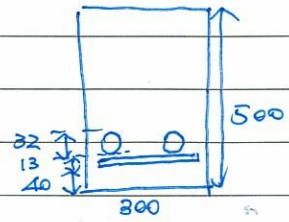
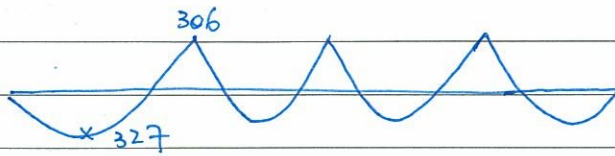


a) after 0.85 distribution



$$360 \times 0.85 = 306$$

$$360 - 306 = 54$$

$$54/2 = 27$$

$$300 + 27 = 327$$

height of beam = 500mm. concrete cover: 40mm, stirrup size: 13mm
assume diameter of steel bars 32mm.

$$d = 500 - 40 - 13 - \frac{32}{2} = 431 \text{ mm}$$

$$K = M / bd^2 f_{ck} = (327 \times 10^6) / (300)(431)^2 (40) = 0.147 < 0.167 \quad \delta = 1$$

∴ singly reinforced, compression steel is not needed.

$$z = d \left(0.5 + \sqrt{0.25 - \frac{K}{1.134}} \right) = 0.847d = 365 \text{ mm} < 0.95d$$

$$A_s = M / 0.87 f_{yk} z = 327 \times 10^6 / (0.87 \times 500 \times 365) = 2059.5 \text{ mm}^2$$

provide 3H32 $A_s = 2414 \text{ mm}^2$

b) $K = M / bd^2 f_{ck} = 306 \times 10^6 / (300)(431)^2 (40) = 0.137 > K_{bal} = 0.129$

∴ compression steel is needed.

$$d' = 40 + 13 + \frac{32}{2} = 69 \text{ mm}$$

$$d'/d = 69/431 = 0.16 > 0.125$$

∴ compression steel has not yielded.

$$\epsilon_{sc} = 0.0035(x - d') / x$$

$$x_{bal} = 0.328(431) = 141.4$$

$$= 0.00179169$$

$$f_{sc} = E_s \cdot \epsilon_{sc} = 200 \times 10^3 \times 0.00179169 = 358.34 \text{ N/mm}^2$$

$$A'_{sc} = \frac{(K - K_{bal}) f_{ck} b d^2}{f_{sc} (d - d')} = \frac{(0.137 - 0.129) (40) (300) (431)^2}{358.34 (431 - 69)} = 137.5$$

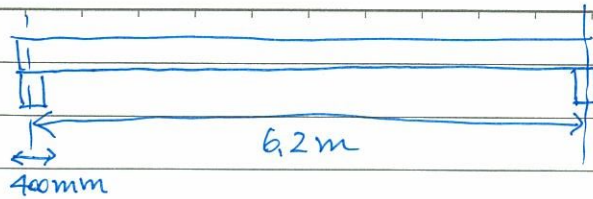
$$A_s = \frac{K_{bal} f_{ck} b d^2}{0.87 f_{yk} z} + A'_{sc} \left(\frac{f_{sc}}{0.87 f_{yk}} \right) \quad z_{bal} = 0.869(431) = 374.54$$

$$= \frac{0.129 (40) (300) (431)^2}{0.87 (500) (374.54)} + 137.5 \left(\frac{358.34}{0.87 \times 500} \right)$$

$$= 1765 + 113.3$$

$$= 1878 \text{ mm}^2$$

2a)



$$\text{Design load} = 1.35 \times 70 + 1.5 \times 46 \\ = 163.5 \text{ kN/m}$$

$$M_{\max} = \frac{1}{8} (163.5)(6.2)^2 = 785.6 \text{ kNm}$$

$$g_k = 70 \text{ kN/m} \quad q_k = 46 \text{ kN/m} \quad h = 575 \quad b_w = 275 \quad d = 575 - 35 - 12 - 3 \times \frac{2}{2}$$

$$n = 1.35(70) + 1.5(46) = 163.5 \text{ kN/m} \quad = 512$$

$$V_{\max} = 163.5 \times 6.2 / 2 = 506.85 \text{ kN}$$

assume steel bar $\phi 32$

$$V_{\text{ef}} = V_{\max} - n \times l_w \times 0.5 \\ = 506.85 - 163.5 \times 400 \times 0.5 \times 1000^{-1} \\ = 474.15 \text{ kN}$$

zone 1

$$V_{\text{rd, max}(22)} = 0.124 b_w d (1 - f_{\text{ck}}/250) f_{\text{ck}} \\ = 0.124 (275) (512) (1 - 40/250) 40 \cdot 10^{-3} \\ = 586.63 \text{ kN} > V_{\text{ef}}$$

$$\text{Let } \theta = 22^\circ \text{ and } \cot(\theta) = 2.5$$

zone 2:

At 1 d ($d = 512 \text{ mm}$) from support face

$$V_{\text{E1d}} = 474.15 - 163.5 \times 0.512 = 390.438 \text{ kN}$$

$$\therefore \frac{A_{\text{sw}}}{s_2} = \frac{V_{\text{E1d}}}{0.78 d f_{\text{yk}} (2.5)} = \frac{390.438 \times 10^3}{0.78 \cdot 512 \cdot 500 \cdot 2.5} = 0.78$$

$$\therefore \text{select } \phi 12 \text{ at } 275 \text{ mm spacing, } A_{\text{sw}}/s = 0.822$$

zone 3:

$$\frac{A_{\text{sw min}}}{s} = \frac{0.08 f_{\text{ck}}^{0.5} b_w}{f_{\text{yk}}} = \frac{0.08 (40)^{0.5} \times 275}{500} = 0.2783$$

$$\text{Select } \phi 12 \text{ at } 400 \text{ mm spacing } A_{\text{sw}}/s = 0.565$$

Actual shear resistance of stirrup is

$$V_{\text{min}} = \frac{A_{\text{sw}}}{s} \cdot 0.78 d f_{\text{yk}} \cot(\theta) = 0.565 (0.78) (512) (500) \times 2.5 \times 10^{-3} \\ = 282.048 \text{ kN}$$

Number of stirrup used for zone 1 & 2

$$X_L = \frac{V_{\text{ef}} - V_{\text{min}}}{n} = \frac{474.15 - 282.048}{163.5} = 1.175 \text{ m}$$

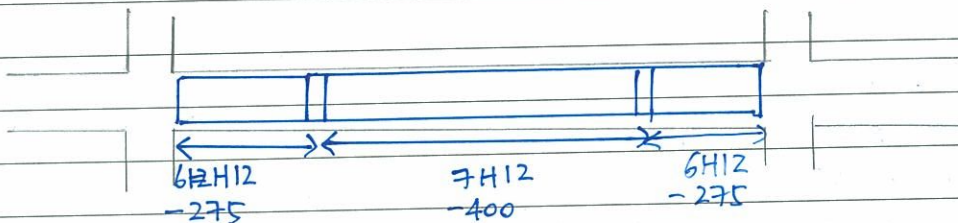
$$\text{Number of links} = 1 + \frac{X_L}{S_2} = 1 + \frac{1.175 \times 10^3}{275} = 5.27 = 6$$

$$\text{Length} = 5 \times 275 = 1375 \text{ mm}$$

number of stirrups used for zone 3.

$$\begin{aligned} L_3 &= L - 2 \times (\text{half width of support}) - 1375 \times 2 \\ &= 6200 - 2 \times (200) - 1375 \times 2 \\ &= 3050 \text{ mm} \end{aligned}$$

$$\text{Number of links} = \frac{L_3}{S_3} - 1 = \frac{3050}{400} - 1 = 6.625 = 7$$



$$a) F_1 = 1 - 0.1 [bf/bw - 1] = 1 - 0.1 [650/275 - 1] = 0.864$$

$$F_2 = \frac{7}{6.2} > 1 \quad F_2 = 1.0$$

$$K = 1$$

$$\psi_2 = 0.6, \quad G_k/Q_k = 70/46 = 1.52, \quad \gamma_G = 1.35, \quad G_{su} = 260 \text{ N/mm}^2$$

$$d = 575 - 35 - 12 - 32/2 = 512 \text{ mm}$$

$$k = \frac{785.6 \times 10^6}{40 \times 650 \times 512^2} = 0.1153 \quad (\text{assume neutral axis lies within flange})$$

$$z = 0.885d = 453 \text{ mm}$$

$$s = 2(d - z) = 2(512 - 453) = 117.6 \text{ mm} < 150 \therefore \text{assumption was correct}$$

$$A_s = 785.6 \times 10^6 / ((0.87) \times 500 \times 453) = 3986.7 \text{ mm}^2 \quad (A_{sreq})$$

$$A_{sprov} \text{ 5H32 } (4023 \text{ mm}^2)$$

$$p = 100(3986) / (275 \times 512) = 2.83\% > 2\% \Rightarrow l/d = 14$$

$$G_s = 260 \times 3987 / 4023 = 258 \text{ ,,}$$

$$F_3 = 310 / 258 = 1.2$$

$$\text{allowable } l/d = 1 \times 14 \times 0.864 \times 1.0 \times 1.2 = 14.5$$

$$\text{Actual } l/d = 6.2(1000) / 512 = 12.11 < 14.5 \text{ (OK)}$$

$$3a) \quad 6/5 = 1.2 \quad n = (0.15 \times 25 + 1.25) \times 1.35 + 1.5 \times 4 = 12.75 \text{ KN/m}^2$$

$$M_x = 0.074 \times 12.75 \times 5^2 = 23.5875 \text{ KNm} \quad d_x = 120 \text{ mm}$$

$$M_y = 0.056 \times 12.75 \times 5^2 = 17.85 \text{ KNm} \quad d_y = 110 \text{ mm}$$

Flexure along X direction:

$$\frac{M}{bd^2 f_{ck}} = \frac{23.5875 \times 10^6}{1000(120)^2 (25)} = 0.0655$$

$$z = d \left(0.5 + \sqrt{0.25 - \frac{0.0655}{1.134}} \right) = 0.9384 d$$

$$A_{s \text{ req}} = \frac{23.5875 \times 10^6}{0.87 \times 500 \times 0.9384 \times 120} = 481.5 \text{ mm}^2/\text{m}$$

$$A_{s \text{ prov}} = H10-150 (524 \text{ mm}^2/\text{m})$$

Flexure along y direction

$$\frac{M}{bd^2 f_{ck}} = \frac{17.85 \times 10^6}{1000(110)^2 (25)} = 0.059$$

$$z = d \left(0.5 + \sqrt{0.25 - \frac{0.059}{1.134}} \right) = 0.945 d$$

$$A_{s \text{ req}} = \frac{17.85 \times 10^6}{0.87 \times 500 \times 0.945 \times 110} = 394.75 \text{ mm}^2/\text{m}$$

$$A_{s \text{ prov}} = H10-180 (437 \text{ mm}^2/\text{m})$$

Deflection check (x direction)

$$P_o = 10^{-3} \sqrt{f_{ck}} = 10^{-3} (25)^{1/2} = 0.005$$

$$P = A_{s \text{ req}} / bd = 481.5 / (1000)(120) = 0.0040 < P_o$$

$$k = 1$$

$$\frac{l}{d} = k \left[11 + 1.5 \sqrt{f_{ck}} \frac{P_o}{P} + 3.2 \sqrt{f_{ck}} \left(\frac{P_o}{P} - 1 \right)^{3/2} \right]$$

$$= 1 \left[11 + 1.5 \sqrt{25} \frac{0.005}{0.004} + 3.2 \sqrt{25} \left(\frac{0.005}{0.004} - 1 \right)^{3/2} \right]$$

$$= 22.375$$

$$\text{Allowable } L/d = 22.375 \times A_{s \text{ prov}} / A_{s \text{ req}} = 22.375 \times 524 / 481.5 = 24.35$$

$$\text{Actual } L/d_x = 5000 / 120 = 41.67 > 24.35 \text{ (Not ok)}$$

b) ① increase $A_{s \text{ prov}}$

$$\text{span}/d = 41.67 = 22.375 \times MF \quad MF = 1.86 = A_{s \text{ prov}} / A_{s \text{ req}}$$

$$A_{s \text{ prov}} = 1.86 \times 481.5 = 897 \text{ mm}^2$$

$$\text{USE H10-80 (982 mm}^2)$$

② increase slab thickness to 175mm

$$d_x = 145 \text{ mm} \quad d_y = 135 \text{ mm}$$

$$n = (0.175 \times 25 + 1.25) \times 1.35 + 1.5 \times 4 = 13.6 \text{ kN/m}^2$$

$$M_x = 0.047 \times 13.6 \times 5^2 = 15.98 \text{ kNm}$$

$$M_y = 0.056 \times 13.6 \times 5^2 = 19.04 \text{ kNm}$$

x direction :

$$\frac{M}{bd^2 f_{ck}} = \frac{15.98 \times 10^6}{1000 (145)^2 (25)} = 0.0304$$

$$z = d \left(0.5 + \sqrt{0.25 - \frac{k}{1.134}} \right) = 0.97d \quad \text{use } z = 0.95d$$

$$A_{sreq} = \frac{15.98 \times 10^6}{0.87 \times 500 \times 0.95 \times 145} = 266.7 \text{ mm}^2/\text{m}$$

$$\text{use H10} - \overset{250}{\cancel{286}} \overset{275}{\cancel{275}} \quad (A_{sprov} = \overset{314}{\cancel{286}} \text{ mm}^2/\text{m})$$

$$p = A_{sreq} / b d x = 266.7 / (1000) / 145 = 0.00184 < 0.35\%$$

$$\text{Allowable } L/d = 30 \times A_{sprov} / A_{sreq} = 30 \times \overset{314}{\cancel{286}} / 266.7 = \overset{314}{\cancel{32.25}} 35.32$$

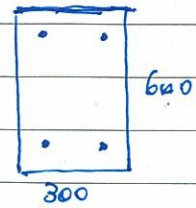
$$\text{Actual } L/d_x = 5000 / 145 = 34.5 < 35.32 \text{ (OK)}$$

4a) 1. Pure axial compression ($M=0$)

$$N_0 = 0.567 f_{ck} \cdot A_{col} + 0.87 f_{yk} A_{sc}$$

$$= 0.567 \times 25 \cdot 300 \times 600 + 0.87 (500) (300) (600) (0.02)$$

$$= 4117.5 \text{ kN} \quad \text{point 1 } (0, 4117.5)$$



2. Balanced condition of failure: $\epsilon_{cu} = 0.0035$, $d/h = 0.9$, $d = 540 \text{ mm}$, $d' = 60$

$$\epsilon_y = 0.87 \times 500 / 200000 = 0.00217$$

$$X_{bal} = \frac{d}{1 + \frac{\epsilon_y}{0.0035}} = \frac{540}{1 + \frac{0.00217}{0.0035}} = 333 \text{ mm}$$

check if the compression steel has yielded

$$\epsilon_{sc} = 0.0035 \left(\frac{x - d'}{x} \right) = 0.0035 \left(\frac{333 - 60}{333} \right) = 0.0029 > 0.0025 \rightarrow \text{yield}$$

$$F_{s1} = F_{s2} = 0.87 f_{yk} \times 300 \times 600 \times 0.02 = 1566000 \text{ N}$$

$$F_c = 0.567 f_{ck} \times 300 \times 0.8 X_{bal} = 1132866 \text{ N}$$

$$N = N_{bal} = F_c + F_{s1} - F_{s2} = 1132866 \text{ N} = 1132.9 \text{ kN}$$

$$M_{bal} = F_c (300 - 0.4 X_{bal}) + (F_{s1} + F_{s2}) (d - 300)$$

$$= 1132866 (300 - 0.4(333)) + (1566000 + 1132866) (540 - 300)$$

$$= 836.7 \text{ kNm}$$

point 2: (836.7, 1132.9)

3. Pure bending ($N=0$)

assume the compression steel has not yielded

$$\epsilon_{s1} = \frac{x - 60}{x} \times 0.0035$$

$$f_{s1} = \frac{x - 60}{x} \times 700$$

$$0.567 \times 25 \times 300 \times 0.8x + \left(\frac{x - 60}{x} \right) \times 1800 \times 700 = 0.87 \times 500 \times 1800$$

$$3402x + 1260000 \left(\frac{x - 60}{x} \right) = 783000$$

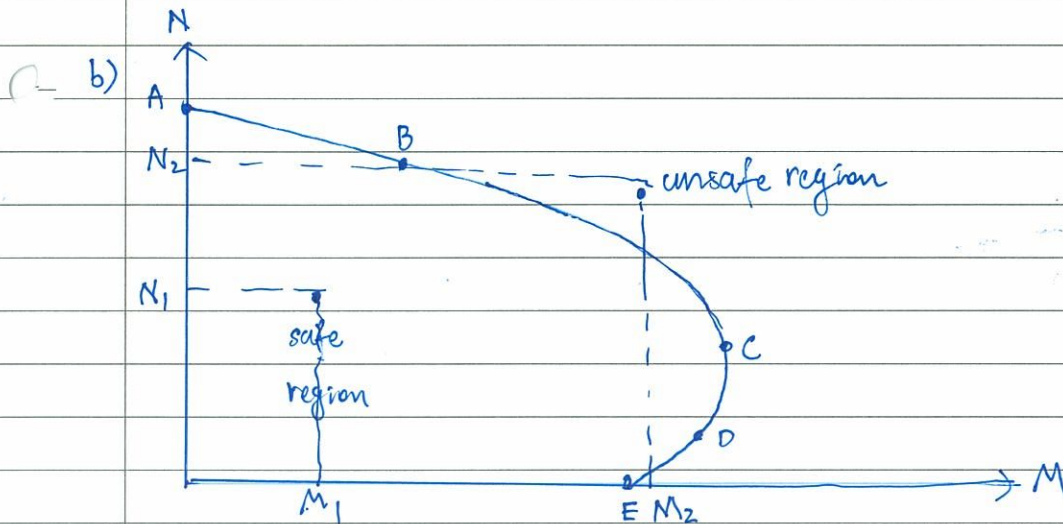
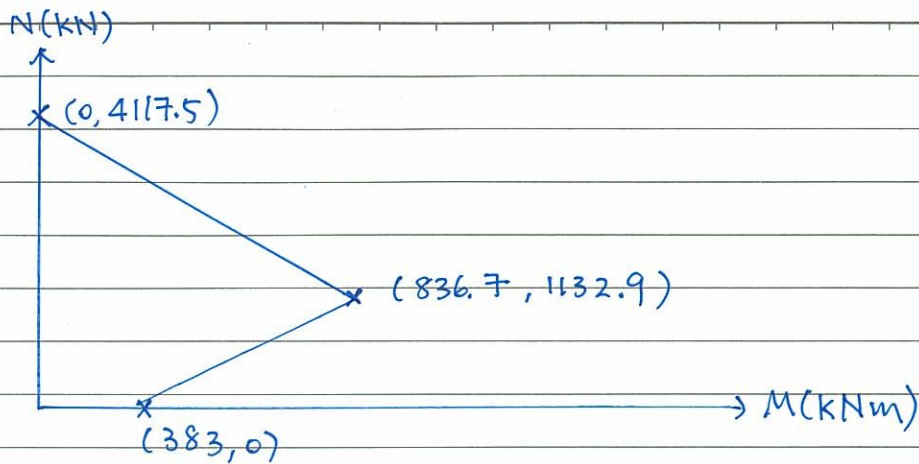
$$3402x^2 + 1260000x - 75600000 = 783000x$$

$$x = 774431 / 8184 = 94.6$$

$$f_{s1} = 256.15 \Rightarrow F_{s1} = 461077$$

$$M = F_c (d - 0.4x) + F_{s1} (d - 60) = 382.93 \text{ kNm}$$

point 3: (383, 0)



A-B: all zero tension

A-C: compression controlled failure, tension steel has not yielded, compression steel has yielded

C-E: tension controlled failure, tension steel has yielded, compression steel has not.

C: balanced failure in crushing of concrete (0.0035) and yielding of tensile steel (0.00217) at the same time

beyond pt C, $x < x_{bal}$

E: pure bending.

Umar