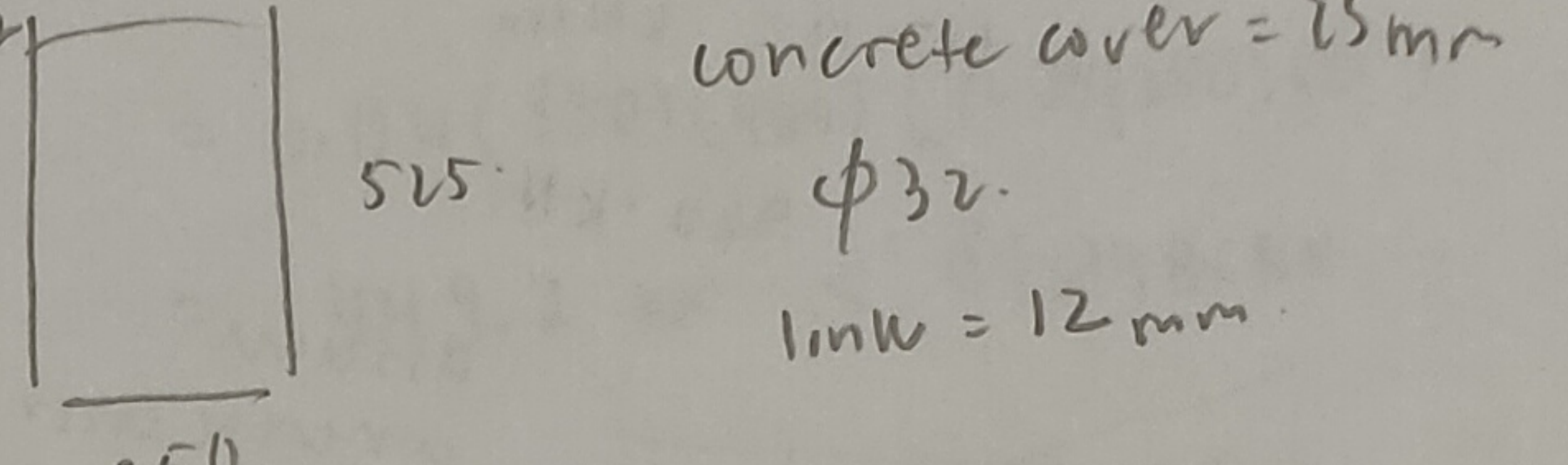
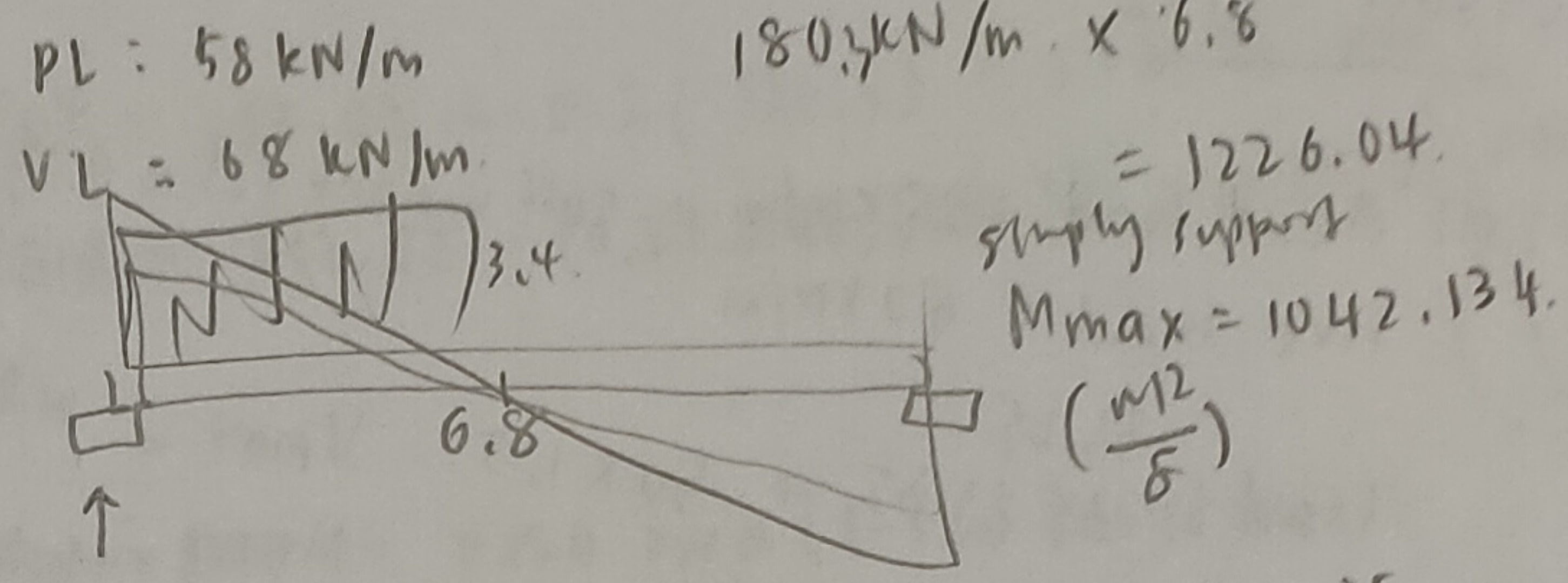


$F_{cc} + F_{sc} = F_{st}$   
 $F_{cw} + F_{cf} + F_{sc} = F_{st}$



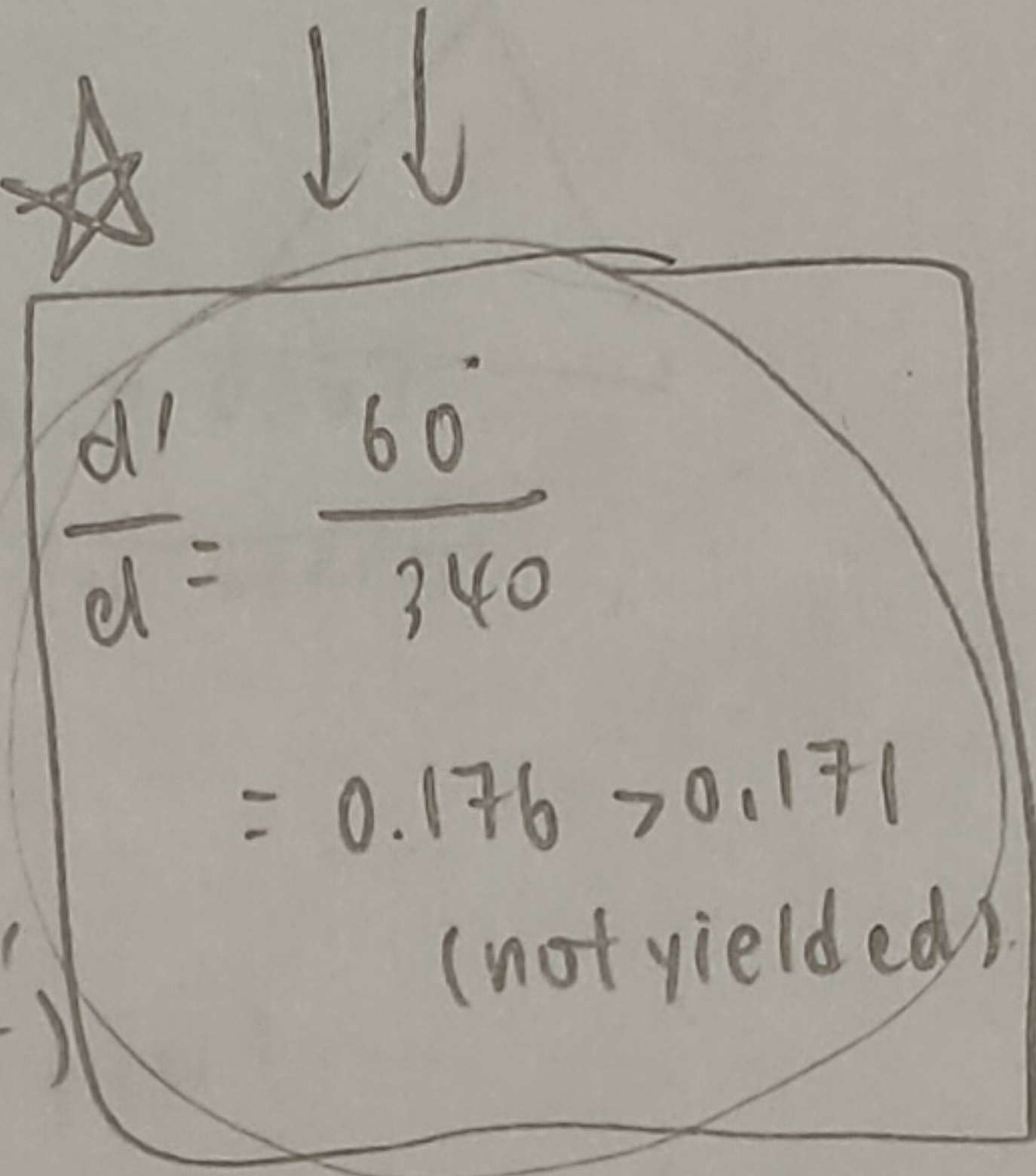
Assume NA <sup>above</sup> ~~below~~ flange

$F_{cf} + F_{cw} = F_{st}$   
 $0.87 \times 40 \times (400 - 200) \times 100 + 0.567 \times 40 \times 200 \times 0.8x$   
 $= 0.87 \times 500 \times ( )$   
 $453600 + 3628.8x =$

Do not assume comp steel yield!

$d = 525 - 25 - 12 - \frac{32}{2} = 460$   
 $k = \frac{M}{f_{cu} b d^2} = \frac{1042.134 \times 10^3}{25 \times 350 \times 460^2} = 0.568 > 0.167$   
 (Comp. steel needed)

$F_c + F_{sc} = F_{st}$   
 $0.567 \times 40 \times 400 \times 0.8x + 0.87(500)(603)$   
 $= 0.87(500)(2414)$   
 $0.567 \times 40 \times 400 \times 0.8x = 787785$



$d' = 25 + 12 + 16 = 53$   
 $\frac{d'}{d} = 0.115 < 0.171$  yielded.

Assume below flange  $x = 108.55 > 100$

$F_{cf} + F_{cw} + F_{sc} = F_{st}$   
 $0.567 f_{ck} (b - b_w) h_f + 0.567 f_{cw} b_w (0.8x) + 0.87 f_{sc} (603) = 0.87(500)(2414)$

$A_s' = \frac{(k - k_{bal}) f_{cu} b d^2}{0.87 f_{yk} (d - d')}$   
 $= 4141.286 \text{ mm}^2$   
 $A_s = \frac{k_{bal} f_{cu} b d^2}{0.87 f_{yk} z} + A_s'$   
 $= 1884.43 + 4141.286 = 6025.71$

$453600 + 0.567(40)(200)(0.8x) = 787785$   
 $0.567(40)(200)(0.8x) = 334185$   
 $x = 92.09 \text{ mm}$

$453600 + 3628.8x + 700 \frac{(x-60)}{x} (603) = 1050090$   
 $3628.8x + 422100 \left(\frac{x-60}{x}\right) = 596490$

$\frac{x}{d} = 0.326 < 0.617$

$3628.8x^2 + 422100x - 25326000 = 596490x$

$x = 110.96 \text{ mm}$  or  $-62.89 \text{ mm}$   
 $> h_f \therefore \text{correct!}$

$M_f = 0.567(40)(400-200)(100)(340 - 0.5 \times 100)$   
 $= 131.54 \text{ kNm}$

$k_w = \frac{M - M_f}{f_{cu} b_w d^2} = 0.074 < 0.167$

$M_w = F_{cw} (d - 0.4x) = 0.567(40)(200)(0.8 \times 110.96)(340 - 0.4 \times 110.96)$   
 $= 119.03 \text{ kNm}$

$M_R = M_f + M_w + F_{sc} z_c$   
 $= 131.94 \text{ kNm} + 250 \text{ kNm} = 381.94 \text{ kNm} > 250 \text{ kNm} \text{ ok!}$

$F_{sc} z_c = 422100 \left(\frac{x-60}{x}\right) (d - 0.4x)$   
 $= 257.3 \text{ kNm}$   
 $= 250 + 257.3 = 507.3 \text{ kNm} > 250 \text{ kNm}$



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$(1.2 \times 0.1) + (0.7 \times 0.7)$

1) a) dead load = 25 kN/m + self weight  $(25 \times 0.33) = 33.25$   
 live load = 50 kN/m.

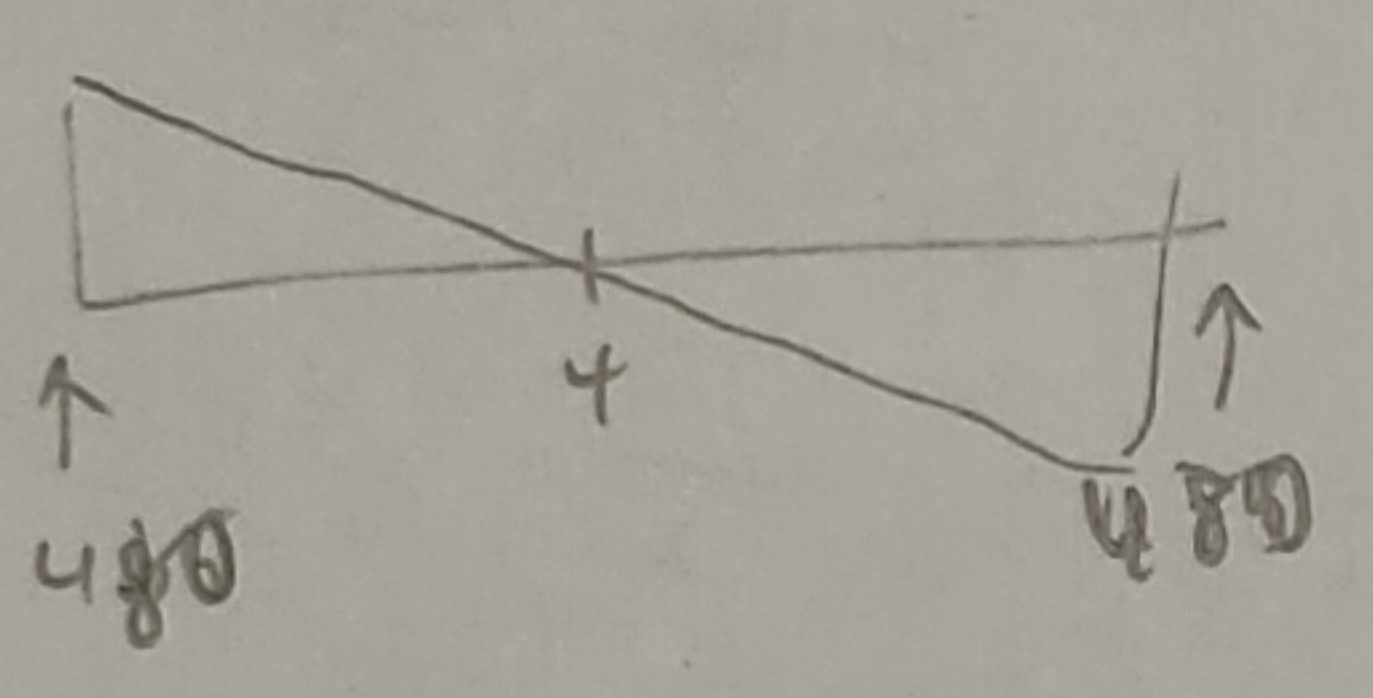
2) a)  $F_c = F_{ST}$

load =  $33.25 + 50 \times 1.5 = 112.0$  kN/m.

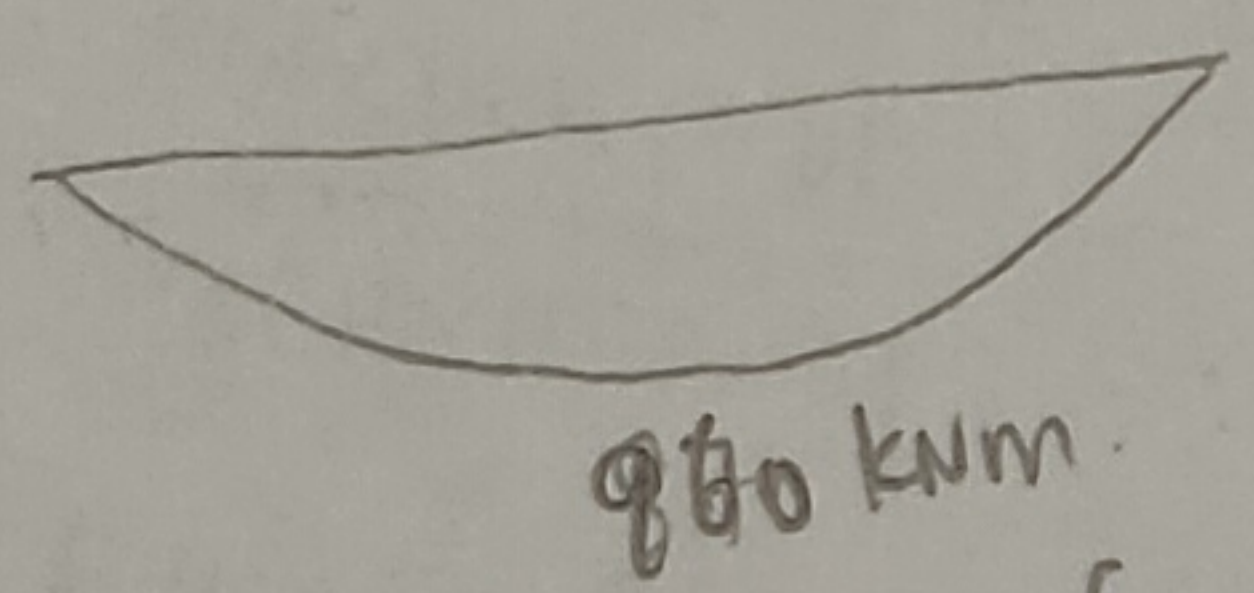
$V_{max} = wL/2 = \frac{120(8)}{2} = 480$   
 $M_{max} = wL^2/8 = \frac{120(8)^2}{8} = 960$

$0.567 f_{ck} b_s = 0.87 \times 500 \times 943$   
 $0.567 f_{ck} (600)(0.8x) = 410205$   
 $10886.4x = 410205$

$1120 \times 8 = 960$  kN



assume concrete cover = 30  
 link dia = 8  
 $d = 800 - 30 - 8 - \frac{32}{2}$

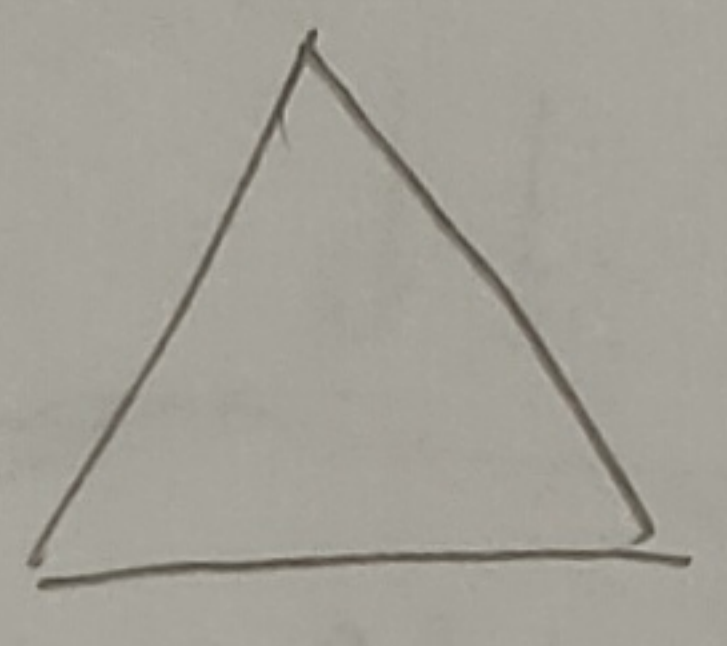


$= 746$   
 $f_{cu} = 40$  N/mm<sup>2</sup>

max opening

$\eta = 0.45d = 550(0.45) = 247.5$  mm.  
 $s = 0.8x = 198$  mm.

$k = \frac{M}{f_{cu} b d^2} = \frac{960 \times 10^6}{25 \times 1200 \times 746^2} = 0.058 < 0.167$



$z = (0.5 + \sqrt{0.25 - \frac{k}{1.135}}) d = 705$  mm

Area =  $\frac{1}{2} \times 600 \times 600 - 150L = 180000 - 150L$

$s = a(d-z) = 82$  mm

$0.567 \times 40 \times (180000 - 150L) = 410205$

$s > h_f$ :

$M_f = 0.567 f_{cu} (b_s b_w) h_f (d - 0.5 h_f) = 1420.68$  kNm

$4082400 - 3402L = 410205$

$k_w = \frac{(M - M_f)}{f_{cu} b_w d^2}$

$-3402L = -3672195$

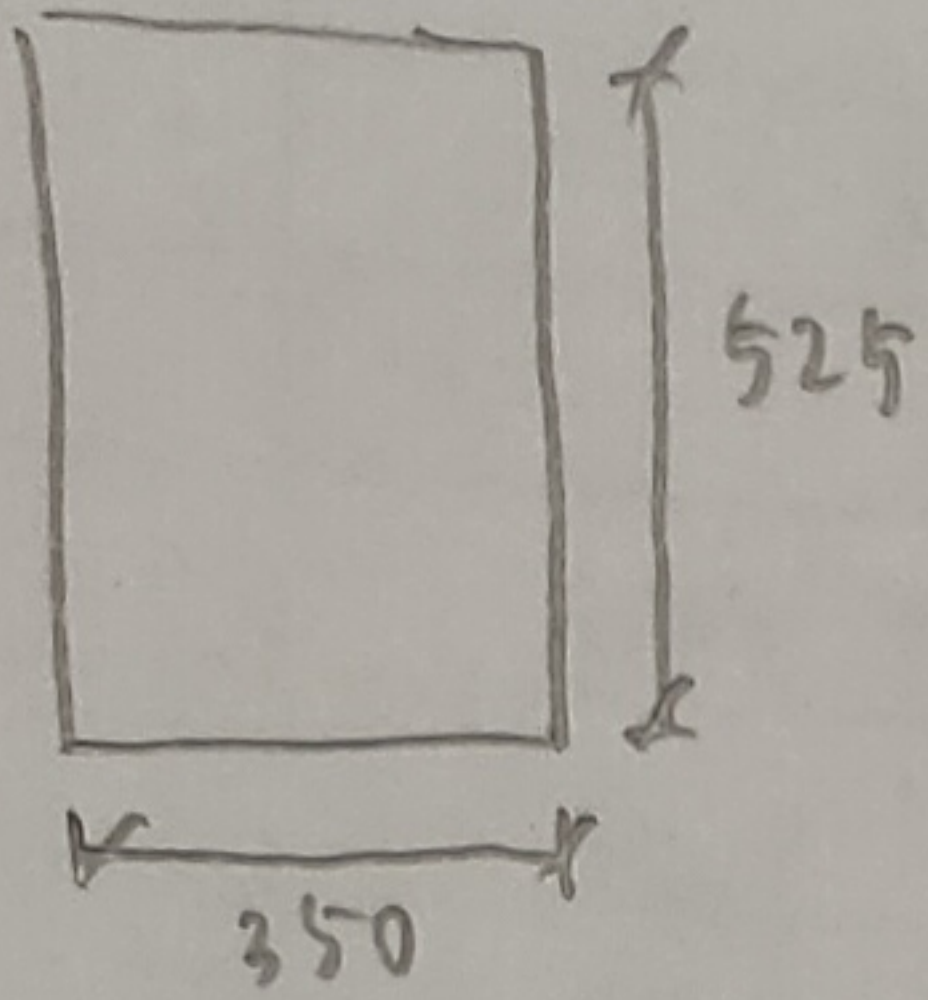
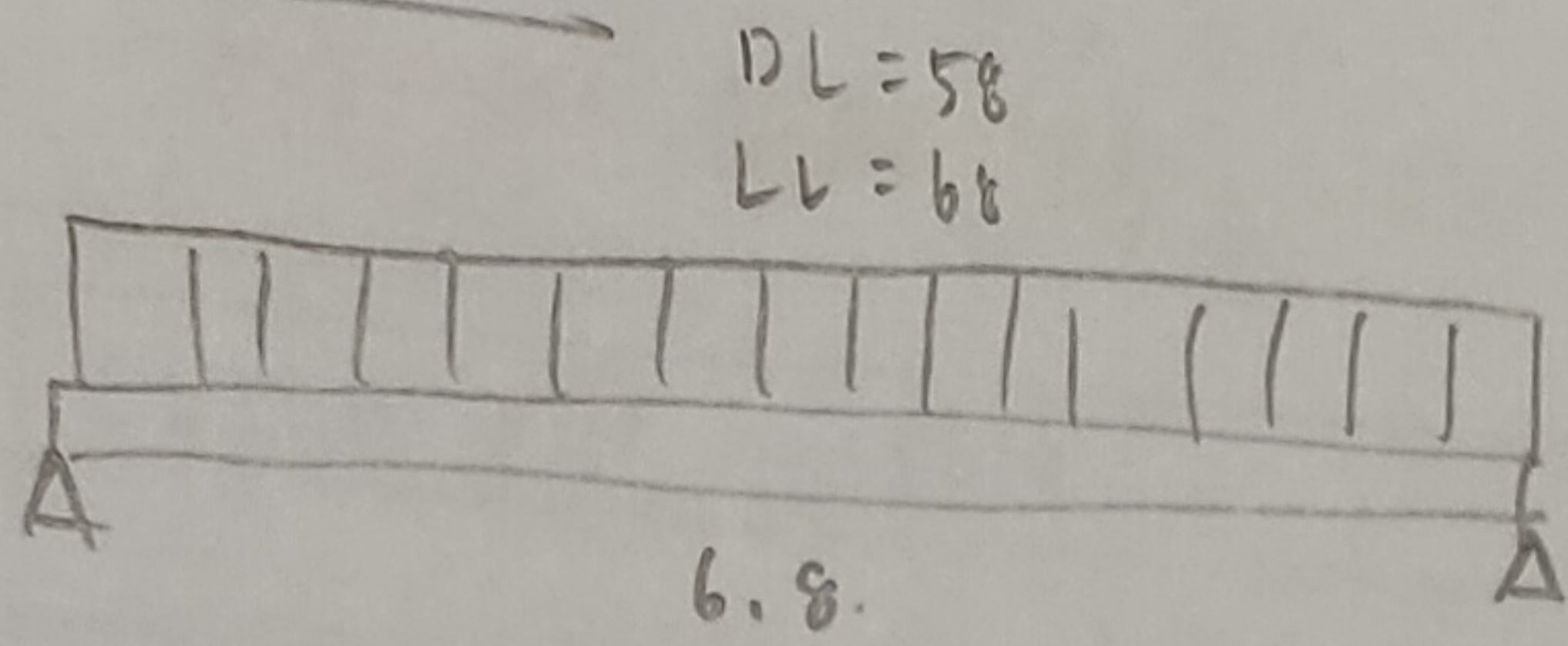
$A_s = \frac{M}{0.47 f_y \eta z} = \frac{960 \times 10^6}{0.87 \times 500 \times 705} = 3130$  mm<sup>2</sup>

$L = 1079$

$4.132 \times 10^4 = 3218$  mm<sup>2</sup>



PYP 18/19



Assume  
 concrete cover = 25mm  
 link diameter = 12mm  
 bar diameter = 32mm  
 $d = 525 - 25 - 12 - \frac{32}{2}$   
 $= 472 \text{ mm}$   
 $d = 460 \text{ mm}$

Load =  $1.35 \times 58 + 1.5 \times 68 = 180.3$

$V_{max} = wL/2 = 613.02 \text{ kN}$

$M_{max} = wL^2/8 = 1042.134 \text{ kNm}$

$k = \frac{M}{f_{cu} b d^2} = \frac{1042.134 \times 10^6}{25 \times 350 \times 460^2} = 0.563 > 0.167$   
 Comp. steel needed.

$d' = 25 + 12 + \frac{32}{2} = 53$

$\frac{d'}{d} = \frac{53}{460} = 0.115 < 0.171$  comp steel yield!

$A_s' = \frac{(k - k_{bal}) f_{cu} b d^2}{0.87 f_{yk} (d - d')} = \frac{(0.563 - 0.167) (25) (350) (460)^2}{0.87 (500) (460 - 53)}$   
 $= 4141.3 \text{ mm}^2$

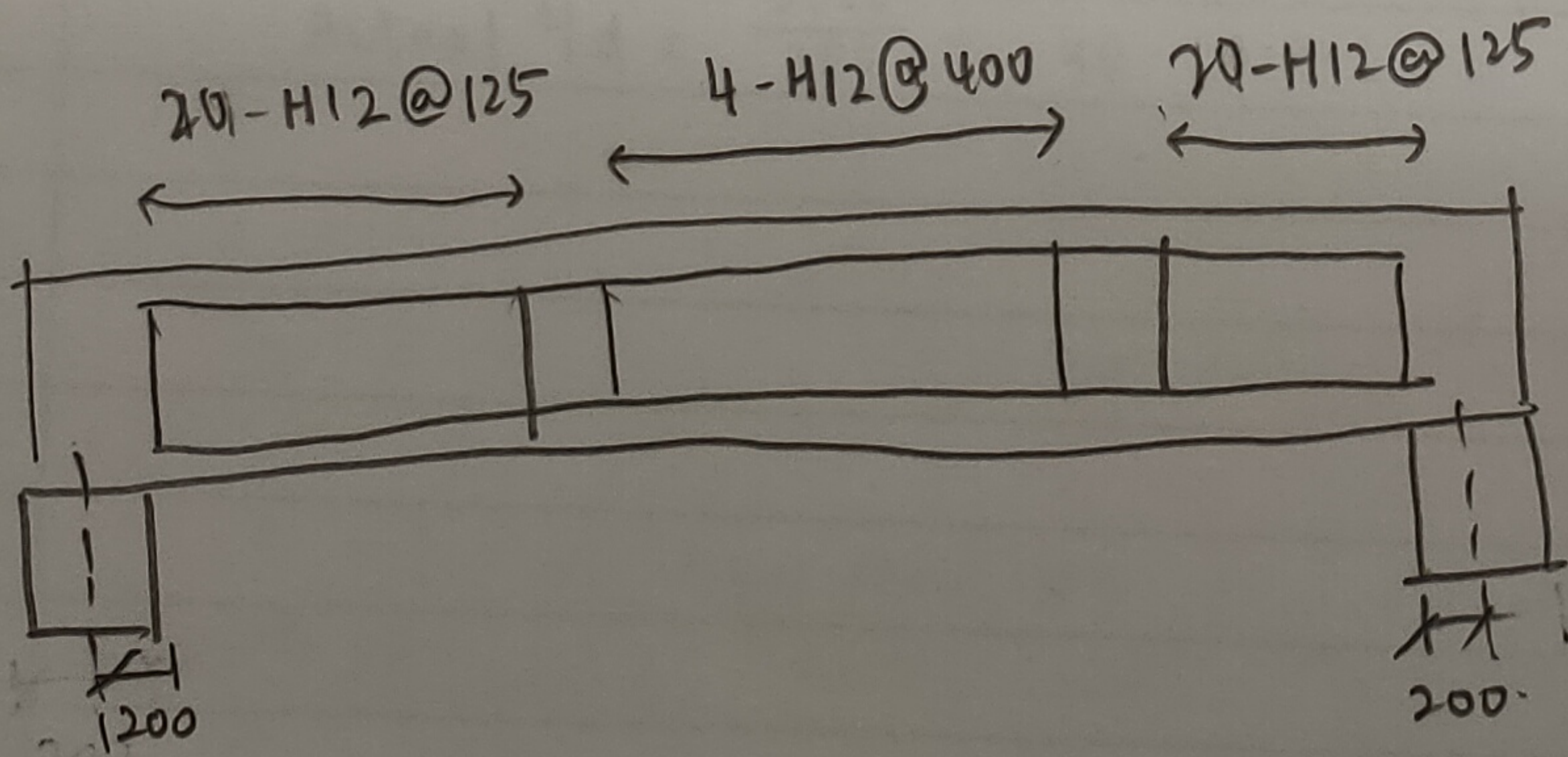
⇒ provide 6H32 (= 4827 mm<sup>2</sup>)

$A_s = \frac{k_{bal} f_{cu} b d^2}{0.87 f_{yk} z} + A_s'$   
 $z = d \left( 0.5 + \sqrt{0.25 - \frac{k}{1.135}} \right)$   
 $z = 0.82d$

$= \frac{0.167 (25) (350) (460)^2}{0.87 (500) (0.82 \times 460)} + A_s'$

$= 1884.43 + 4141.3 = 6025.73 \text{ mm}^2$

⇒ 8H32 (= 6437 mm<sup>2</sup>)



$z_3 \Rightarrow X_L = 6.8 - 2(2.375) - 2(0.2)$   
 $= 1.55 \text{ m}$

no. of links =  $\frac{X_L}{s} - 1 = \frac{1650}{400} - 1 = 3.125$   
 $\approx 4$

b)  $V_{EF} = 613.02 - 0.2(180.3) = 576.96 \text{ kN}$   
 $V_{EId} = 613.02 - (0.2 + 0.46)(180.3) = 494.02 \text{ kN}$

$V_{Rd,max(22)} = 0.124 b w d (1 - f_{cu} / 250) f_{cu}$   
 $= 0.124 (350) (460) (1 - 25/250) (25)$   
 $= 449.2 \text{ kN} < 576.96 \text{ kN}$

$V_{Rd,max(45)} = 0.18 b w d (1 - f_{cu} / 250) f_{cu}$   
 $= 652.1 \text{ kN} > 576.96$

$\theta = 0.5 \sin^{-1} \left\{ \frac{V_{EF}}{V_{Rd,max(45)}} \right\}$   
 $= 0.5 \sin^{-1} \left( \frac{576.96}{652.1} \right)$   
 $= 31.11^\circ$

$\cot \theta = 1.66$

$\left( \frac{A_{sw}}{s} \right) = \frac{V_{EId}}{0.78 f_{yk} d \cot \theta} = \frac{494.02}{0.78 (460) (500) (1.66)}$   
 $= 1.66$

⇒ use  $\phi 12 @ 125$  spacing  
 $\frac{A_{sw}}{s} = 1.808$

Minimum stirrup

$V_2 = 0.0624 (f_{cu}^{0.5} b w d) \cot \theta$   
 $= 0.0624 (25^{0.5} (350) (460)) (1.66)$   
 $= 83.385 \text{ kN}$

$\frac{A_{sw}}{s} = \frac{V_2}{0.78 d f_{yk} \cot \theta} = \frac{83.385}{0.78 (460) (500) (1.66)}$   
 $\frac{0.09 f_{cu}^{0.5} b w}{f_{yk}} = 0.28$

⇒ use  $\phi 12 @ 400$  spacing ( $A_{sw}/s = 0.565$ )

$V_2 = \frac{A_{sw}}{s} \times 0.78 d f_{yk} \cot \theta$   
 $= 168.26 \text{ kN}$

$X_2 = \frac{V_{EF} - V_{min}}{W} = \frac{576.96 - 168.26}{180.3}$

$= 2.27 \text{ m}$

measure from face of support,  $X = 2.27 - 0.2/2 = 2.17$

no. of stirrup =  $1 + \frac{X}{s} = 1 + \frac{2170}{125} = 17.76$

$20$   
 $(17 - 1) \times 125 = 2125$   
 $\approx 20$



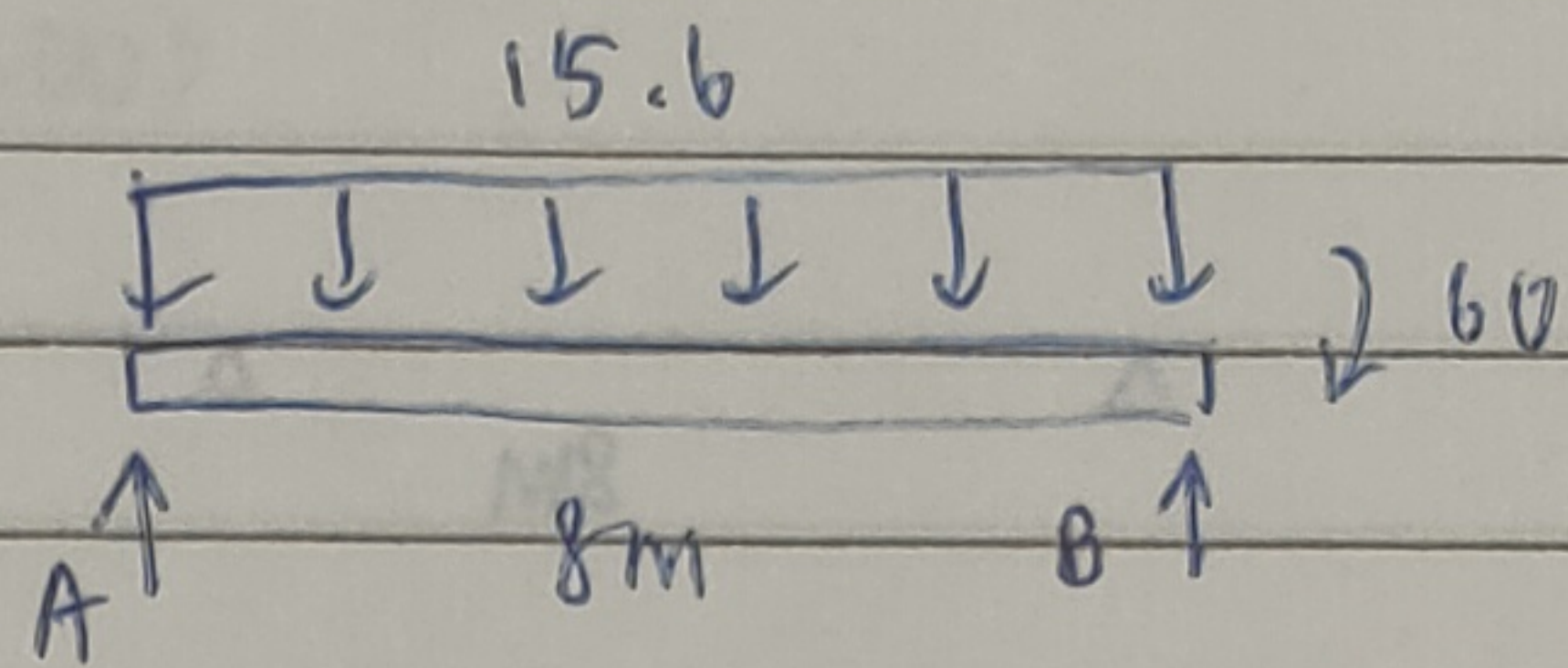
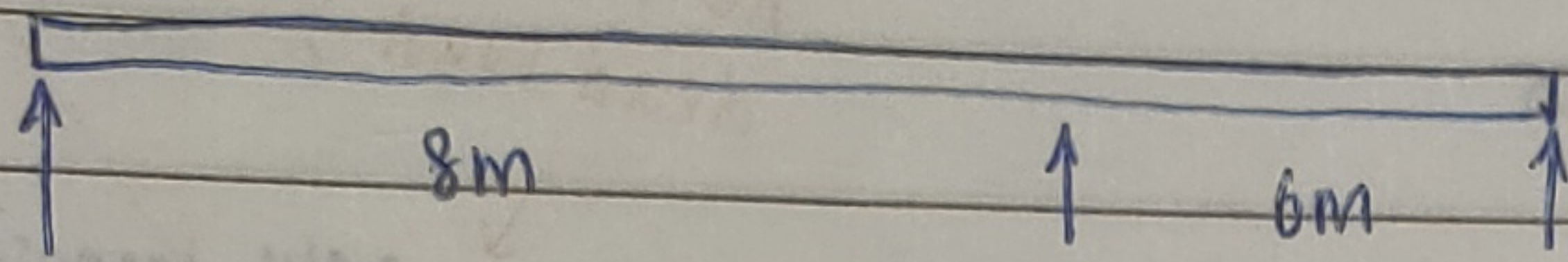
# One-way spanning slab.

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3)



Slab thickness = 240mm

$$DL = 0.24 \times 25 = 6 \text{ kN/m}^2$$

$$LL = 1.5 \text{ kN/m}^2$$

assume each bay = 30 m<sup>2</sup>

$$Q_u / G_u = 5/6 = 0.83 < 1.25$$

$$Q_u = 5 \leq 5 \text{ kN/m}^2$$

∴ use single load case analysis

$$W = 1.35 \times 6 + 1.5 \times 5 = 15.6$$

$$M_{max} = 102.08 \text{ kNm}$$

$$d = 200 \text{ mm}$$

0.116 (after redistribution)

$$k = \frac{M}{f_{cu} b d^2} = 0.102 < 0.167 \text{ (singly reinforced)}$$

$$z = d \left( 0.5 + \sqrt{0.25 - \frac{k}{1.134}} \right) = 0.9 d$$

$$A_{s, req} = \frac{M}{0.87 f_{yk} z} = 1303.7 \text{ mm}^2$$

provide H13 - 9 @ (A<sub>s, prov</sub> = 1475 mm<sup>2</sup>)

$$\sum M_B = 0$$

$$R_A(8) = 15.6(8)(4) - 60(0.8)$$

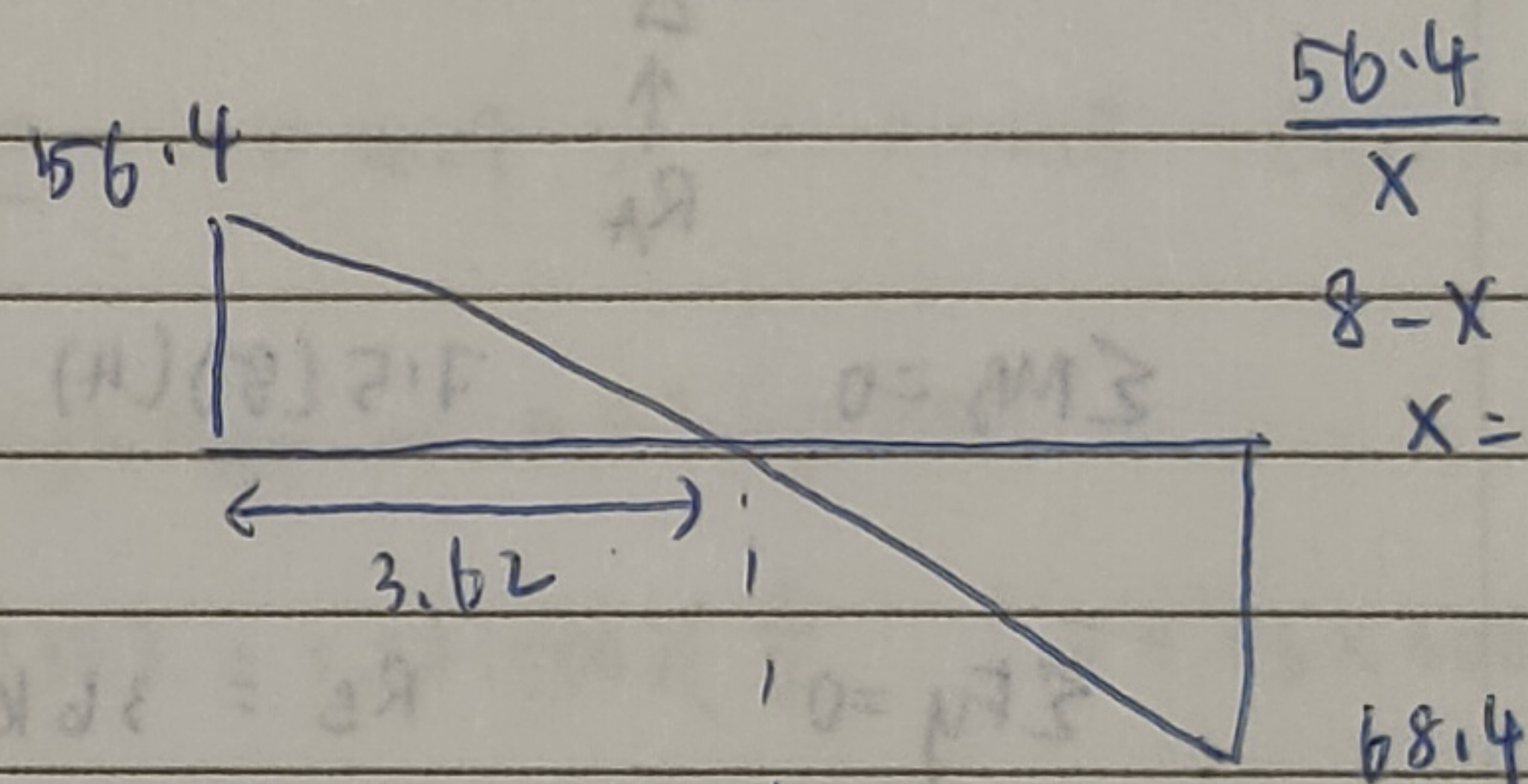
$$R_A = 56.4 \text{ kN}$$

$$\sum F_y = 0$$

$$R_A + R_B = 15.6(8)$$

$$R_B = 68.4 \text{ kN}$$

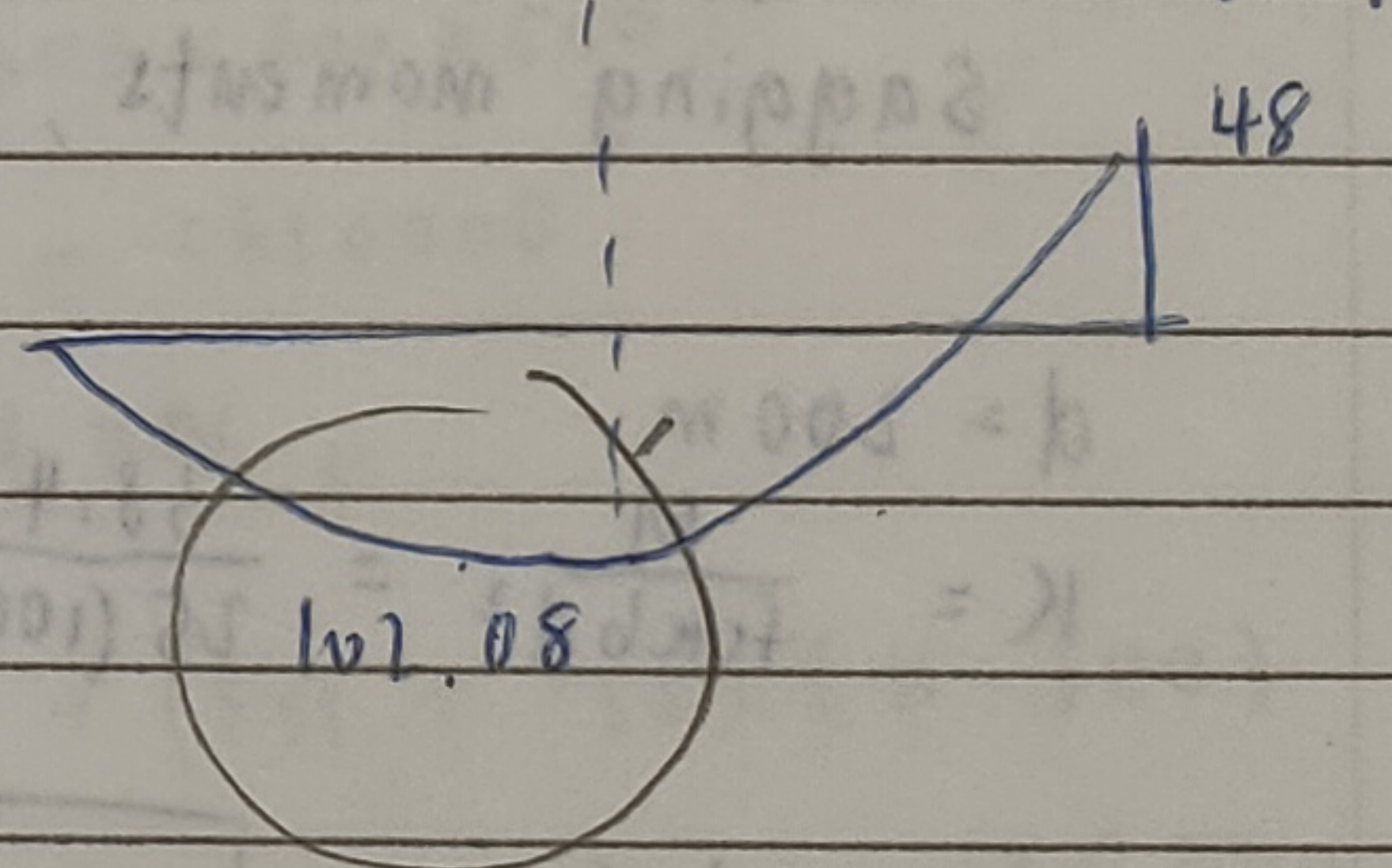
redistribution  
↓



$$\frac{56.4}{x} = \frac{68.4}{8-x}$$

$$8-x = 1.213x$$

$$x = 3.62$$



b) deflection check

$$p = \frac{A_s}{bd} = 0.0065$$

$$p_o = 10^{-3} f_{cu} = 0.005$$

$p > p_o$  (Figure 7) ⇒  $l/d = 17$

$$\text{Allowable } l/d = 17 \times \frac{1475}{1303.7} = 19.23$$

$$\text{Actual } l/d = \frac{8000}{200} = 40 > 19.23$$

$$l/d = 1.3 \left[ 11 + 1.5 \sqrt{25 \frac{0.005}{0.0065} + \frac{1}{12} \sqrt{25} \right]}$$

$$= 21.8$$

$$\text{Allowable} = 21.8 \times \frac{1475}{1303.7} = 24.7$$

$$\text{Actual} = 40 > 24.7$$

$$\frac{21.8}{40} \times \frac{40}{21.8} = 1.87 > 1.5$$

⇒ increase slab thickness

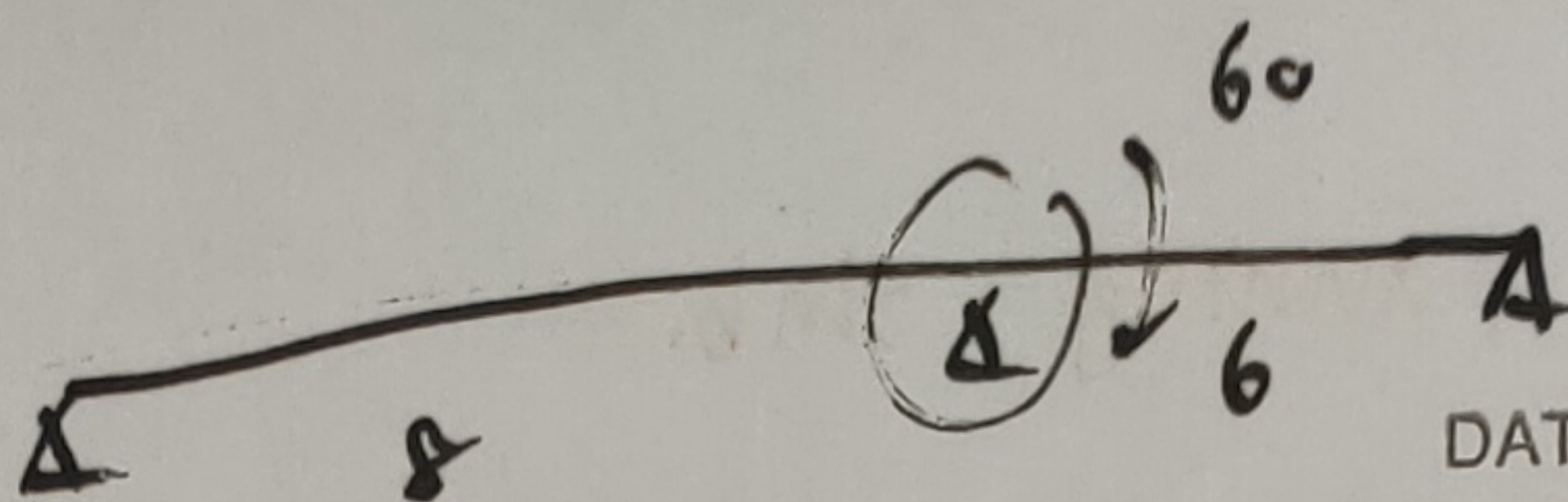
$$f_{t,1.6} = \frac{f_{t,28}}{\gamma} \times \gamma_c = b \cdot d \cdot \gamma_c$$

$$f_{t,1.6} < 0.4 = \frac{8000}{200} = 40$$

$$f_{t,1.6} < 0.4 = \frac{8000}{200} = 40$$



Question don't understand?

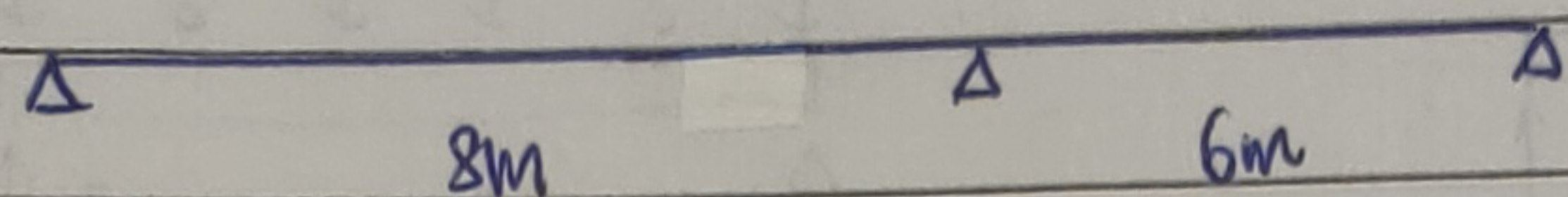


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3) a)



no include dead load?

only imposed load.

$$DL = 0.4 \times 25 = 6 \text{ kN/m}^2$$

$$IL = 5 \text{ kN/m}^2$$

$$W = 1.35 \times 6 + 1.5 \times 5 = 15.6 \text{ kN/m (for 1m strip)}$$

$$F = W \cdot l = 124.8 \text{ kN}$$

$$IL = 5 \text{ kN/m}^2$$

$$W = 1.5 \times 5 = 7.5 \text{ kN/m}$$

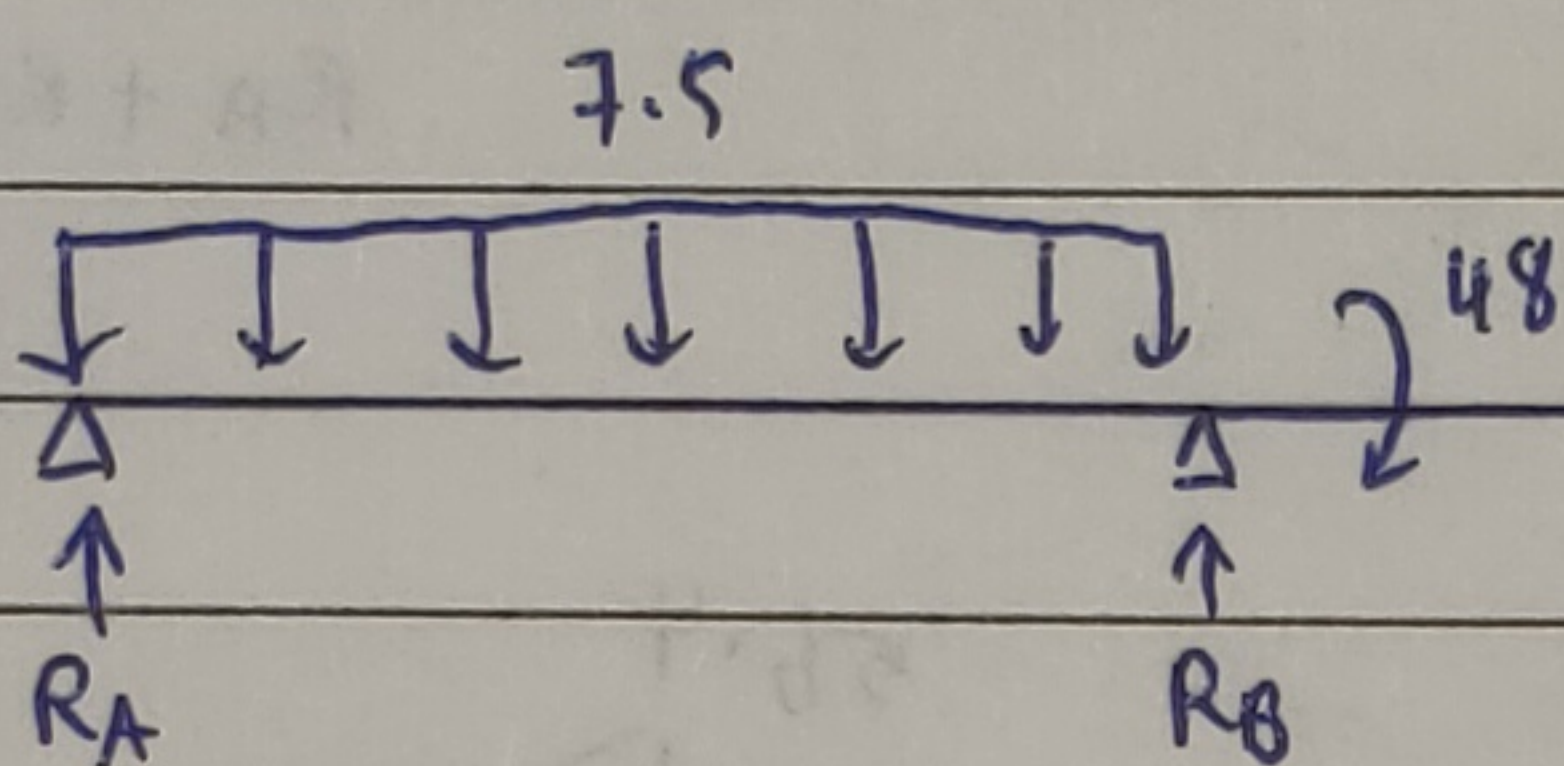
$$F = W \cdot l = 60 \text{ kN}$$

Elastic moment at support B

$$= 60 \times 0.125 \times 8 = 60 \text{ kNm}$$

New support moment

$$= 60 \times 0.8 = 48 \text{ kNm}$$

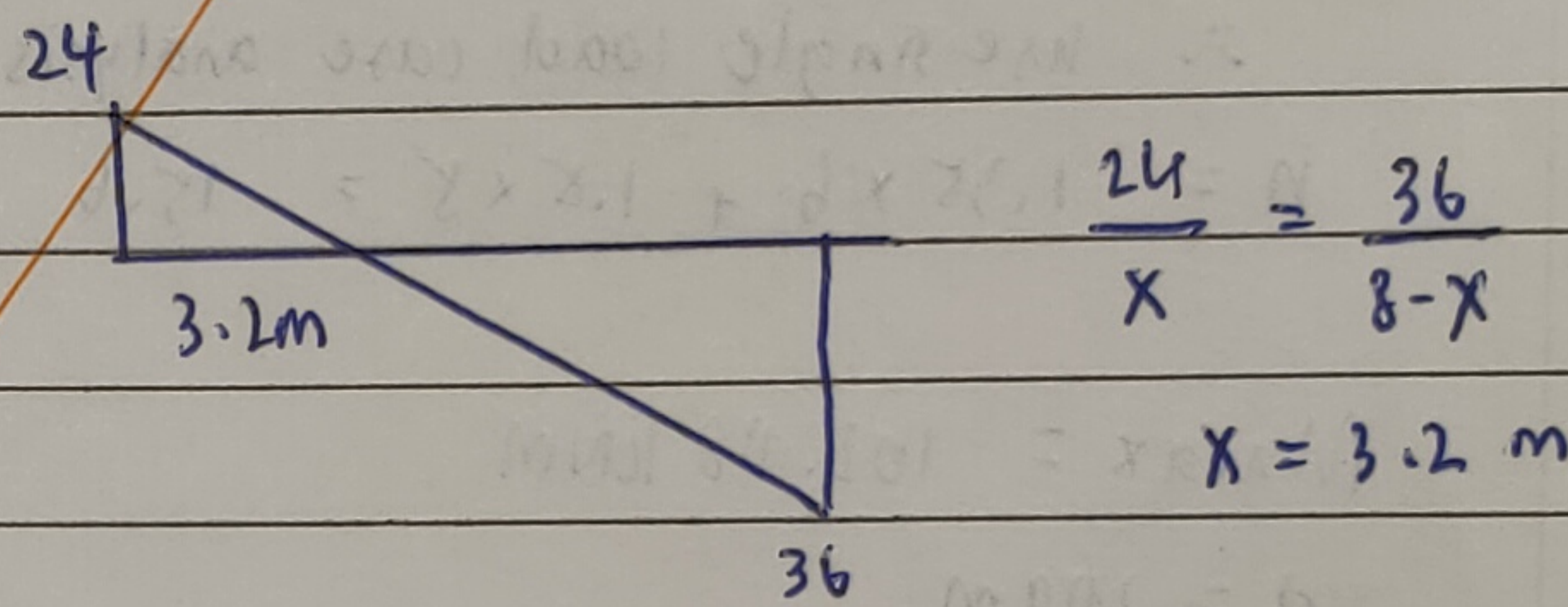


$$\sum M_B = 0 \quad 7.5(8)(4) - 48 = R_A(8)$$

$$R_A = 24 \text{ kN}$$

$$\sum F_y = 0 \quad R_B = 36 \text{ kN}$$

$$\text{Sagging moments, } M_{\max} = 24 \times 3.2 \times \frac{1}{2} = 38.4 \text{ kNm}$$



$$\frac{24}{x} = \frac{36}{8-x}$$

$$x = 3.2 \text{ m}$$

$$d = 200 \text{ mm}$$

$$k = \frac{M}{f_{ck} b d^2} = \frac{38.4 \times 10^6}{25(1000)(200)^2} = 0.0384 < 0.167 \text{ (singly reinforcement)}$$

$$z = d \left( 0.5 + \sqrt{0.25 - \frac{k}{1.134}} \right) = 0.965 d < 0.95 d$$

$$A_s = \frac{M}{0.87 f_y k z} = \frac{38.4 \times 10^6}{0.87 \times 500 \times 0.95 \times 200} = 464.61 \text{ mm}^2 \text{ (} A_{s, \text{req}} \text{)}$$

Provide  $\phi 13$  at spacing of 275 mm,  $A_{s, \text{prov}} = 483 \text{ mm}^2$

$$b) \rho = A_{s, \text{req}} / b d = 0.232\% \leq 0.35\%$$

Basic ratio = 30

$$\text{Allowable } l/d = 30 \times \frac{A_{s, \text{prov}}}{A_{s, \text{req}}} = 31.187$$

$$\text{Actual } l/d = \frac{8000}{200} = 40 > 31.187 \therefore \text{not satisfied.}$$

⇒ Increase the  $A_{s, \text{prov}}$

$$30 \times MF = 40$$

$$\frac{A_{s, \text{prov}}}{A_{s, \text{req}}} = 1.33 < 1.5$$

$$A_{s, \text{prov}} = 619.48 \text{ mm}^2$$

$$\Rightarrow H13 = 200 \text{ (} A_{s, \text{prov}} = 664 \text{ mm}^2 \text{)}$$



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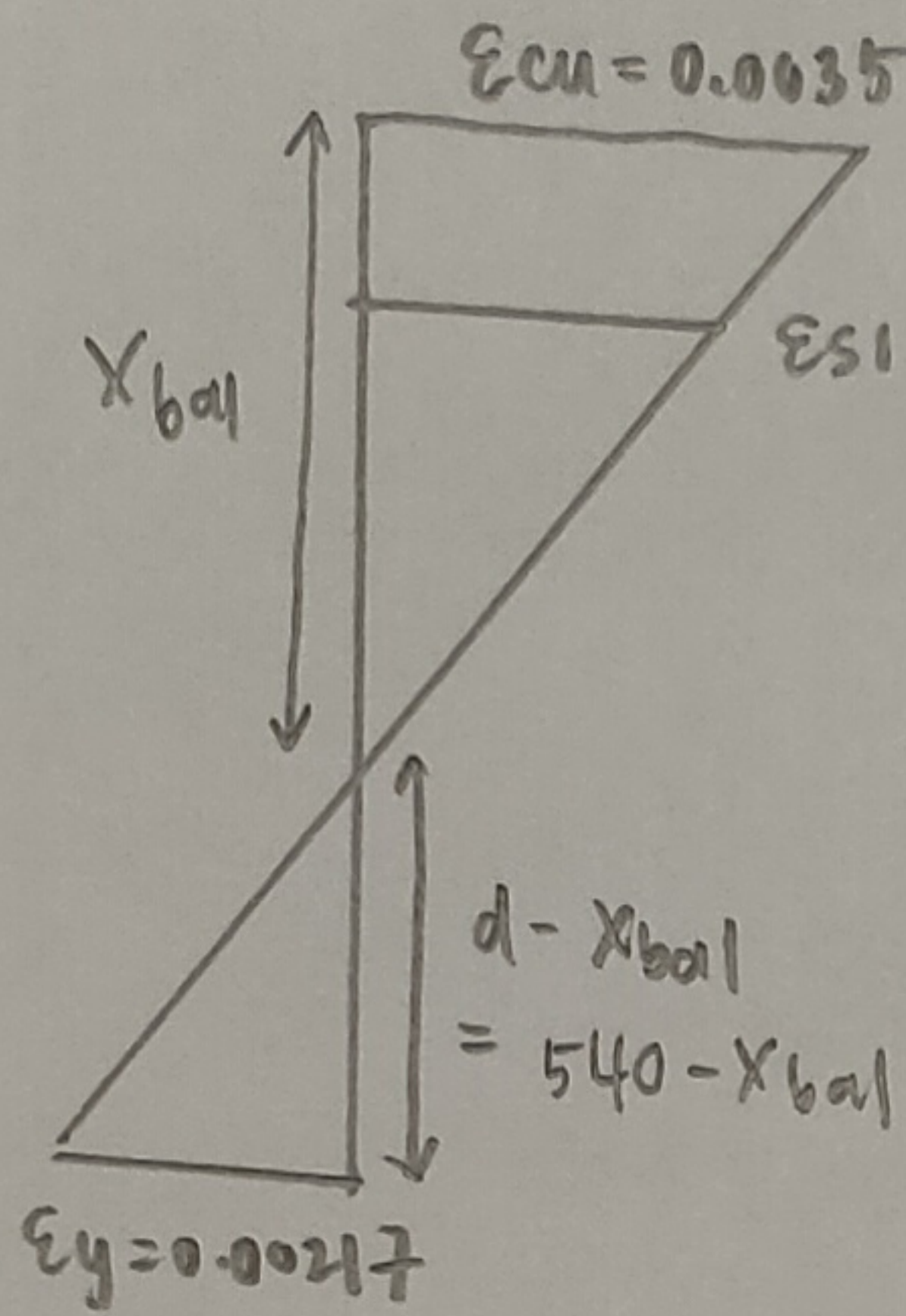
a) For pure compression failure ( $M=0$ )

$$N_0 = 0.567 f_{ck} A_c + 0.87 f_{yk} A_{sc}$$

$$= 0.567 (50) (600 \times 500) + 0.87 (500) (0.03 \times 600 \times 500)$$

$$= \underline{12420 \text{ kN}}$$

b) Balanced condition of failure



$$\frac{X_{bal}}{540 - X_{bal}} = \frac{0.0035}{0.00217}$$

$$0.62 X_{bal} = 540 - X_{bal}$$

$$1.62 X_{bal} = 540$$

$$X_{bal} = 333 \text{ mm}$$

check if compress steel yield

$$\Rightarrow \epsilon_{sc} = 0.0035 \times \frac{333 - 60}{333} = 0.0029 > 0.00217 \text{ (yielded)}$$

$$N_{bal} = 0.567 f_{ck} A_c + 0.87 f_{yk} A_{sc1} - 0.87 f_{yk} A_{sc2}$$

$$= 0.567 (50) (500) (0.8 \times 333) + 0.87 (500) \left( \frac{1}{3} \times 500 \times 0.03 \times 600 \times 500 \right)$$

$$- 0.87 (500) \left( \frac{2}{3} \times 500 \times 0.03 \times 600 \times 500 \right)$$

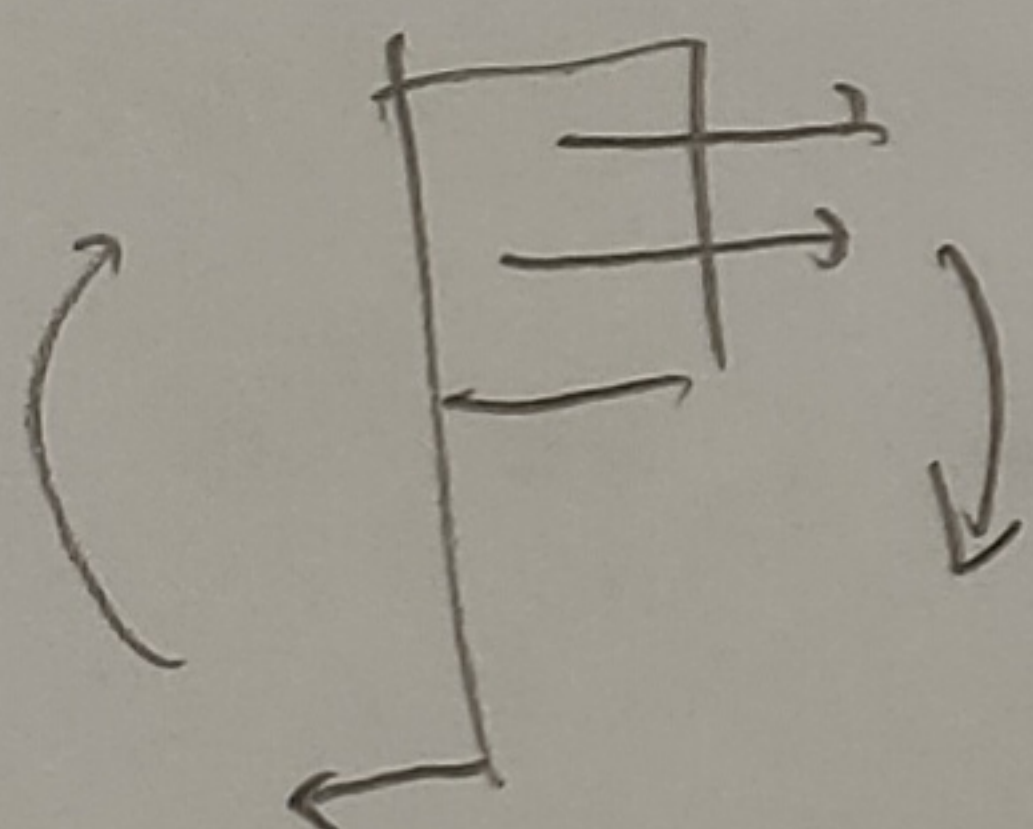
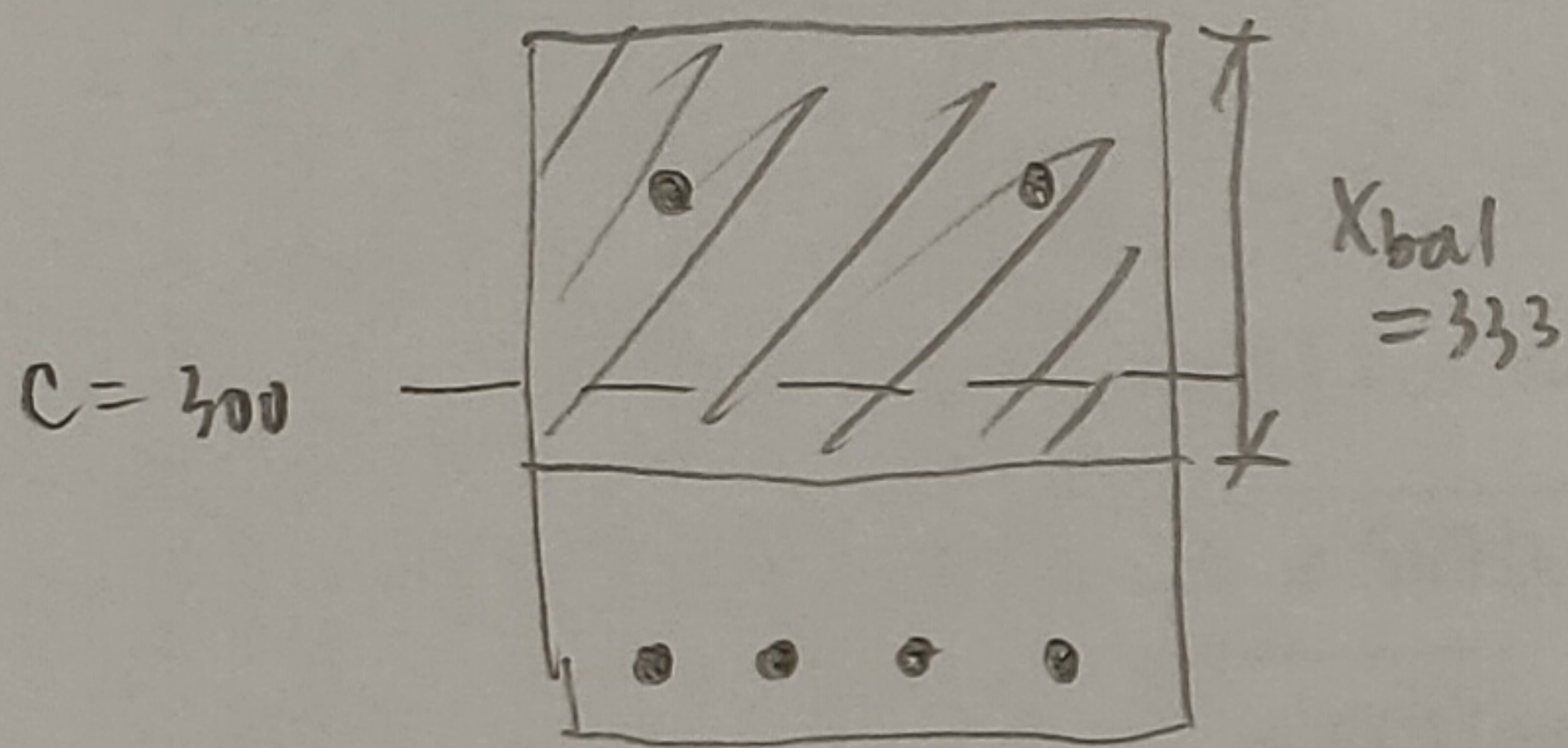
$$= 3776220 + 1305000 - 2610000$$

$$= 2471220 = \underline{2471.22 \text{ kN}}$$

$$M_{bal} = F_c (300 - 0.4 (333)) + (F_{s1} + F_{s2}) (d - 300)$$

$$= 3776220 (166.8) + (1305000 + 2610000) (540 - 300)$$

$$= \underline{1569.5 \text{ kNm}}$$



c) Pure bending failure ( $N=0$ )

Assume comp. steel has NOT yielded.

$$\epsilon_{s1} = \frac{x-60}{x} \times 0.0035$$

$$f_{s1} = E_{s1} \epsilon_{s1} = 200 \times 10^3 \times 0.0035 \times \frac{x-60}{x}$$

$$= \frac{700(x-60)}{x}$$

$$\sum F = 0$$

$$F_{s1} + F_c = F_{s2}$$

$$0.87 \left( \frac{700(x-60)}{x} \right) \left( \frac{1}{3} \times 0.03 \times 600 \times 500 \right) + 0.567 (50) (500) (0.4x) = 0.87 (500) \left( \frac{2}{3} \times 0.03 \times 600 \times 500 \right)$$

$$2100000 \left( \frac{x-60}{x} \right) + 11340x = 2610000$$

$$2100000x - (26000000) + 11340x^2 - 2610000x = 0$$

$$11340x^2 - 510000x - 12600000 = 0$$

$$x = 130.3 \text{ mm}$$

$$f_{s1} \Rightarrow 377.67 \text{ MPa} \rightarrow F_{s1} = 1133000 \text{ N}$$



Taking moment at centreline of tension steel.

$$\begin{aligned}
 M &= F_c(d-0.4x) + F_s(d-d') \\
 &= 0.567(50)(500)(0.8 \times 130.3)(540 - 0.4 \times 130.3) + 1133000.77(540 - 60) \\
 &= 720892463.8 + 543840369.6 \\
 &= \underline{1264.73 \text{ kNm}}
 \end{aligned}$$

