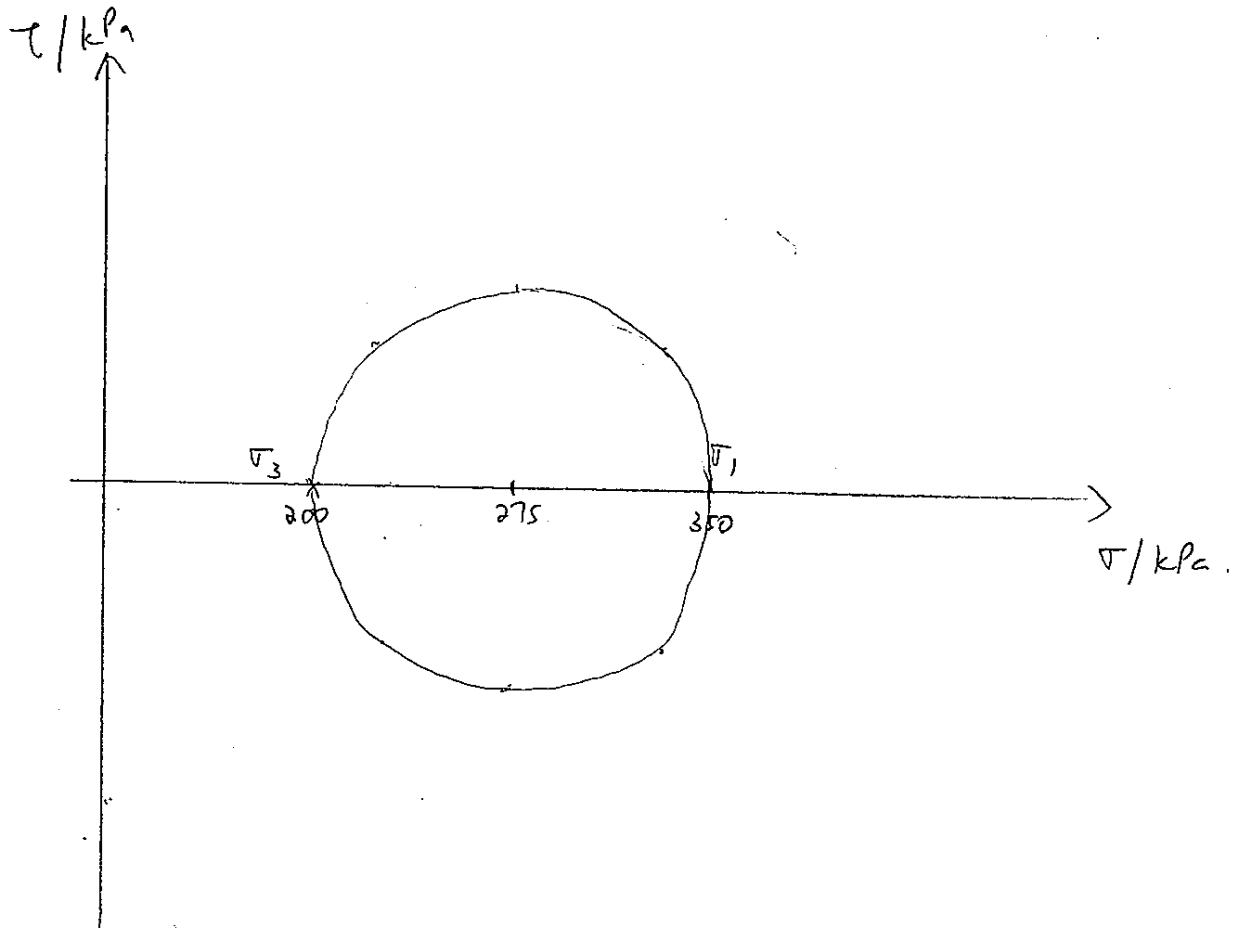


1a)

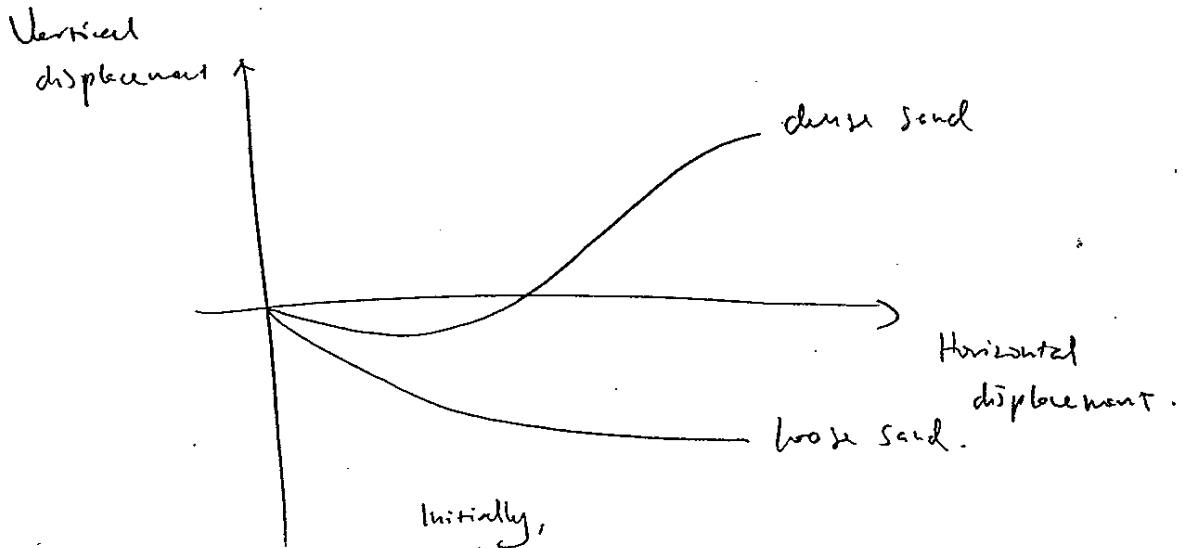


$$\sigma_1 - \sigma_3 = 350 - 200 = 150$$

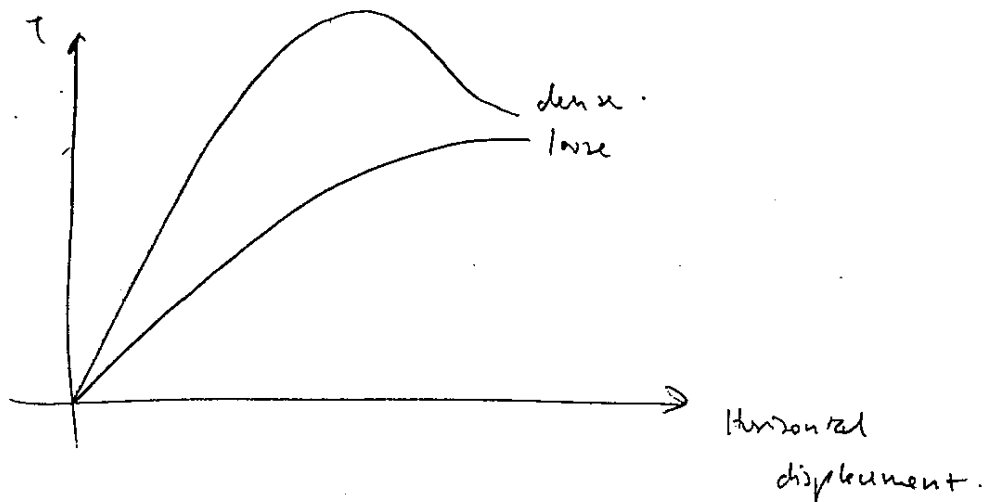
$$\text{Normal} = \frac{\sigma_1 + \sigma_3}{2} + \frac{\sigma_1 - \sigma_3}{2} \cos 2\theta = 395.55 \text{ kPa}$$

$$\text{Shear} = \frac{\sigma_1 - \sigma_3}{2} \sin 2\theta = 67.41 \text{ kPa}$$

b.



Initially,
 Dense sand: Downward displacement due to normal load. Later, experience dilation (expansion when sand particles go over each other).
 Loose sand: Experience contraction due to normal load.



Dense sand: Beyond peak τ , no additional shear stress needed to increase horizontal displacement.
 Loose sand: τ increase to ϕ constant value - shear stress as additional horizontal pressure needed to increase horizontal displacement.

k) i)

$$a_f = (B \times D) - (d \times B)$$

$$\sigma_f = \frac{N}{a_f}$$

$$\tau_f = \frac{F}{a_f}$$

Test	a_f (mm^2) $\times 10^{-3}$	τ_f (kPa)	σ_f (kPa)
1	3.15	73	100
2	3	126	200
3	2.766	179	300

Test 1:

$$60 \times 60 = 3600$$

$$7.5 \times 60 = 450$$

$$a_f = 3600 - 450 = 3.15 \times 10^3 \text{ mm}^2$$

$$\tau_f = \frac{270}{3.15 \times 10^{-3}} = 73.0 \text{ kPa}, \quad \sigma_f = \frac{315}{3.15 \times 10^{-3}} = 100 \text{ kPa}$$

$$1 \text{ mm}^2 = 0.001^2 = 1 \times 10^{-6} \text{ m}^2$$

Test 2:

$$a_f = 3600 - (10 \times 60) = 3 \times 10^3 \text{ mm}^2$$

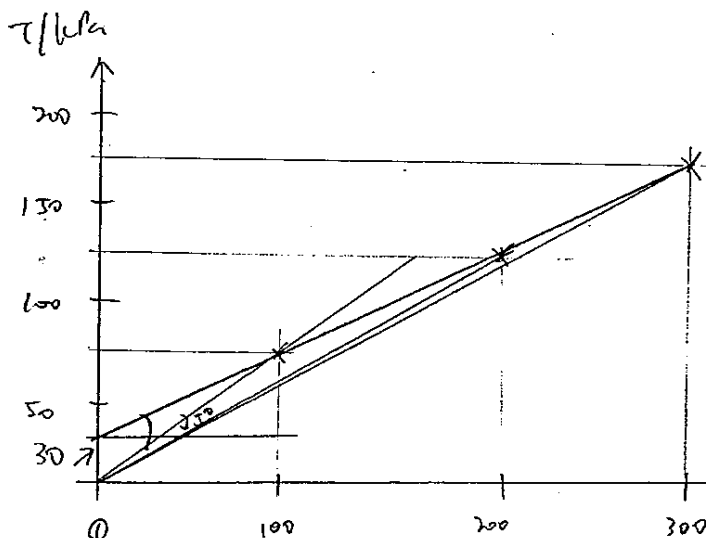
$$\tau_f = \frac{379}{3 \times 10^{-3}} = 126 \text{ kPa}, \quad \sigma_f = \frac{600}{3 \times 10^{-3}} = 200 \text{ kPa}$$

Test 3:

$$a_f = 3600 - (3.9 \times 60) = 2.766 \times 10^3$$

$$\tau_f = \frac{496}{2.766 \times 10^{-3}} = 179 \text{ kPa}$$

$$\sigma_f = \frac{830}{2.766 \times 10^{-3}} = 300 \text{ kPa}$$



from graph,

$$c' \approx 30 \text{ kPa}$$

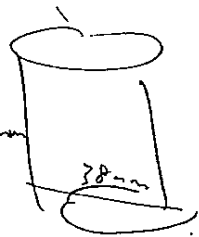
$$\phi' \approx 25^\circ$$

(c) ii) Secant ϕ' :

Test	
1	35°
2	29°
3	28°

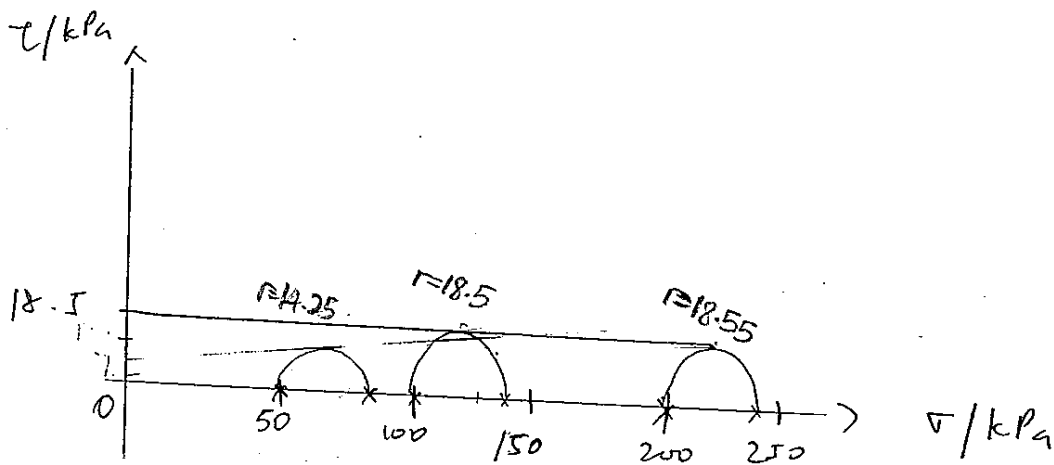
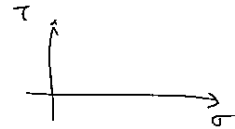
2b) i) $\epsilon_a = \frac{\Delta l}{l_0}$ $\epsilon_v = \frac{\Delta V}{V_0}$

σ_3	ϵ_a	$A = \frac{A_0}{1 - \epsilon_a}$	$\frac{N}{A}$ (kPa) $\sigma_1 - \sigma_3$	$(\sigma_1 - \sigma_3) + \sigma_3$ σ_1
50	0.067	1142	28.5	78.5
100	0.096	1254	37.0	137.0
200	0.121	1290	37.1	237.1



$V_0 = \frac{\pi (38)^2}{4} \times 76 = 86.2 \times 10^3 \text{ mm}^3$

$A_0 = \frac{\pi (38)^2}{4} = 1134 \text{ mm}^2$



Undrained shear strength of clay $\approx 18.5 \text{ kPa}$

~~45~~

2b) ii) Lower.

At deeper clay, pore water pressure increase,
effective stress decrease (total stress - pore pressure)
→ shear strength decrease.

Sand:

2c)

Normally consolidated soil ~~with $\phi' = 1$~~

$$K_0 = 1 - \sin \phi'$$

$$= 1 - \sin 28^\circ$$

$$= 0.531$$

$$\gamma_w = 9.81 \text{ kN/m}^3$$

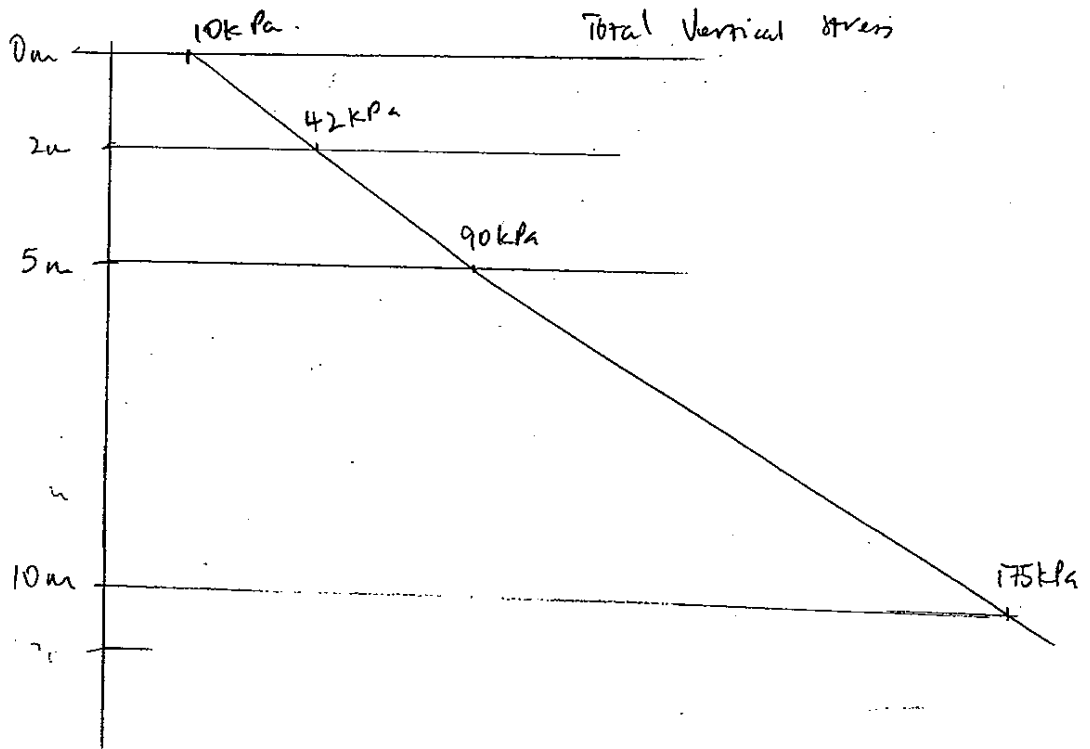
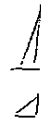
At depth $0m$, $\sigma_v = 10 \text{ kPa}$.

" $2m$, $\sigma_v = \frac{16}{10} \times 2 = \cancel{64 \text{ kPa}} \cdot \cancel{64 \text{ kPa}} = 42 \text{ kPa}$.

" $5m$, $\sigma_v = (16 \times 3) + 42 = 90 \text{ kPa}$

" $10m$, $\sigma_v = (5 \times 17) + 90 = 175 \text{ kPa}$

$$m = \frac{y}{x}$$



2c) continued.

Sand: $K_{o1} = 1 - \sin 28 = 0.531$

Dense sand: $K_{o2} = 1 - \sin 42 = 0.331$

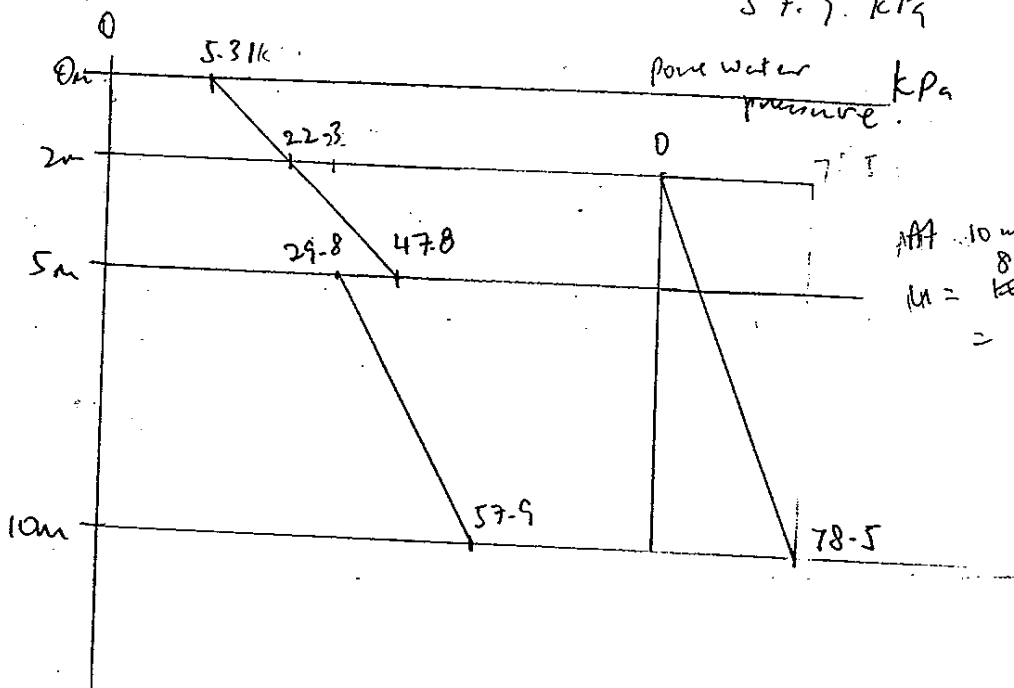
Depth 0m: $\sigma_h = K_{o1} \sigma_v = (0.531)(10) = 5.31 \text{ kPa}$

" 2m: $\sigma_h = K_{o1}(\sigma_v + \gamma z) = (0.531)(10 + 16(2)) = 22.3 \text{ kPa}$

" 5m: $\sigma_h = K_{o1}(\sigma_v + \gamma z) = (0.531)[(10)(3) + 22.3] = 47.8 \text{ kPa}$

(dense sand) $\sigma_h = K_{o2}(\sigma_v + \gamma z) = (0.331)(10 + 17(5)) = 29.8 \text{ kPa}$

" 10m: $\sigma_h = K_{o2}(\sigma_v + \gamma z) = (0.331)(5)(17) + 29.8 = 57.9 \text{ kPa}$



At 10m depth,
 $u = \frac{8}{10} \times 9.81 = 7.85 \text{ kPa}$

3b) continued.

$$\text{force // slip plane} = W \sin 25^\circ = (90 + 10m) \sin 25$$

For failure of slope:

$$W \sin 25 = \tau \times l_d$$
$$(90 + 10m) \sin 25 = 0.473 (90 + 10m) \times 1.10.$$

$$\Rightarrow 1 = \frac{[(1+m)(18) + m(20)(5)(\cos 25)^2 - m(5)(9.8)(\cos 25)^2] \tan 35}{[(1+m)(18) + m(50)] (5) \sin 25 \cos 25}$$

$$m = 0.5739$$

4a)

Soil compaction: Benefits:

- Increase unit weight of soil by reducing air.
- ~~Increased~~ ^{higher} unit weight increase soil normal stress.
- ~~the~~ higher normal stress increase shear strength of soil. ($\tau = c' + \sigma \tan \phi'$)

$$\tau = c' + \sigma$$

Compaction:

Applied stress to soil to cause air to be displaced (removed)

Consolidation:

~~Applied stress~~
stress applied to soil to cause water to be displaced (removed)

4b)

Field tests:

1. Find in-situ density using,
 - sand-cone method or
 - rubber bladder field density test.

Lab tests:

1. Relative density test (purpose: to find maximum & minimum density)
2. Grain size distribution test (purpose: find particle sizes in soil)
3. Water content test.