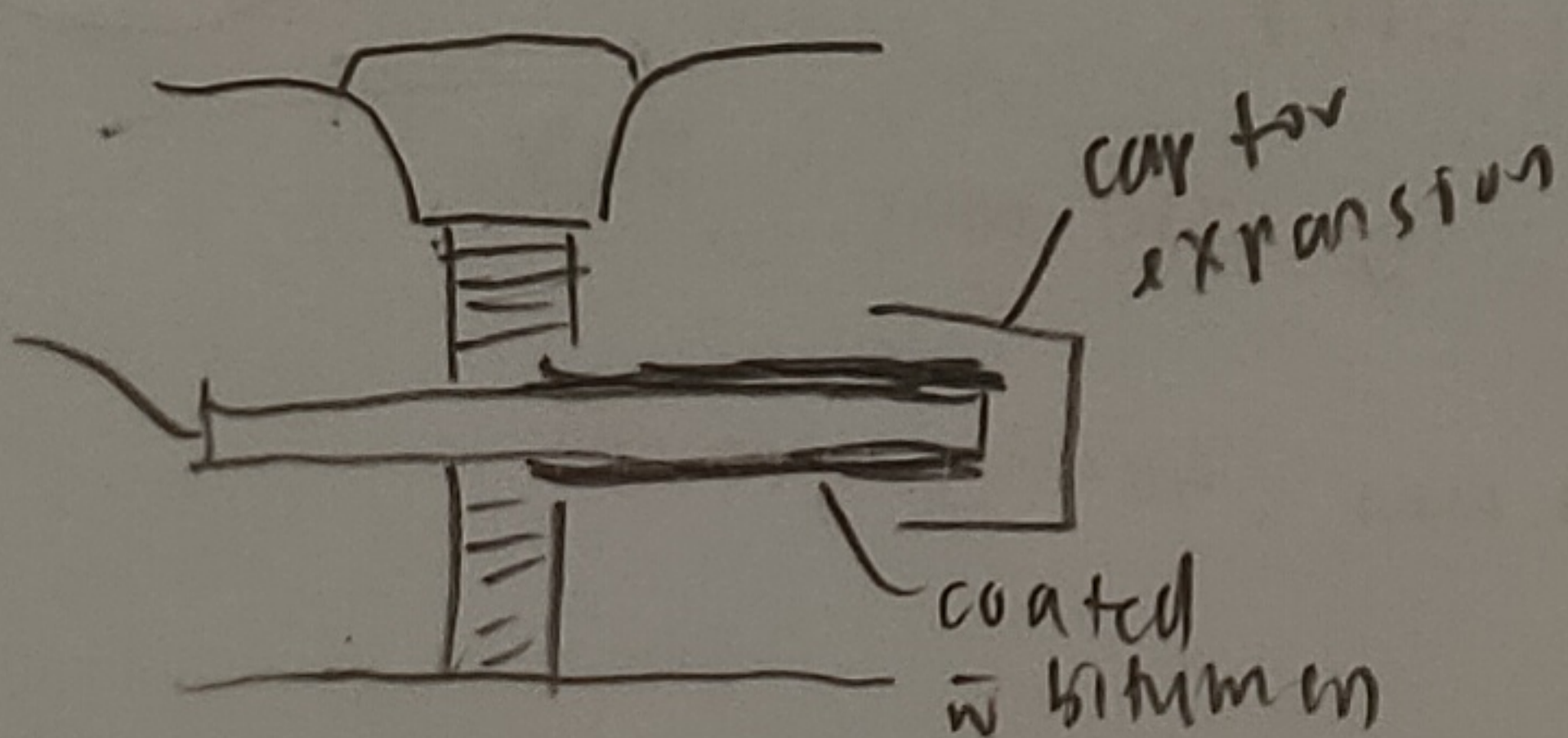
6) a) In rigid pavement structure, the SIB is used to remedy an unsatisfactory S/G condition. It controls S/G volume change as SIB holds down S/G & absorbs some expansion. SIB also improves drainage of water from surface or variable WT. S/G also controls mud pumping which is caused by heavy load, water accumulation & unsuitable soil. S/G also controls frost damage & forms working surface.

b)



Expansion joints are transverse joint for expansion. It is a full depth gap of size 20-25 mm. It consists of a non-protuding & compressible filler capped by bituminous rubberised sealant (for waterproofing). Load transfer is done by dowel bars with one half debonded and installed parallel to each other on surface & joint centreline. It also serve as contraction, construction & warping joints.

Round
dowel
bars



7) a) Equivalent single-axle load or ESAL represent the standard load unit for design, which is 8160 kg (18000 lb) \rightarrow 80kN load on a single axle with pair of dual wheels on each side. Different axle loads can be converted to ESAL using equivalency factors (from table from AASHTO). The damage caused by the loadings can be calculated based on fourth power relationship where damage \propto 4th power of axle load. The loads can also obtained from truck types using truck equivalency factors.

b) i) Daily ESAL = 800 ESAL/day

ESAL in a year = $800 \times 365 = 292000$ ESAL/yr

In 20-year $\Rightarrow 292000 \times fg = 292000 \times \frac{(1+g)^n - 1}{g}$
 $= 292000 \times \frac{(1+0.02)^{20} - 1}{0.02}$

$= 7094831.98 \rightarrow 3547415.5$

≈ 7 million ESALs \Rightarrow 3.55 mil ESALs

ii) Variance value.

S_0 .

ii) $R = 80\%$

$S_0 = 0.45$ (typical for flexible pavement)

$W_{18} = 7$ mil

$\Delta PSI = 4 - 2 = 2$

Variance = 0.3

$S_0 = 0.55$

$SN_1, MR = 30,000$ psi

$SN_2, MR = 15,000$ psi

$SN_3, MR = 6,000$ psi

iii) Variance value represent the uncertainty of the prv design. It is a function of many factors such as variation in traffic prediction, variation in materials or construction & variation in prv performances.

From nomograph

$SN_1 = 2.7$ (2.5)

$SN_2 = 3.5$ (3.3)

$SN_3 = 5$ (4.3)

layer coefficient

$a_1 = 0.42$

$a_2 = 0.249 (\log_{10} MRBS) - 0.977 = 0.249 (\log_{10} 30,000) - 0.977 = 0.138$ 0.15

$a_3 = 0.227 (\log_{10} MRBS) - 0.839 = 0.227 (\log_{10} 15,000) - 0.839 = 0.11$ 0.11

$D_1 = \frac{SN_1}{a_1} = \frac{2.7(25.4)}{0.42} = 163.286 \approx 170$ mm

$D_2 = \frac{SN_2 - a_1 D_1^*}{a_2 m_2} = \frac{3.5(25.4) - 0.42(170)}{0.138(1.20)} = 105.68 \approx 110$ mm 90

$D_3 = \frac{SN_3 - a_1 D_1^* - a_2 m_2 D_2^*}{a_3 m_3} = \frac{5(25.4) - 0.42(170) - 0.138(1.20)(110)}{0.11(1.10)} = 308.96$ mm ≈ 310 mm 240

170 mm asphalt concrete, 110 mm crushed stone & 310 mm sandy gravel